From Sparse to Dense: GPT-4 Summarization with Chain of Density Prompting

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Abstract

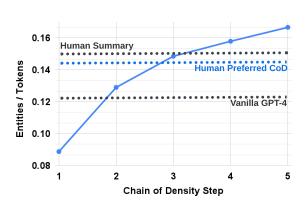
Selecting the "right" amount of information to include in a summary is a difficult task. A good summary should be detailed and entity-centric without being overly dense and hard to follow. To better understand this tradeoff, we solicit increasingly dense GPT-4 summaries with what we refer to as a "Chain of Density" (CoD) prompt. Specifically, GPT-4 generates an initial entitysparse summary before iteratively incorporating missing salient entities without increasing the length. Summaries generated by CoD are more abstractive, exhibit more fusion, and have less of a lead bias than GPT-4 summaries generated by a vanilla prompt. We conduct a human preference study on 100 CNN DailyMail articles and find that humans prefer GPT-4 summaries that are more dense than those generated by a vanilla prompt and almost as dense as human written summaries. Qualitative analysis supports the notion that there exists a tradeoff between informativeness and readability. 500 annotated CoD summaries, as well as an extra 5,000 unannotated summaries, are freely available on HuggingFace¹.

1 Introduction

Automatic summarization has come a long way in the past few years, largely due to a paradigm shift away from supervised fine-tuning on labeled datasets to zero-shot prompting with Large Language Models (LLMs), such as GPT-4 (OpenAI, 2023). Without additional training, careful prompting can enable fine-grained control over summary characteristics, such as length (Goyal et al., 2022), topics (Bhaskar et al., 2023), and style (Pu and Demberg, 2023).

An overlooked aspect is the information density of an summary. In theory, as a compression of another text, a summary *should* be denser–containing a higher concentration of information–than the source document. Given the high latency of LLM decoding (Kaddour et al., 2023), covering more information in fewer

¹https://huggingface.co/datasets/ griffin/chain_of_density



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Figure 1: Chain of Density (**CoD**) summaries grow increasingly entity dense, starting off closer to vanilla GPT-4 summaries and eventually surpassing that of human written summaries. Human annotations suggest that a density similar to that of human-written summaries is preferable–striking the right balance between clarity (favors *less* dense) and informativeness (favors *more* dense).

words is a worthy goal, especially for real-time applications. Yet, how dense is an open question. A summary is uninformative if it contains insufficient detail. If it contains too much information, however, it can become difficult to follow without having to increase the overall length. Conveying more information subject to a fixed token budget requires a combination of abstraction, compression, and fusion. There is a limit to how much space can be made for additional information before becoming illegible or even factually incorrect.

In this paper, we seek to identify this limit by soliciting human preferences on a set of increasingly dense summaries produced by GPT-4. Treating entities, and, in particular, the average number of entities per token, as a proxy for density, we generate an initial, entitysparse summary. Then, we iteratively identify and fuse 1-3 missing entities from the previous summary without increasing the overall length (5x overall). Each summary has a higher ratio of entities to tokens than the previous one. Based on human preference data, we determine that humans prefer summaries that are almost as dense as human-written summaries and more

Chain of Density (CoD) Prompt



Figure 2: Chain of Density (**CoD**) Prompt and example output. At each step, 1-3 additional details (entities) are added to the previous summary without increasing the length. To make room for new entities, existing content is re-written (e.g., compression, fusion). Half the annotators (2/4) prefer the second to last summary, with the others preferring the final one.

dense than those generated by a vanilla GPT-4 prompt. Our primary contributions are to:

- Develop a prompt-based iterative method (**CoD**) for making summaries increasingly entity dense.
- Conduct both human and automatic evaluation of increasingly dense summaries on CNN/Dailymail articles to better understand the tradeoff between informativeness (favoring more entities) and clarity (favoring fewer entities).
- Open source GPT-4 summaries, annotations, and a set of 5,000 unannotated **CoD** summaries to be used for evaluation or distillation.

2 Chain of Density Prompting

Prompt. Our goal is to generate a set of summaries with GPT-4 with varying levels of information density, while controlling for length, which has proven to be a strong confounder when evaluating summaries (Fabbri et al., 2021; Liu et al., 2023b). To do this, we formulate a single Chain of Density (**CoD**) prompt, whereby an initial summary is generated and made increasingly entity dense. Specifically, for a fixed number of turns, a set of unique salient entities from the source text are identified and fused into the previous summary without increasing the length. The first summary is entity-sparse as it focuses on only 1-3 initial entities.

To maintain the same length while increasing the number of entities covered, abstraction, fusion, and compression is explicitly encouraged, rather than dropping meaningful content from previous summaries.

CoD Outputs (Added Details from previous)

Figure 2 displays the prompt along with an example output. Rather than be prescriptive about the types of entities, we simply define a Missing Entity as:

- Relevant: to the main story.
- **Specific**: descriptive yet concise (5 words or fewer).
- Novel: not in the previous summary.
- Faithful: present in the Article.
- Anywhere: located anywhere in the Article.

Data. We randomly sample 100 articles from the CNN/DailyMail summarization (Nallapati et al., 2016) test set for which to generate **CoD** summaries.

Reference Points. For frame of reference, we compare **CoD** summary statistics to human-written bullet-point style reference summaries as well as summaries generated by GPT-4 with a vanilla prompt: "Write a VERY short summary of the Article. Do not exceed 70 words." We set the desired token length to match that of **CoD** summaries (shown in Table 1).

3 Statistics

Direct statistics (tokens, entities, entity density) are ones directly controlled for by **CoD**, while Indirect

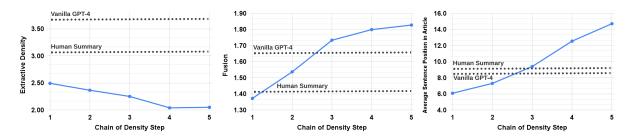


Figure 3: CoD-generated summaries grow increasingly abstractive while exhibiting more fusion and less of a lead bias.

statistics are expected byproducts of densification.

CoD Step	Tokens	Entities	Density (E/T)
1	72	6.4	0.089
2	67	8.7	0.129
3	67	9.9	0.148
4	69	10.8	0.158
5	72	12.1	0.167
Human	60	8.8	0.151
Vanilla GPT-4	70	8.5	0.122

Table 1: Explicit statistics for GPT-4 CoD summaries.

Direct Statistics. In Table 1, we compute tokens with NLTK (Loper and Bird, 2002), measure unique entities with Spacy², and compute entity density as the ratio. The **CoD** prompt largely adheres to a fixed token budget. In fact, the second step leads to an average 5-token (72 to 67) reduction in length as unnecessary words are removed from the initially verbose summary. The entity density rises–starting at 0.089, initially below Human and Vanilla GPT-4 (0.151 and 0.122)–to 0.167 after 5 steps of densification.

Indirect Statistics. *Abstractiveness* should increase with each CoD step because summaries are iteratively re-written to make space for each additional entity. We measure abstractiveness with extractive density: the average squared length of extractive fragments (Grusky et al., 2018). Similarly, the level of concept Fusion should increase monotonically as entities are added to a fixed-length summary. We proxy fusion as average number of source sentences aligned to each summary sentence. For alignment, we use the relative ROUGE gain method (Zhou et al., 2018), which aligns source sentences to a target sentence until the relative ROUGE gain of an additional sentence is no longer positive. We also expect the Content Distribution-the position in the Article from which summary content is sourced-to shift. Specifically, we expect that CoD summaries initially exhibit a strong Lead Bias yet gradually start to pull in entities from the

middle and end of the article. To measure this, we use our alignments from fusion and measure the average sentence rank of all aligned source sentences. Figure 3 confirms these hypotheses: abstractiveness increases with the number of re-writing steps (lower extractive density on the left), the rate of fusion rises (middle figure), and the summaries start to incorporate content from the middle and end of the article (right figure). Interestingly, all **CoD** summaries are more abstractive than both human written and baseline summaries.

4 Results

To better understand the tradeoffs present with **CoD** summaries, we conduct a preference-based human study and a rating-based evaluation with GPT-4.

CoD	% Share of First Place Votes				
Step	Individual Annotators Aggregate				
1	3.0	2.0	13.0	17.4	8.3
2	25.0	28.0	43.0	31.4	30.8
3	22.0	28.0	21.0	24.4	23.0
4	29.0	25.0	13.0	26.7	22.5
5	21.0	17.0	10.0	16.3	15.5

Table 2: Breakdown of first-place votes for CoD summaries by step. Based on aggregate preferences, the modal CoD step is 2, median is 3, and expected is 3.06.

Human Preferences. We conduct a human evaluation to assess the impact of densification on human assessments of overall quality. Specifically, the first four authors of the paper were presented with randomly shuffled **CoD** summaries, along with the articles, for the same 100 articles (5 steps * 100 = 500 total summaries). Based on the definition of a "good summary" from Stiennon et al. (2020) (Table 6 from their paper), each annotator indicated their top preferred summary. Table 2 reports the breakdown of first place votes by **CoD** step across annotators–as well as aggregated across annotators. First, we report a low Fleiss' kappa (Fleiss, 1971) of 0.112, which points to the subtle differences between summaries and the subjective nature of the task. Recent work has

²https://spacy.io.

CoD Step	Entity Density	Informative	Quality	Coherence	Attributable	Overall	GPT-4 Eval Average
1	0.089	4.34	4.75	4.96	4.96	4.41	4.69
2	0.129	4.62	4.79	4.92	5.00	4.58	4.78
3	0.148	4.67	4.76	4.84	5.00	4.57	4.77
4	0.158	4.74	4.69	4.75	5.00	4.61	4.76
5	0.167	4.73	4.65	4.61	4.97	4.58	4.71

Table 3: GPT-4 Likert-scale (1-5) assessments of Chain of Density (CoD) Summaries by step.

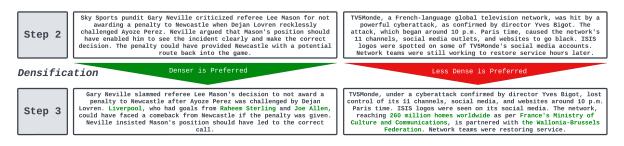


Figure 4: An example of a human-preferred densification step (left) and one which is not preferred. For the left, the bottom summary is preferred because the addition of "Liverpool" and the goal-scorers is relevant. The second summary makes room with sensible compressions, such as synthesizing "a potential route back into the game" into "a comeback". For the right, the addition of more details on "TVMonde" does not make up for the presence of an awkward fusion of entities ("cyberattack", and "Yves Bigot"), which was a direct result of having to tighten the previous summary.

similarly noted low instance-level agreement when judging GPT-based summaries (Goyal et al., 2022).

Yet, at the system level, some trends start to emerge. For 3 of the 4 annotators, **CoD** step 1 received the largest share of first-place votes across the 100 examples (28, 43, and 31.4%, respectively). Yet, in aggregate, 61% of first placed summaries (23.0+22.5+15.5) involved ≥ 3 densification steps. The median preferred **CoD** step is in the middle (3), and the expected step is 3.06.

Based on the average density of Step 3 summaries, we can roughly infer a preferred entity density of ~ 0.15 across the **CoD** candidates. From Table 1, we can see that this density aligns with human-written summaries (0.151), yet is noticeable higher than summaries produced with a vanilla GPT-4 prompt (0.122).

Automatic Metrics. As an evaluator, GPT-4 has been shown to adequately correlate to human judgments (Fu et al., 2023; Liu et al., 2023a), even potentially outperforming crowd-sourced workers on some annotation tasks (Gilardi et al., 2023). As a complement to our human evaluation (below), we prompt GPT-4 to rate CoD summaries (1-5) along 5 dimensions: Informative, Quality, Coherence, Attributable, and Overall. The definitions of Informative, Quality, and Attributable come from Aharoni et al. (2023), while Coherence comes from Fabbri et al. (2021)³. Overall aims to capture the qualities jointly. Please see Appendix A for the prompts used

to solicit scores for each dimension. Table 3 suggests that densification is correlated with informativeness, yet there is a limit, with the score peaking at Step 4 (4.74). Article-free dimensions: **Quality** and **Coherence**, decline sooner (after 2 and 1 steps, respectively). All summaries are deemed **Attributable** to the source article. The **Overall** scores skew toward denser and more informative summaries, with **Step 4** having the highest score. On average across dimensions, the first and last **CoD** steps are *least* favored, while the middle three are close (4.78, 4.77, and 4.76, respectively).

In Appendix A, we report highest summarylevel correlations of the **Overall** metric to human judgments (0.31 Pearson correlation), yet note low correlations overall–a phenomenon observed by Deutsch et al. (2022) when summaries are of similar quality.

Qualitative Analysis. There exists a clear trade-off between coherence / readability of summaries and informativeness. To illustrate, in Figure 4, we present two CoD steps: one for which the summary is improved with more detail, and one for which the summary is harmed. On average, intermediate CoD summaries best achieved this balance, yet we leave it to future work to precisely define and quantify this tradeoff.

5 Related Work

GPT Summarization. Goyal et al. (2022) benchmarked GPT-3 on news article summarization and found that humans preferred GPT-3 summaries over previous supervised baselines, which was

³Quality and Coherence are article-independent metrics.

not reflective of existing reference-based and reference-free metrics. Zhang et al. (2023) find that zeroshot GPT-3 summaries perform on par with humans by soliciting high-quality summaries from freelance writers. **Entity-Based Summarization.** Narayan et al. (2021) proposed generating entity chains as a planning step for supervised fine-tuning of summarization models, in contrast to keywords (Li et al., 2020; Dou et al., 2021) or purely extractive units (Dou et al., 2021; Adams et al., 2023a). Entities have also been incorporated for summarization as a form of control (Liu and Chen, 2021; He et al., 2022; Maddela et al., 2022), to improve faithfulness (Nan et al., 2021; Adams et al., 2022), and as a unit for evaluation (Cao et al., 2022; Adams et al., 2023b).

6 Conclusion

We study the impact of summary densification on human preferences of overall quality. We find that a degree of densification is preferred, yet, when summaries contain too many entities per token, it is very difficult maintain readability and coherence. We open-source annotated test set as well as a larger un-annotated training set for further research into the topic of fixed-length, variable density summarization.

7 Limitations

We only analyze **CoD** for a single domain, news summarization. Annotations did not show high summary-level agreement yet did start to show system-level trends, which is in line with previous work on LLM-based evaluation (Goyal et al., 2022). Finally, GPT-4 is a closed source model so we cannot share model weights. We do, however, publish all evaluation data, annotations, as well as 5,000 un-annotated **CoD** to be used for downstream uses cases, e.g., density distillation into an open-sourced model such as LLAMA-2 (Touvron et al., 2023).

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A GPT-4 Metrics

For the GPT-4 Likert-style evaluation, we use the following prompt template.

```
Article: {{Article}}
Summary: {{Summary}}
```

```
Please rate the summary
(1=worst to 5=best) with
respect to {{Dimension}}.
```

{{Definition}}

Below, we present the definitions provided for each quality metric.

- **Informative**: An informative summary captures the important information in the article and presents it accurately and concisely.
- **Quality**: A high quality summary is comprehensible and understandable.
- **Coherence**: A coherent summary is well-structured and well-organized.
- Attributable: Is all the information in the summary fully attributable to the Article?
- **Overall Preference**: A good summary should convey the main ideas in the Article in a concise, logical, and coherent fashion.

The **Quality** and **Coherence** prompts do not include the Article in the prompt. These definitions were paraphrased from previous summarization annotation efforts: (Fabbri et al., 2021; Aharoni et al., 2023).

Dimension	Correlation
Informative	0.215
Quality	0.120
Coherence	0.178
Attributable	0.245
Overall	0.311

Table 4: Summary-Level Pearson Correlation coefficientbetween human preferences and GPT-4 Likert ratings.

Meta-Evaluation. To compute the summary-level correlation, we first turned the preference data into a vector representing the number of times that summary received a first-placed vote. Table 4 demonstrates, unsurprisingly, that a prompt designed to capture overall summary rating has the highest summary-level Pearson correlation to overall preferences (31), yet overall correlations are still low.