

# Accurate Online Posterior Alignments for Principled Lexically-Constrained Decoding

**Soumya Chatterjee**

IIT Bombay

soumya@cse.iitb.ac.in

**Sunita Sarawagi**

IIT Bombay

sunita@iitb.ac.in

**Preethi Jyothi**

IIT Bombay

pjyothi@cse.iitb.ac.in

## Abstract

Online alignment in machine translation refers to the task of aligning a target word to a source word when the target sequence has only been partially decoded. Good online alignments facilitate important applications such as lexically constrained translation where user-defined dictionaries are used to inject lexical constraints into the translation model. We propose a novel posterior alignment technique that is truly online in its execution and superior in terms of alignment error rates compared to existing methods. Our proposed inference technique jointly considers alignment and token probabilities in a principled manner and can be seamlessly integrated within existing constrained beam-search decoding algorithms. On five language pairs, including two distant language pairs, we achieve consistent drop in alignment error rates. When deployed on seven lexically constrained translation tasks, we achieve significant improvements in BLEU specifically around the constrained positions.

## 1 Introduction

Online alignment seeks to align a target word to a source word at the decoding step when the word is output in an auto-regressive neural translation model (Kalchbrenner and Blunsom, 2013; Cho et al., 2014; Sutskever et al., 2014). This is unlike the more popular offline alignment task that uses the entire target sentence (Och and Ney, 2003). State of the art methods of offline alignment based on matching of whole source and target sentences (Jalili Sabet et al., 2020; Dou and Neubig, 2021) are not applicable for online alignment where we need to commit on the alignment of a target word based on only the generated prefix thus far.

An important application of online alignment is lexically constrained translation which allows injection of domain-specific terminology and other phrasal constraints during decoding (Hasler et al.,

2018; Hokamp and Liu, 2017; Alkhouli et al., 2018; Crego et al., 2016). Other applications include preservation of markups between the source and target (Müller, 2017), and supporting source word edits in summarization (Shen et al., 2019). These applications need to infer the specific source token which aligns with output token. Thus, alignment and translation is to be done simultaneously.

Existing online alignment methods can be categorized into Prior and Posterior alignment methods. Prior alignment methods (Garg et al., 2019; Song et al., 2020) extract alignment based on the attention at time step  $t$  when outputting token  $y_t$ . The attention probabilities at time-step  $t$  are conditioned on tokens output before time  $t$ . Thus, the alignment is estimated *prior* to observing  $y_t$ . Naturally, the quality of alignment can be improved if we condition on the target token  $y_t$  (Shankar and Sarawagi, 2019). This motivated Chen et al. (2020) to propose a posterior alignment method where alignment is calculated from the attention probabilities at the next decoder step  $t + 1$ . While alignment quality improved as a result, their method is not truly online since it does not generate alignment *synchronously* with the token. The delay of one step makes it difficult and cumbersome to incorporate terminology constraints during beam decoding.

We propose a truly online posterior alignment method that provides higher alignment accuracy than existing online methods, while also being synchronous. Because of that we can easily integrate posterior alignment to improve lexicon-constrained translation in state of the art constrained beam-search algorithms such as VDBA (Hu et al., 2019). Our method (Align-VDBA) presents a significant departure from existing papers on alignment-guided constrained translation (Chen et al., 2020; Song et al., 2020) that employ a greedy algorithm with poor constraint satisfaction rate (CSR). For example, on a ja $\rightarrow$ en their CSR is 20 points lower than ours. Moreover, the latter does not benefit

from larger beam sizes unlike VDBA-based methods that significantly improve with larger beam widths. Compared to [Chen et al. \(2020\)](#), our method improves average overall BLEU scores by 1.2 points and average BLEU scores around the constrained span by up to 9 points. In the evaluations performed in these earlier work, VDBA was not allocated the slightly higher beam size needed to pro-actively enforce constraints without compromising BLEU. Compared to [Hu et al. \(2019\)](#) (VDBA), this paper’s contributions include online alignments and their use in more fluent constraint placement and efficient allocation of beams.

### Contributions

- A truly online posterior alignment method that integrates into existing NMT systems via a trainable light-weight module.
- Higher online alignment accuracy on five language pairs including two distant language pairs where we improve over the best existing method in seven out of ten translation tasks.
- Principled method of modifying VDBA to incorporate posterior alignment probabilities in lexically-constrained decoding. VDBA enforces constraints ignoring source alignments; our change (Align-VDBA) leads to more fluent constraint placement and significant BLEU increase particularly for smaller beams.
- Establishing that VDBA-based pro-active constrained inference should be preferred over prevailing greedy alignment-guided inference ([Chen et al., 2021](#); [Song et al., 2020](#)). Further, VDBA and our Align-VDBA inference with beam size 10 provide 1.2 BLEU increase over these methods with the same beam size.

## 2 Posterior Online Alignment

Given a sentence  $\mathbf{x} = x_1, \dots, x_S$  in the source language and a sentence  $\mathbf{y} = y_1, \dots, y_T$  in the target language, an alignment  $\mathcal{A}$  between the word strings is a subset of the Cartesian product of the word positions ([Brown et al., 1993](#); [Och and Ney, 2003](#)):  $\mathcal{A} \subseteq \{(s, t) : s = 1, \dots, S; t = 1, \dots, T\}$  such that the aligned words can be considered translations of each other. An online alignment at time-step  $t$  commits on alignment of the  $t^{\text{th}}$  output token conditioned only on  $\mathbf{x}$  and  $\mathbf{y}_{<t} = y_1, y_2, \dots, y_{t-1}$ . Additionally, if token  $y_t$  is also available we call it a posterior online alignment. We seek to embed online alignment with existing NMT systems. We will first briefly describe the architecture of state

of the art NMT systems. We will then elaborate on how alignments are computed from attention distributions in prior work and highlight some limitations, before describing our proposed approach.

### 2.1 Background

Transformers ([Vaswani et al., 2017](#)) adopt the popular encoder-decoder paradigm used for sequence-to-sequence modeling ([Cho et al., 2014](#); [Sutskever et al., 2014](#); [Bahdanau et al., 2015](#)). The encoder and decoder are both multi-layered networks with each layer consisting of a multi-headed self-attention and a feedforward module. The decoder layers additionally use multi-headed attention to encoder states. We elaborate on this mechanism next since it plays an important role in alignments.

#### 2.1.1 Decoder-Encoder Attention in NMTs

The encoder transforms the  $S$  input tokens into a sequence of token representations  $\mathbf{H} \in \mathbb{R}^{S \times d}$ . Each decoder layer (indexed by  $\ell \in \{1, \dots, L\}$ ) computes multi-head attention over  $\mathbf{H}$  by aggregating outputs from a set of  $\eta$  independent attention heads. The attention output from a single head  $n \in \{1, \dots, \eta\}$  in decoder layer  $\ell$  is computed as follows. Let the output of the self-attention sub-layer in decoder layer  $\ell$  at the  $t^{\text{th}}$  target token be denoted as  $\mathbf{g}_t^\ell$ . Using three projection matrices  $\mathbf{W}_Q^{\ell,n}, \mathbf{W}_V^{\ell,n}, \mathbf{W}_K^{\ell,n} \in \mathbb{R}^{d \times d_n}$ , the query vector  $\mathbf{q}_t^{\ell,n} \in \mathbb{R}^{1 \times d_n}$  and key and value matrices,  $\mathbf{K}^{\ell,n} \in \mathbb{R}^{S \times d_n}$  and  $\mathbf{V}^{\ell,n} \in \mathbb{R}^{S \times d_n}$ , are computed using the following projections:  $\mathbf{q}_t^{\ell,n} = \mathbf{g}_t^\ell \mathbf{W}_Q^{\ell,n}$ ,  $\mathbf{K}^{\ell,n} = \mathbf{H} \mathbf{W}_K^{\ell,n}$ , and  $\mathbf{V}^{\ell,n} = \mathbf{H} \mathbf{W}_V^{\ell,n}$ .<sup>1</sup> These are used to calculate the attention output from head  $n$ ,  $\mathbf{Z}_t^{\ell,n} = P(\mathbf{a}_t^{\ell,n} | \mathbf{x}, \mathbf{y}_{<t}) \mathbf{V}^{\ell,n}$ , where:

$$P(\mathbf{a}_t^{\ell,n} | \mathbf{x}, \mathbf{y}_{<t}) = \text{softmax} \left( \frac{\mathbf{q}_t^{\ell,n} (\mathbf{K}^{\ell,n})^\top}{\sqrt{d}} \right) \quad (1)$$

For brevity, the conditioning on  $\mathbf{x}, \mathbf{y}_{<t}$  is dropped and  $P(\mathbf{a}_t^{\ell,n})$  is used to refer to  $P(\mathbf{a}_t^{\ell,n} | \mathbf{x}, \mathbf{y}_{<t})$  in the following sections.

Finally, the multi-head attention output is given by  $[\mathbf{Z}_t^{\ell,1}, \dots, \mathbf{Z}_t^{\ell,\eta}] \mathbf{W}^O$  where  $[\ ]$  denotes the column-wise concatenation of matrices and  $\mathbf{W}^O \in \mathbb{R}^{d \times d}$  is an output projection matrix.

#### 2.1.2 Alignments from Attention

Several prior work have proposed to extract word alignments from the above attention prob-

<sup>1</sup> $d_n$  is typically set to  $\frac{d}{\eta}$  so that a multi-head attention layer does not introduce more parameters compared to a single head attention layer.

abilities. For example Garg et al. (2019) propose a simple method called NAIVEATT that aligns a source word to the  $t^{\text{th}}$  target token using  $\text{argmax}_j \frac{1}{\eta} \sum_{n=1}^{\eta} P(a_{t,j}^{\ell,n} | \mathbf{x}, \mathbf{y}_{<t})$  where  $j$  indexes the source tokens. In NAIVEATT, we note that the attention probabilities  $P(a_{t,j}^{\ell,n} | \mathbf{x}, \mathbf{y}_{<t})$  at decoding step  $t$  are not conditioned on the current output token  $y_t$ . Alignment quality would benefit from conditioning on  $y_t$  as well. This observation prompted Chen et al. (2020) to extract alignment of token  $y_t$  using attention  $P(a_{t,j}^{\ell,n} | \mathbf{x}, \mathbf{y}_{\leq t})$  computed at time step  $t + 1$ . The asynchronicity inherent to this shift-by-one approach (SHIFTATT) makes it difficult and more computationally expensive to incorporate lexical constraints during beam decoding.

## 2.2 Our Proposed Method: POSTALN

We propose POSTALN that produces posterior alignments synchronously with the output tokens, while being more computationally efficient compared to previous approaches like SHIFTATT. We incorporate a lightweight alignment module to convert prior attention to posterior alignments in the same decoding step as the output. Figure 1 illustrates how this alignment module fits within the standard Transformer architecture.

The alignment module is placed at the penultimate decoder layer  $\ell = L - 1$  and takes as input (1) the encoder output  $\mathbf{H}$ , (2) the output of the self-attention sub-layer of decoder layer  $\ell$ ,  $\mathbf{g}_t^\ell$  and, (3) the embedding of the decoded token  $\mathbf{e}(y_t)$ . Like in standard attention it projects  $\mathbf{H}$  to obtain a key matrix, but to obtain the query matrix it uses both decoder state  $\mathbf{g}_t^\ell$  (that summarizes  $\mathbf{y}_{<t}$ ) and  $\mathbf{e}(y_t)$  to compute the posterior alignment  $P(\mathbf{a}_t^{\text{post}})$  as:

$$P(\mathbf{a}_t^{\text{post}}) = \frac{1}{\eta} \sum_{n=1}^{\eta} \text{softmax} \left( \frac{\mathbf{q}_{t,\text{post}}^n (\mathbf{K}_{\text{post}}^n)^\top}{\sqrt{d}} \right),$$

$$\mathbf{q}_{t,\text{post}}^n = [\mathbf{g}_t^\ell, \mathbf{e}(y_t)] \mathbf{W}_{Q,\text{post}}^n, \quad \mathbf{K}_{\text{post}}^n = \mathbf{H} \mathbf{W}_{K,\text{post}}^n$$

Here  $\mathbf{W}_{Q,\text{post}}^n \in \mathbb{R}^{2d \times d_n}$  and  $\mathbf{W}_{K,\text{post}}^n \in \mathbb{R}^{d \times d_n}$ .

This computation is synchronous with producing the target token  $y_t$ , thus making it compatible with beam search decoding (as elaborated further in Section 3). It also accrues minimal computational overhead since  $P(\mathbf{a}_t^{\text{post}})$  is defined using  $\mathbf{H}$  and  $\mathbf{g}_t^{L-1}$ , that are both already cached during a standard decoding pass. Note that if the query vector  $\mathbf{q}_{t,\text{post}}^n$  is computed using only  $\mathbf{g}_t^{L-1}$ , without concatenating  $\mathbf{e}(y_t)$ , then we get prior alignments

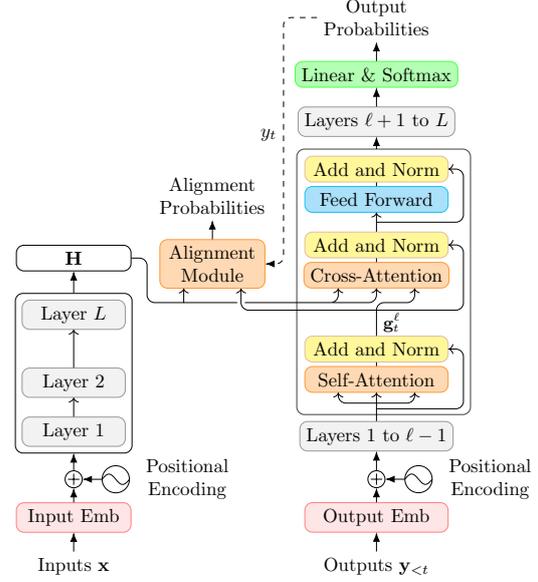


Figure 1: Our alignment module is an encoder-decoder attention sub-layer, similar to the existing cross-attention sub-layer. It takes as inputs the encoder output  $\mathbf{H}$  as the key, and the concatenation of the output of the previous self-attention layer  $\mathbf{g}_t^\ell$  and the currently decoded token  $y_t$  as the query, and outputs posterior alignment probabilities  $\mathbf{a}_t^{\text{post}}$ .

that we refer to as PRIORATT. In our experiments, we explicitly compare PRIORATT with POSTALN to show the benefits of using  $y_t$  in deriving alignments while keeping the rest of the architecture intact.

**Training** Our posterior alignment sub-layer is trained using alignment supervision, while freezing the rest of the translation model parameters. Specifically, we train a total of  $3d^2$  additional parameters across the matrices  $\mathbf{W}_{K,\text{post}}^n$  and  $\mathbf{W}_{Q,\text{post}}^n$ . Since gold alignments are very tedious and expensive to create for large training datasets, alignment labels are typically obtained using existing techniques. We use bidirectional symmetrized SHIFTATT alignments, denoted by  $S_{i,j}$  that refers to an alignment between the  $i^{\text{th}}$  target word and the  $j^{\text{th}}$  source word, as reference labels to train our alignment sub-layer. Then the objective (following Garg et al. (2019)) can be defined as:

$$\mathbf{W}_{Q,\text{post}}^n \max_{\mathbf{W}_{K,\text{post}}^n} \frac{1}{T} \sum_{i=1}^T \sum_{j=1}^S S_{i,j} \log(P(a_{i,j}^{\text{post}} | \mathbf{x}, \mathbf{y}_{\leq i}))$$

Next, we demonstrate the role of posterior online alignments on an important downstream task.

### 3 Lexicon Constrained Translation

In the lexicon constrained translation task, for each to-be-translated sentence  $\mathbf{x}$ , we are given a set of source text spans and the corresponding target tokens in the translation. A constraint  $\mathcal{C}_j$  comprises a pair  $(\mathcal{C}_j^x, \mathcal{C}_j^y)$  where  $\mathcal{C}_j^x = (p_j, p_j + 1 \dots, p_j + \ell_j)$  indicates input token positions, and  $\mathcal{C}_j^y = (y_1^j, y_2^j \dots, y_{m_j}^j)$  denote target tokens that are translations of the input tokens  $x_{p_j} \dots x_{p_j + \ell_j}$ . For the output tokens we do not know their positions in the target sentence. The different constraints are non-overlapping and each is expected to be used exactly once. The goal is to translate the given sentence  $\mathbf{x}$  and satisfy as many constraints in  $\mathcal{C} = \bigcup_j \mathcal{C}_j$  as possible while ensuring fluent and correct translations. Since the constraints do not specify target token position, it is natural to use online alignments to guide when a particular constraint is to be enforced.

#### 3.1 Background: Constrained Decoding

Existing inference algorithms for incorporating lexicon constraints differ in how pro-actively they enforce the constraints. A passive method is used in Song et al. (2020) where constraints are enforced only when the prior alignment is at a constrained source span. Specifically, if at decoding step  $t$ ,  $i = \operatorname{argmax}_{i'} P(a_{t,i'})$  is present in some constraint  $\mathcal{C}_j^x$ , the output token is fixed to the first token  $y_1^j$  from  $\mathcal{C}_j^y$ . Otherwise, the decoding proceeds as usual. Also, if the translation of a constraint  $\mathcal{C}_j$  has started, the same is completed ( $y_2^j$  through  $y_{m_j}^j$ ) for the next  $m_j - 1$  decoding steps before resuming unconstrained beam search. The pseudocode for this method is provided in Appendix G.

For the posterior alignment methods of Chen et al. (2020) this leads to a rather cumbersome inference (Chen et al., 2021). First, at step  $t$  they predict a token  $\hat{y}_t$ , then start decoding step  $t + 1$  with  $\hat{y}_t$  as input to compute the posterior alignment from attention at step  $t + 1$ . If the maximum alignment is to the constrained source span  $\mathcal{C}_j^x$  they *revise* the output token to be  $y_1^j$  from  $\mathcal{C}_j^y$ , but the output score for further beam-search continues to be of  $\hat{y}_t$ . In this process both the posterior alignment and token probabilities are misrepresented since they are both based on  $\hat{y}_t$  instead of the finally output token  $y_1^j$ . The decoding step at  $t + 1$  needs to be restarted after the revision. The overall algorithm continues to be normal beam-search, which implies that the constraints are not enforced pro-actively.

Many prior methods have proposed more proactive methods of enforcing constraints, including the Grid Beam Search (GBA, Hokamp and Liu (2017)), Dynamic Beam Allocation (DBA, Post and Vilar (2018)) and Vectorized Dynamic Beam Allocation (VDBA, Hu et al. (2019)). The latest of these, VDBA, is efficient and available in public NMT systems (Ott et al., 2019; Hieber et al., 2020). Here multiple *banks*, each corresponding to a particular number of completed constraints, are maintained. At each decoding step, a hypothesis can either start a new constraint and move to a new bank or continue in the same bank (either by not starting a constraint or progressing on a constraint mid-completion). This allows them to achieve near 100% enforcement. However, VDBA enforces the constraints by considering only the target tokens of the lexicon and totally ignores the alignment of these tokens to the source span. This could lead to constraints being placed at unnatural locations leading to loss of fluency. Examples appear in Table 4 where we find that VDBA just attaches the constrained tokens at the end of the sentence.

#### 3.2 Our Proposal: Align-VDBA

We modify VDBA with alignment probabilities to better guide constraint placement. The score of a constrained token is now the joint probability of the token, and the probability of the token being aligned with the corresponding constrained source span. Formally, if the current token  $y_t$  is a part of the  $j^{\text{th}}$  constraint *i.e.*  $y_t \in \mathcal{C}_j^y$ , the generation probability of  $y_t$ ,  $P(y_t | \mathbf{x}, \mathbf{y}_{<t})$  is scaled by multiplying with the alignment probabilities of  $y_t$  with  $\mathcal{C}_j^x$ , the source span for constraint  $i$ . Thus, the updated probability is given by:

$$\underbrace{P(y_t, \mathcal{C}_j^x | \mathbf{x}, \mathbf{y}_{<t})}_{\text{Joint Prob}} = \underbrace{P(y_t | \mathbf{x}, \mathbf{y}_{<t})}_{\text{Token Prob}} \underbrace{\sum_{r \in \mathcal{C}_j^x} P(a_{t,r}^{\text{post}} | \mathbf{x}, \mathbf{y}_{<t})}_{\text{Src Align. Prob.}} \quad (2)$$

$P(y_t, \mathcal{C}_j^x | \mathbf{x}, \mathbf{y}_{<t})$  denotes the joint probability of outputting the constrained token and the alignment being on the corresponding source span. Since the supervision for the alignment probabilities was noisy, we found it useful to recalibrate the alignment distribution using a temperature scale  $T$ , so that the recalibrated probability is  $\propto \Pr(a_{t,r}^{\text{post}} | \mathbf{x}, \mathbf{y}_{<t})^{\frac{1}{T}}$ . We used  $T = 2$  *i.e.*, square-root of the alignment probability.

Align-VDBA also uses posterior alignment probabilities to also improve the efficiency of VDBA.

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**Algorithm 1** Align-VDBA: Modifications to DBA shown in blue. (Adapted from Post and Vilar (2018))

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1: Inputs beam:  $K$  hypothesis in beam, scores:  $K \times |V_T|$  matrix of scores where scores[ $k, y$ ] denotes the score of  $k^{\text{th}}$  hypothesis extended with token  $y$  at this step, constraints:  $\{(C_j^x, C_j^y)\}$ , threshold
2: candidates  $\leftarrow [(k, y, \text{scores}[k, y], \text{beam}[k].\text{constraints.add}(y)) \text{ for } k, y \text{ in ARGMAX\_K}(\text{scores})$ 
3: for  $1 \leq k \leq K$  do ▷ Go over current beam
4:   for all  $y \in V_T$  that are unmet constraints for beam[ $k$ ] do ▷ Expand new constraints
5:     alignProb  $\leftarrow \Sigma_{\text{constraint\_xs}(y)} \text{POSTALN}(k, y)$  ▷ Modification in blue (Eqn (2))
6:     if alignProb > threshold then
7:       candidates.append( ( $k, y, \text{scores}[k, y] \times \text{alignProb}$ ), beam[ $k$ ].constraints.add( $y$ ) )
8:       candidates.append( ( $k, y, \text{scores}[k, y]$ , beam[ $k$ ].constraints.add( $y$ ) ) ) ▷ Original DBA Alg.
9:    $w = \text{ARGMAX}(\text{scores}[k, :])$ 
10:  candidates.append( ( $k, w, \text{scores}[k, w]$ , beam[ $k$ ].constraints.add( $w$ ) ) ) ▷ Best single word
11: newBeam  $\leftarrow \text{ALLOCATE}(\text{candidates}, K)$ 
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Currently, VDBA attempts beam allocation for each unmet constraint since it has no way to discriminate. In Align-VDBA we allocate only when the alignment probability is greater than a threshold. When the beam size is small (say 5) this yields higher accuracy due to more efficient beam utilization. We used a threshold of 0.1 for all language pairs other than ro→en for which a threshold of 0.3 was used. Further, the thresholds were used for the smaller beam size of 5 and not for larger beam sizes of 10 and 20.

We present the pseudocode of our modification (steps 5, 6 and 7, in blue) to DBA in Algorithm 1. Other details of the algorithm including the handling of constraints and the allocation steps (step 11) are involved and we refer the reader to Post and Vilar (2018) and Hu et al. (2019) to understand these details. The point of this code is to show that our proposed posterior alignment method can be easily incorporated into these algorithms so as to provide a more principled scoring of constrained hypothesis in a beam than the ad hoc revision-based method of Chen et al. (2021). Additionally, posterior alignments lead to better placement of constraints than in the original VDBA algorithm.

## 4 Experiments

We first compare our proposed posterior online alignment method on quality of alignment against existing methods in Section 4.2, and in Section 4.3, we demonstrate the impact of the improved alignment on the lexicon-constrained translation task.

### 4.1 Setup

We deploy the fairseq toolkit (Ott et al., 2019) and use transformer\_iwslt\_de\_en pre-configured model for all our experiments. Other configuration parameters include: Adam optimizer with  $\beta_1 = 0.9$ ,  $\beta_2 = 0.98$ , a learning rate of  $5e-4$

	de-en	en-fr	ro-en	en-hi	ja-en
Training	1.9M	1.1M	0.5M	1.6M	0.3M
Validation	994	1000	999	25	1166
Test	508	447	248	140	1235

Table 1: Number of sentence pairs for the five datasets used. Note that gold alignments are available only for the handful of sentence pairs in the test set.

with 4000 warm-up steps, an inverse square root schedule, weight decay of  $1e-4$ , label smoothing of 0.1, 0.3 probability dropout and a batch size of 4500 tokens. The transformer models are trained for 50,000 iterations. Then, the alignment module is trained for 10,000 iterations, keeping the other model parameters fixed. A joint byte pair encoding (BPE) is learned for the source and the target languages with 10k merge operation (Sennrich et al., 2016) using subword-nmt.

All experiments were done on a single 11GB Nvidia GeForce RTX 2080 Ti GPU on a machine with 64 core Intel Xeon CPU and 755 GB memory. The vanilla Transformer models take between 15 to 20 hours to train for different datasets. Starting from the alignments extracted from these models, the POSTALN alignment module trains in about 3 to 6 hours depending on the dataset.

### 4.2 Alignment Task

We evaluate online alignments on ten translation tasks spanning five language pairs. Three of these are popular in alignment papers (Zenkel et al., 2019): German-English (de-en), English-French (en-fr), Romanian-English (ro-en). These are all European languages that follow the same subject-verb-object (SVO) ordering. We also present results on two distant language pairs, English-Hindi (en-hi) and English-Japanese (ja-en), that follow a SOV word order which is different from the SVO

Method	Delay	de-en		en-fr		ro-en		en-hi		ja-en	
		de→en	en→de	en→fr	fr→en	ro→en	en→ro	en→hi	hi→en	ja→en	en→ja
Statistical Methods (Not Online)											
GIZA++ (Och and Ney, 2003)	End	18.9	19.7	7.3	7.0	27.6	28.3	35.9	36.4	41.8	39.0
FastAlign (Dyer et al., 2013)	End	28.4	32.0	16.4	15.9	33.8	35.5	-	-	-	-
No Alignment Training											
NAIVEATT (Garg et al., 2019)	0	32.4	40.0	24.0	31.2	37.3	33.2	49.1	53.8	62.2	63.5
SHIFTATT (Chen et al., 2020)	+1	20.0	22.9	14.7	20.4	26.9	27.4	35.3	38.6	53.6	48.6
With Alignment Training											
PRIORATT	0	23.4	25.8	14.0	16.6	29.3	27.2	36.4	35.1	52.7	50.9
SHIFTAET (Chen et al., 2020)	+1	15.8	<b>19.5</b>	10.3	<b>10.4</b>	22.4	23.7	29.3	29.3	42.5	<b>41.9</b>
POSTALN [Ours]	0	<b>15.5</b>	<b>19.5</b>	<b>9.9</b>	<b>10.4</b>	<b>21.8</b>	<b>23.2</b>	<b>28.7</b>	<b>28.9</b>	<b>41.2</b>	42.2

Table 2: AER for de-en, en-fr, ro-en, en-hi, ja-en language pairs. “Delay” indicates the decoding step at which the alignment of the target token is available. NAIVEATT, PRIORATT and POSTALN are truly online and output alignment at the same time step (delay=0), while SHIFTATT and SHIFTAET output one decoding step later.

word order of English. Data statistics are shown in Table 1 and details are in Appendix C.

**Evaluation Method:** For evaluating alignment performance, it is necessary that the target sentence is exactly the same as for which the gold alignments are provided. Thus, for the alignment experiments, we force the output token to be from the gold target and only infer the alignment. We then report the Alignment Error Rate (AER) (Och and Ney, 2000) between the gold alignments and the predicted alignments for different methods. Though our focus is online alignment, for comparison to previous works, we also report results on bidirectional symmetrized alignments in Appendix D.

**Methods compared:** We compare our method with both existing statistical alignment models, namely GIZA++ (Och and Ney, 2003) and FastAlign (Dyer et al., 2013), and recent Transformer-based alignment methods of Garg et al. (2019) (NAIVEATT) and Chen et al. (2020) (SHIFTATT and SHIFTAET). Chen et al. (2020) also propose a variant of SHIFTATT called SHIFTAET that delays computations by one time-step as in SHIFTATT, and additionally includes a learned attention sub-layer to compute alignment probabilities. We also present results on PRIORATT which is similar to POSTALN but does not use  $y_t$ .

**Results:** The alignment results are shown in Table 2. First, AERs using statistical methods FastAlign and GIZA++ are shown. Here, for fair comparison, the IBM models used by GIZA++ are trained on the same sub-word units as the Transformer models and sub-word alignments are converted to word level alignments for AER calculations. (GIZA++ has remained a state-of-the-art alignment technique and continues to be compared against.) Next, we present alignment results for two vanilla

Transformer models - NAIVEATT and SHIFTATT - that do not train a separate alignment module. The high AER of NAIVEATT shows that attention-as-is is very distant from alignment but posterior attention is closer to alignments than prior. Next we look at methods that train alignment-specific parameters: PRIORATT, a prior attention method; SHIFTAET and POSTALN, both posterior alignment methods. We observe that with training even PRIORATT has surpassed non-trained posterior. The posterior attention methods outperform the prior attention methods by a large margin, with an improvement of 4.0 to 8.0 points. Within each group, the methods with a trained alignment module outperform the ones without by a huge margin. POSTALN performs better or matches the performance of SHIFTAET (achieving the lowest AER in nine out of ten cases in Table 2) while avoiding the one-step delay in alignment generation. Even on the distant languages, POSTALN achieves significant reductions in error. For ja→en, we achieve a 1.3 AER reduction compared to SHIFTAET which is not a truly online method. Figure 2 shows examples to illustrate the superior alignments of POSTALN compared to NAIVEATT and PRIORATT.

### 4.3 Impact of POSTALN on Lexicon-Constrained Translation

We next depict the impact of improved AERs from our posterior alignment method on a downstream lexicon-constrained translation task. Following previous work (Hokamp and Liu, 2017; Post and Vilar, 2018; Song et al., 2020; Chen et al., 2020, 2021), we extract constraints using the gold alignments and gold translations. Up to three constraints of up to three words each are used for each sentence. Spans correctly translated by a greedy decoding

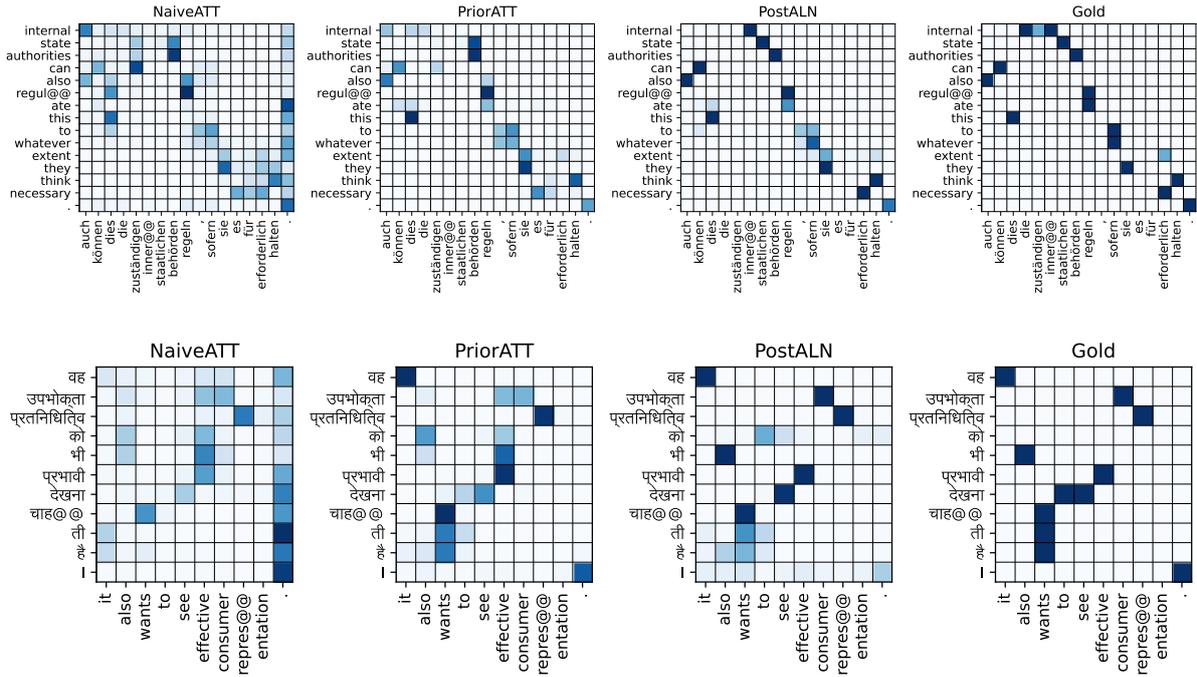


Figure 2: Alignments for de→en (top-row) and en→hi (bottom-row) by NAIVEATT, PRIORATT, and POSTALN. Note that POSTALN is most similar to Gold alignments in the last column.

Method	de→en				en→fr				ro→en				en→hi				ja→en			
	BLEU-C	CSR	BLEU	Time																
No constraints	0.0	4.6	32.9	87	0.0	8.7	34.8	64	0.0	8.8	33.4	47	0.0	6.3	19.7	21	0.0	8.8	18.9	237
NAIVEATT	28.7	86.1	36.6	147	36.5	88.0	38.3	93	33.3	92.3	36.5	99	22.5	88.4	23.6	27	15.1	75.9	20.2	315
PRIORATT	35.0	92.8	37.6	159	42.1	94.4	38.9	97	36.0	91.2	37.2	100	27.2	91.5	24.4	28	16.7	79.7	20.4	326
SHIFTATT	41.0	96.6	38.7	443	45.0	93.5	38.7	239	39.2	94.2	37.4	241	23.2	78.7	21.9	58	15.2	72.7	19.3	567
SHIFTAET	43.1	97.5	<b>39.1</b>	458	46.6	94.3	39.0	235	40.8	94.4	37.6	263	24.3	80.2	22.0	62	18.1	75.9	19.7	596
POSTALN	42.7	97.2	39.0	399	46.3	94.1	38.7	218	40.0	93.5	37.4	226	23.8	79.0	22.0	47	18.2	75.7	19.7	460
VDBA	<b>44.5</b>	98.9	38.5	293	51.9	98.5	39.5	160	43.1	99.1	37.9	165	29.8	92.3	24.5	49	24.3	95.6	21.6	494
Align-VDBA	<b>44.5</b>	98.6	38.6	357	<b>52.9</b>	98.4	<b>39.7</b>	189	<b>44.1</b>	98.9	<b>38.1</b>	203	<b>30.5</b>	91.5	<b>24.7</b>	70	<b>25.1</b>	95.5	<b>21.8</b>	630

Table 3: Constrained translation results showing BLEU-C, CSR (Constraint Satisfaction Rate), BLEU scores and total decoding time (in seconds) for the test set. Align-VDBA has the highest BLEU-C on all datasets.

are not selected as constraints.

**Metrics:** Following prior work (Song et al., 2020), we report BLEU (Papineni et al., 2002), time to translate all test sentences, and Constraint Satisfaction Rate (CSR). However, since it is trivial to get 100% CSR by always copying, we report another metric to evaluate the appropriateness of constraint placement: We call this measure BLEU-C and compute it as the BLEU of the constraint (when satisfied) and a window of three words around it. All numbers are averages over five different sets of randomly sampled constraint sets. The beam size is set to ten by default; results for other beam sizes appear in Appendix E.

**Methods Compared:** First we compare all the alignment methods presented in Section 4.2 on the constrained translation task using the alignment based token-replacement algorithm of Song et al.

(2020) described in Section 3.1. Next, we present a comparison between VBDA (Hu et al., 2019) and our modification Align-VDBA.

**Results:** Table 3 shows that VDBA and our Align-VDBA that pro-actively enforce constraints have a much higher CSR and BLEU-C compared to the other lazy constraint enforcement methods. For example, for ja→en greedy methods can only achieve a CSR of 76% compared to 96% of the VDBA-based methods. In terms of overall BLEU too, these methods provide an average increase in BLEU of 1.2 and an average increase in BLEU-C of 5 points. On average, Align-VDBA has a 0.7 point greater BLEU-C compared to VDBA. It also has a greater BLEU than VDBA on all the five datasets. In Table 9 of Appendix we show that for smaller beam-size of 5, the gap between Align-VDBA and VDBA is even larger (2.1 points greater BLEU-C and 0.4

Constraints	(gesetz zur, <b>law also</b> ), (dealer, <b>pusher</b> )
Gold	of course, if a drug addict becomes a <b>pusher</b> , then it is right and necessary that he should pay and answer before the <b>law also</b> .
VDBA	certainly, if a drug addict becomes a <b>dealer</b> , it is right and necessary that he should be brought to justice before the <b>law also pusher</b> .
Align-VDBA	certainly, if a drug addict becomes a <b>pusher</b> , then it is right and necessary that he should be brought to justice before the <b>law also</b> .
Constraints	(von mehrheitsverfahren, <b>of qualified</b> )
Gold	... whether this is done on the basis of a vote or of consensus, and whether unanimity is required or some form <b>of qualified</b> majority.
VDBA	... whether this is done by means <b>of qualified</b> votes or consensus, and whether unanimity or form of majority procedure apply.
Align-VDBA	... whether this is done by voting or consensus, and whether unanimity or form <b>of qualified</b> majority voting are valid.
Constraints	(zustimmung der, <b>strong backing of</b> )
Gold	... which were adopted with the <b>strong backing of</b> the ppe group and the support of the socialist members.
VDBA	... which were then adopted with broad agreement from the ppe group and with the <b>strong backing of</b> the socialist members.
Align-VDBA	... which were then adopted with <b>strong backing of</b> the ppe group and with the support of the socialist members.
Constraints	(den usa, <b>the usa</b> ), (sicherheitssystem an, <b>security system that</b> ), (entwicklung, <b>development</b> )
Gold	matters we regard as particularly important are improving the working conditions between the weu and the eu and the <b>development</b> of a european <b>security system that</b> is not dependent on <b>the usa</b> .
VDBA	we consider <b>the usa</b> 's european security system to be particularly important in improving working conditions between the weu and the eu and developing a european <b>security system that</b> is independent of the united states <b>development</b> .
Align-VDBA	we consider the <b>development</b> of the <b>security system that</b> is independent of <b>the usa</b> to be particularly important in improving working conditions between the weu and the eu .

Table 4: Anecdotes showing constrained translations produced by VDBA vs. Align-VDBA.

points greater BLEU). Table 4 lists some example translations by VDBA vs. Align-VDBA. We observe that VDBA places constraints at the end of the translated sentence (e.g., “pusher”, “development”) unlike Align-VDBA. In some cases where constraints contain frequent words (like of, the, etc.), VDBA picks the token in the wrong position to tack on the constraint (e.g., “strong backing of”, “of qualified”) while Align-VDBA places the constraint correctly.

Dataset →	IATE.414		Wiktionary.727	
Method (Beam Size) ↓	BLEU ( $\Delta$ )	CSR	BLEU ( $\Delta$ )	CSR
Baseline (5)	25.8	76.3	26.0	76.9
Train-by-app. (5)	26.0 (+0.2)	92.9	26.9 (+0.9)	90.7
Train-by-rep. (5)	26.0 (+0.2)	94.5	26.3 (+0.3)	93.4
No constraints (10)	29.7	77.0	29.9	72.4
SHIFTAET (10)	29.9	95.9	30.4	97.2
VDBA (10)	<b>30.9</b>	99.8	30.9	99.4
Align-VDBA (10)	<b>30.9 (+1.2)</b>	99.8	<b>31.1 (+1.2)</b>	99.5

Table 5: Constrained translation results on the two real world constraints from Dinu et al. (2019).

**Real World Constraints:** We also evaluate our method using real world constraints extracted from IATE and Wiktionary datasets by Dinu et al. (2019). Table 5 compares Align-VDBA with the soft-constraints method of Dinu et al. (2019) that requires special retraining to teach the model to copy constraints. We reproduced the numbers from their paper in the first three rows. Their baseline is almost 4 BLEU points worse than ours since they used a smaller transformer NMT model, thus making running times incomparable. When we compare the increment  $\Delta$  in BLEU over the respective baselines, Align-VDBA shows much greater gains of +1.2 vs. their +0.5. Also, Align-VDBA provides

a larger CSR of 99.6 compared to their 92. Results for other beam sizes and other methods and metrics appear in Appendix F.

## 5 Related Work

**Online Prior Alignment from NMTs:** Zenkel et al. (2019) find alignments using a single-head attention submodule, optimized to predict the next token. Garg et al. (2019) and Song et al. (2020) supervise a single alignment head from the penultimate multi-head attention with prior alignments from GIZA++ alignments or FastAlign. Bahar et al. (2020) and Shankar et al. (2018) treat alignment as a latent variable and impose a joint distribution over token and alignment while supervising on the token marginal of the joint distribution.

**Online Posterior Alignment from NMTs:** Shankar and Sarawagi (2019) first identify the role of posterior attention for more accurate alignment. However, their NMT was a single-headed RNN. Chen et al. (2020) implement posterior attention in a multi-headed Transformer but they incur a delay of one step between token output and alignment. We are not aware of any prior work that extracts truly online posterior alignment in modern NMTs.

**Offline Alignment Systems:** Several recent methods apply only in the offline setting: Zenkel et al. (2020) extend an NMT with an alignment module; Nagata et al. (2020) frame alignment as a question answering task; and Jalili Sabet et al. (2020); Dou and Neubig (2021) leverage similarity between contextual embeddings from pretrained multilingual models (Devlin et al., 2019).

**Lexicon Constrained Translation:** Hokamp and Liu (2017) and Post and Vilar (2018); Hu et al.

(2019) modify beam search to ensure that target phrases from a given constrained lexicon are present in the translation. These methods ignore alignment with the source but ensure high success rate for appearance of the target phrases in the constraint. Song et al. (2020) and Chen et al. (2021) do consider source alignment but they do not enforce constraints leading to lower CSR. Dinu et al. (2019) and Lee et al. (2021) propose alternative training strategies for constraints, whereas we focus on working with existing models. Recently, non autoregressive methods have been proposed for enforcing target constraints but they require that the constraints are given in the order they appear in the target translation (Susanto et al., 2020).

## 6 Conclusion

In this paper we proposed a simple architectural modification to modern NMT systems to obtain accurate online alignments. The key idea that led to high alignment accuracy was conditioning on the output token. Further, our designed alignment module enables such conditioning to be performed synchronously with token generation. This property led us to Align-VDBA, a principled decoding algorithm for lexically constrained translation based on joint distribution of target token and source alignments. Future work includes increase efficiency of constrained inference and harnessing such joint distributions for other forms of constraints, for example, nested constraints.

**Limitations:** All existing methods for hard constrained inference, including ours, come with considerable runtime overheads. Soft constrained methods are not accurate enough.

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## A Alignment Error Rate

Given gold alignments consisting of sure alignments  $\mathcal{S}$  and possible alignments  $\mathcal{P}$ , and the predicted alignments  $\mathcal{A}$ , the Alignment Error Rate (AER) is defined as (Och and Ney, 2000):

$$\text{AER} = 1 - \frac{|\mathcal{A} \cap \mathcal{P}| + |\mathcal{A} \cap \mathcal{S}|}{|\mathcal{A}| + |\mathcal{S}|}$$

Note that here  $\mathcal{S} \subseteq \mathcal{P}$ . Also note that since our models are trained on sub-word units but gold alignments are over words, we need to convert alignments between word pieces to alignments between words. A source word and a target word are said to be aligned if there exists an alignment link between any of their respective word pieces.

## B BLEU-C

Given a reference sentence, a predicted translation and a set of constraints, for each constraints, a segment of the sentence is chosen which contains the constraint and window size words (if available) surrounding the constraint words on either side. Such segments, called spans, are collected for the reference and predicted sentences in the test set and BLEU is computed over these spans. If a constraint is not satisfied in the prediction, the corresponding span is considered to be the empty string. An example is shown in Table 6. Table 7 shows how BLEU-C varies as a function of varying window size for a fixed English-French constraint set with beam size set to 10.

Window Size →	2	3	4	5	6	7	8
No constraints	0.0	0.0	0.0	0.0	0.0	0.0	0.0
NAIVEATT	34.4	32.0	30.4	29.5	29.4	29.5	29.7
PRIORATT	41.5	38.7	36.4	35.1	34.9	35.0	35.2
SHIFTATT	44.9	41.5	38.9	37.3	36.4	36.2	36.0
SHIFTAET	47.0	43.2	40.4	38.7	38.0	37.6	37.4
POSTALN	46.4	42.7	39.8	38.0	37.1	36.9	36.6
VDBA	54.9	50.5	46.8	44.6	43.5	43.0	42.6
Align-VDBA	56.4	51.7	47.9	45.6	44.4	43.7	43.3

Table 7: BLEU-C vs Window Size

## C Description of the Datasets

The European languages consist of parallel sentences for three language pairs from the Europarl Corpus and alignments from Mihalcea and Pedersen (2003), Och and Ney (2000), Vilar et al. (2006). Following previous works (Ding et al., 2019; Chen et al., 2020), the last 1000 sentences of the training data are used as validation data.

For English-Hindi, we use the dataset from Martin et al. (2005) consisting of 3440 training sentence

pairs, 25 validation and 90 test sentences with gold alignments. Since training Transformers requires much larger datasets, we augment the training set with 1.6 million sentences from the IIT Bombay Parallel Corpus (Kunchukuttan et al., 2018). We also add the first 50 sentences from the dev set of IIT Bombay Parallel Corpus with manually annotated alignments to the test set giving a total of 140 test sentences.

For Japanese-English, we use The Kyoto Free Translation Task (Neubig, 2011). It comprises roughly 330K training, 1166 validation and 1235 test sentences. As with other datasets, gold alignments are available only for the test sentences. The Japanese text is already segmented and we use it without additional changes.

The real world constraints datasets of Dinu et al. (2019) are extracted from the German-English WMT newstest 2017 task with the IATE dataset consisting of 414 sentences (451 constraints) and the Wiktionary 727 sentences (879 constraints). The constraints come from the IATE and Wiktionary terminology databases.

All datasets were processed using the scripts provided by Zenkel et al. (2019) at <https://github.com/lilt/alignment-scripts>. Computation of BLEU and BLEU-C, and the paired test were performed using sacrebleu (Post, 2018).

## D Bidirectional Symmetrized Alignment

We report AERs using bidirectional symmetrized alignments in Table 8 in order to provide fair comparisons to results in prior literature. The symmetrization is done using the *grow-diagonal* heuristic (Koehn et al., 2005; Och and Ney, 2000). Since bidirectional alignments need the entire text in both languages, these are not online alignments.

Method	de-en	en-fr	ro-en	en-hi	ja-en
Statistical Methods					
GIZA++	18.6	<b>5.5</b>	26.3	35.9	39.7
FastAlign	27.0	10.5	32.1	-	-
No Alignment Training					
NAIVEATT	29.2	16.9	31.4	43.8	57.1
SHIFTATT	16.9	7.8	24.3	30.9	46.2
With Alignment Training					
PRIORATT	22.0	10.1	26.3	32.1	48.2
SHIFTAET	15.4	5.6	<b>21.0</b>	26.7	40.1
POSTALN	<b>15.3</b>	<b>5.5</b>	<b>21.0</b>	<b>26.1</b>	<b>39.5</b>

Table 8: AERs for bidirectional symmetrized alignments. POSTALN consistently performs the best.

Reference	we consider the <b>development</b> of a robust <b>security system</b> that is independent of the	
Prediction	we consider developing a robust <b>security system</b> which is independent of the	
BLEU-C (Window Size = 2)		
Cons. No	Reference Spans	Predicted Spans
1	consider the <b>development</b> of a	(empty sentence)
2	a robust <b>security system</b> that is	a robust <b>security system</b> which is
BLEU-C = BLEU(Reference Spans, Predicted Spans)		

Table 6: An example BLEU-C computation

## E Additional Lexicon-Constrained Translation Results

Constrained translation results for beam sizes 5 and 10 are shown in Table 9. We also present results for Align-VDBA without the alignment probability based beam allocation as Align-VDBA\* in Table 9. We can see that our beam allocation technique results in better beam utilization as evidenced by improvements in BLEU and BLEU-C, and reduction total decoding time.

Paired bootstrap resampling test (Koehn, 2004) results with respect to Align-VDBA for beam size 10 are shown in Table 10.

## F Additional Real World Constrained Translation Results

Results on the real world constrained translation datasets of Dinu et al. (2019) for all the methods in Table 3 with beam sizes 5, 10 and 20 are presented in Table 11. Paired bootstrap resampling test (Koehn, 2004) results with respect to Align-VDBA for beam size 5 are shown in Table 12

## G Alignment-based Token Replacement Algorithm

The pseudocode for the algorithm used in Song et al. (2020); Chen et al. (2021) and our non-VDBA based methods in Section 4.3 is presented in Algorithm 2. As described in Section 3.1, at each decoding step, if the source token having the maximum alignment at the current step lies in some constraint span, the constraint in question is decoded until completion before resuming normal decoding.

Though different alignment methods are represented using a call to the same ATTENTION function in Algorithm 2, these methods incur varying computational overheads. For instance, NAIVEATT incurs little additional cost, PRIORATT and POSTALN involve a multi-head attention computation. For SHIFTATT and SHIFTAET,

an entire decoder pass is done when ATTENTION is called, thereby incurring a huge overhead as shown in Table 3.

## H Layer Selection for Alignment Supervision of Distant Language Pairs

For the alignment supervision, we used alignments extracted from vanilla Transformers using the SHIFTATT method. To do so, however, we need to choose the decoder layers from which to extract the alignments. The validation AERs can be used for this purpose but since gold validation alignments are not available, Chen et al. (2020) suggest selecting the layers which have the best consistency between the alignment predictions from the two translation directions.

For the European language pairs, this turns out to be layer 3 as suggested by Chen et al. (2020). However, for the distant language pairs Hindi-English and Japanese-English, this is not the case and layer selection needs to be done. The AER between the two translation directions on the validation set, with alignments obtained from different decoder layers, are shown in Tables 13 and 14.

Beam Size	Method	de→en				en→fr				ro→en				en→hi				ja→en			
		BLEU-C	CSR	BLEU	Time	BLEU-C	CSR	BLEU	Time	BLEU-C	CSR	BLEU	Time	BLEU-C	CSR	BLEU	Time	BLEU-C	CSR	BLEU	Time
5	No constraints	0.0	5.0	32.9	78	0.0	8.7	34.6	61	0.0	8.4	33.3	45	0.0	5.6	19.7	18	0.0	7.9	19.1	221
	NAIVEATT	28.9	86.2	36.7	127	36.7	88.6	38.0	87	32.9	91.8	36.3	88	23.0	89.9	23.9	25	15.1	77.0	20.3	398
	PRIORATT	35.3	93.0	37.7	136	42.2	94.7	38.6	89	36.0	91.6	37.0	89	27.6	91.7	24.7	26	16.8	80.2	20.6	353
	SHIFTATT	41.0	96.7	38.7	268	45.2	93.8	38.4	167	39.2	94.4	37.2	160	23.8	81.8	22.0	42	15.1	72.6	19.3	664
	SHIFTAET	43.1	97.6	39.1	291	46.5	94.8	38.6	165	40.8	94.7	37.5	163	24.5	83.6	22.1	44	18.0	76.5	19.6	583
	POSTALN	42.7	97.3	39.0	252	46.1	93.9	38.5	151	39.8	93.5	37.3	141	23.3	79.7	21.7	39	17.9	75.3	19.6	469
	VDBA	39.6	99.4	37.8	203	45.9	99.5	38.5	109	36.6	99.2	36.7	117	27.3	96.6	24.2	37	22.1	96.9	20.9	397
	Align-VDBA*	40.3	99.0	38.0	244	47.4	99.3	38.7	132	37.6	99.7	36.8	139	27.2	95.6	24.1	46	22.5	97.2	21.0	460
	Align-VDBA	41.3	98.8	38.2	236	48.0	98.9	38.7	128	42.0	96.6	37.5	134	28.2	91.3	24.7	45	22.6	93.9	21.2	445
	10	No constraints	0.0	4.6	32.9	87	0.0	8.7	34.8	64	0.0	8.8	33.4	47	0.0	6.3	19.7	21	0.0	8.8	18.9
NAIVEATT		28.7	86.1	36.6	147	36.5	88.0	38.3	93	33.3	92.3	36.5	99	22.5	88.4	23.6	27	15.1	75.9	20.2	315
PRIORATT		35.0	92.8	37.6	159	42.1	94.4	38.9	97	36.0	91.2	37.2	100	27.2	91.5	24.4	28	16.7	79.7	20.4	326
SHIFTATT		41.0	96.6	38.7	443	45.0	93.5	38.7	239	39.2	94.2	37.4	241	23.2	78.7	21.9	58	15.2	72.7	19.3	567
SHIFTAET		43.1	97.5	39.1	458	46.6	94.3	39.0	235	40.8	94.4	37.6	263	24.3	80.2	22.0	62	18.1	75.9	19.7	596
POSTALN		42.7	97.2	39.0	399	46.3	94.1	38.7	218	40.0	93.5	37.4	226	23.8	79.0	22.0	47	18.2	75.7	19.7	460
VDBA		44.5	98.9	38.5	293	51.9	98.5	39.5	160	43.1	99.1	37.9	165	29.8	92.3	24.5	49	24.3	95.6	21.6	494
Align-VDBA		44.5	98.6	38.6	357	52.9	98.4	39.7	189	44.1	98.9	38.1	203	30.5	91.5	24.7	70	25.1	95.5	21.8	630

Table 9: Lexically Constrained Translation Results with different beam sizes. All numbers are average over 5 randomly sampled constraint sets and running times are in seconds. Align-VDBA\* denotes Align-VDBA without alignment probability based beam allocation (*i.e.* with threshold set to 0).

	1	2	3	4	5	6		1	2	3	4	5	6
1	65.5	55.8	56.1	95.2	94.6	96.6	1	93.5	90.0	94.4	92.2	95.1	95.1
2	59.2	47.5	<b>44.5</b>	95.1	91.9	95.8	2	86.5	<b>58.7</b>	86.9	69.4	87.2	86.2
3	62.6	52.1	48.3	93.7	91.4	95.2	3	87.4	59.4	87.1	69.1	87.1	86.2
4	88.6	83.3	82.1	89.9	88.0	90.3	4	89.1	69.1	85.9	74.2	84.9	85.4
5	91.6	87.7	88.5	91.4	88.8	90.2	5	93.4	88.5	89.1	87.1	86.8	88.1
6	93.5	91.1	92.5	92.5	90.5	90.7	6	93.5	89.4	90.0	88.1	87.7	88.7

Table 13: AER between en→hi and hi→en SHIF-TATT alignments on the validation set for EnHi

Table 14: AER between ja→en and en→ja SHIF-TATT alignments on the validation set for JaEn

	de→en	en→fr	ro→en
No constraints	0.0001*	0.0001*	0.0001*
NAIVEATT	0.0001*	0.0001*	0.0001*
PRIORATT	0.0001*	0.0001*	0.0001*
SHIFTATT	0.1700	0.0001*	0.0001*
SHIFTAET	0.0015*	0.0001*	0.0018*
POSTALN	0.0032*	0.0001*	0.0003*
VDBA	0.2666	0.0020*	0.0229*

Table 10:  $p$ -values from paired bootstrap resampling tests with 10000 bootstrap samples for BLEU on Table 3 datasets for beam size 10. Tests are performed with respect to Align-VDBA. \* denotes statistically significant difference from Align-VDBA at power 0.05 ( $p$ -value < 0.05).

Beam Size	Dataset →	IATE.414				Wiktionary.727					
		Method ↓	BLEU-C	CSR	BLEU	Time	BLEU-C	CSR	BLEU	Time	
5	No constraints		27.9	76.6	29.7	134	26.3	72.0	29.9	217	
	NAIVEATT		29.2	96.9	29.2	175	29.0	95.3	29.1	341	
	PRIORATT		31.2	97.1	29.7	198	32.2	95.9	29.9	306	
	SHIFTATT		34.9	96.7	29.9	355	35.3	96.5	30.0	568	
	SHIFTAET		35.2	96.3	30.0	378	35.8	97.1	30.2	637	
	POSTALN		35.3	96.7	30.0	272	35.8	96.7	30.2	467	
	VDBA		35.3	98.8	29.8	258	35.0	99.2	30.4	442	
	Align-VDBA*		35.4	99.8	29.8	280	35.1	99.3	30.3	534	
	Align-VDBA		36.1	98.3	30.1	268	35.9	98.8	30.6	523	
	10	No constraints		28.3	77.0	29.7	113	26.3	72.4	29.9	164
NAIVEATT			28.9	97.3	29.1	145	29.2	95.3	29.1	269	
PRIORATT			31.3	96.9	29.5	155	32.3	96.0	29.9	260	
SHIFTATT			34.9	96.3	29.8	345	35.3	96.8	30.3	600	
SHIFTAET			35.2	95.9	29.9	350	35.9	97.2	30.4	664	
POSTALN			35.1	95.9	29.9	287	35.8	97.0	30.3	458	
VDBA			37.6	99.8	30.9	257	36.9	99.4	30.9	451	
Align-VDBA			37.5	99.8	30.9	353	37.2	99.5	31.1	540	
20		No constraints		28.4	77.2	29.9	103	26.3	72.1	30.0	177
		NAIVEATT		28.9	96.9	29.0	188	29.1	95.4	29.3	325
	PRIORATT		31.3	96.9	29.6	203	32.6	96.4	30.1	338	
	SHIFTATT		34.7	96.1	29.8	528	35.3	96.8	30.2	892	
	SHIFTAET		35.0	95.8	29.9	539	36.1	97.3	30.4	923	
	POSTALN		35.1	96.1	29.9	420	36.0	97.0	30.4	751	
	VDBA		37.8	99.8	30.9	381	37.4	99.2	31.2	680	
	Align-VDBA		37.9	99.8	30.9	465	38.0	99.5	31.3	818	

Table 11: Additional results for the real world constraints for all methods and different beam sizes. Align-VDBA\* denotes Align-VDBA without alignment probability based beam allocation.

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**Algorithm 2**  $k$ -best extraction with argmax replacement decoding.

---

**Inputs:** A  $k \times |V_T|$  matrix of scores (for all tokens up to the currently decoded ones).  $k$  beam states.

```
1: function SEARCH_STEP(beam, scores)
2:   next_toks, next_scores  $\leftarrow$  ARGMAX_K(scores, k=2, dim=1)  $\triangleright$  Best 2 tokens for each beam
3:   candidates  $\leftarrow$  []
4:   for  $0 \leq h < 2 \cdot k$  do
5:     candidate  $\leftarrow$  beam[h//2]
6:     candidate.tokens.append(next_toks[h//2, h%2])
7:     candidate.scores  $\leftarrow$  next_scores[h//2, h%2]
8:     candidates.append(candidate)
9:   attention  $\leftarrow$  ATTENTION(candidates)
10:  aligned_x  $\leftarrow$  ARGMAX(attention, dim=1)
11:  for  $0 \leq h < 2 \cdot k$  do
12:    if aligned_x[h]  $\in C_i^x$  for some  $i$  and not candidates[h].inprogress then  $\triangleright$  Start constraint
13:      candidates[h].inprogress  $\leftarrow$  True
14:      candidates[h].constraintNum  $\leftarrow i$ 
15:      candidates[h].tokenNum  $\leftarrow 0$ 
16:    if candidates[h].inprogress then  $\triangleright$  Replace token with constraint tokens
17:      consNum  $\leftarrow$  candidates[h].constraintNum
18:      candidates[h].tokens[-1]  $\leftarrow$  constraints[consNum][candidates[h].tokenNum]
19:      candidates[h].tokenNum  $\leftarrow$  candidates[h].tokenNum + 1
20:    if constraints[consNum].length == candidates[h].tokenNum then
21:      candidates[h].inprogress  $\leftarrow$  False  $\triangleright$  Finish current constraint
22:  candidates  $\leftarrow$  REMOVE_DUPLICATES(candidates)
23:  newBeam  $\leftarrow$  TOP_K(candidates)
24:  return newBeam
```

---

Dataset	IATE.414			Wiktionary.727		
	BLEU	$\mu \pm 95\% \text{ CI}$	p-value	BLEU	$\mu \pm 95\% \text{ CI}$	p-value
Align-VDBA	30.1	(30.0 $\pm$ 1.7)		30.6	(30.6 $\pm$ 1.2)	
No constraints	29.7	(29.7 $\pm$ 1.7)	0.1059	29.9	(29.9 $\pm$ 1.2)	0.0054*
NAIVEATT	29.2	(29.2 $\pm$ 1.7)	0.0121*	29.1	(29.1 $\pm$ 1.2)	0.0001*
PRIORATT	29.7	(29.6 $\pm$ 1.6)	0.0829	29.9	(29.8 $\pm$ 1.2)	0.0041*
SHIFTATT	29.9	(29.8 $\pm$ 1.6)	0.1827	30.0	(30.0 $\pm$ 1.2)	0.0229*
SHIFTAET	30.0	(29.9 $\pm$ 1.6)	0.2824	30.2	(30.2 $\pm$ 1.2)	0.0588
POSTALN	30.0	(30.0 $\pm$ 1.6)	0.3813	30.2	(30.2 $\pm$ 1.2)	0.0646
VDBA	29.8	(29.7 $\pm$ 1.6)	0.0849	30.4	(30.4 $\pm$ 1.2)	0.0960

Table 12: Paired bootstrap resampling tests with 10000 bootstrap samples for BLEU on [Dinu et al. \(2019\)](#) datasets for beam size 5. \* denotes statistically significant difference from Align-VDBA at power 0.05 (p-value < 0.05).