## Language Models as Compilers: Simulating Pseudocode Execution Improves Algorithmic Reasoning in Language Models

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#### Abstract

Algorithmic reasoning tasks that involve complex logical patterns, such as completing Dyck language, pose challenges for large language models (LLMs), despite their recent success. Prior work has used LLMs to generate programming language and applied external compilers for such tasks. Yet, when on the fly, it is hard to generate an executable code with the correct logic for the solution. Even so, code for one instance cannot be reused for others, although they might require the same logic to solve. We present THINK-AND-EXECUTE, a novel framework that improves LLMs' algorithmic reasoning: (1) In THINK, we discover task-level logic shared across all instances, and express such logic with pseudocode; (2) In Ex-ECUTE, we tailor the task-level pseudocode to each instance and simulate the execution of it. THINK-AND-EXECUTE outperforms several strong baselines (including CoT and PoT) in diverse algorithmic reasoning tasks. We manifest the advantage of using task-level pseudocode over generating instance-specific solutions one by one. Also, we show that pseudocode can better improve LMs' reasoning than natural language guidance, even though they are trained with natural language instructions.

#### 1 Introduction

Reasoning in large language models (LLMs) typically entails analyzing the logical structure underlying a problem and realizing the logic into a sequence of reasoning steps to derive the final answer (Zhou et al., 2022a,b; Hao et al., 2023). In particular, algorithmic reasoning has long been a formidable challenge for LLMs, as it requires to scrutinize a complicated reasoning pattern and to translate it into a long sequence of reasoning steps (Suzgun et al., 2022; Valmeekam et al., 2022; Pan et al., 2023; Zelikman et al., 2023).

To improve the reasoning capabilities of LLMs, prior works have primarily pursued two directions. The first direction includes enhancing the reasoning execution step by generating a rationale in natural language (*e.g.*, Chain-of-Thought (Wei et al., 2022; Kojima et al., 2022)) or a piece of code (*e.g.*, Program-of-Thought (Chen et al., 2023), Program-Aided LMs (Gao et al., 2023)). However, such approaches perform step-by-step reasoning on-the-fly, without a dedicated phase for planning. This necessitates that the LLM analyze the logic and execute it within a single inference call, which constrains its expressiveness. Moreover, when encountering a similar problem, the LLM should solve it without being able to reuse the logic previously understood.

The second direction involves explicitly generating a plan described in natural language (NL) with LLMs. The plan describes the logic of the task and the LLM would subsequently concretize it into a sequence of reasoning steps (*e.g.*, Least-to-Most (Zhou et al., 2022b), Plan-and-Solve (Wang et al., 2023)). Yet, as prior works have mentioned, in our preliminary experiments, we find that NL might not be the optimal medium to describe the logic of the problem (Li et al., 2023). In addition, prior works mostly rely on generating a plan by observing a single instance, which hinders analyzing the core reasoning pattern shared across similar instances in a single task (Zhou et al., 2024).

To address these issues, we introduce THINK-AND-EXECUTE, an algorithmic framework that discovers a logic that reflects the shared reasoning pattern behind a given task, and conducts reasoning by tailoring the logic into each instance. THINK-AND-EXECUTE consists of three distinctive steps; We first ask an LLM to THINK about common reasoning patterns of a task by providing it with a few example questions. Then, the LLM translates the NL description of the logic in a pseudocode format. The pseudocode format allows more flexibility in applying the logic to each instance compared to programming language such as Python. Finally, in EXECUTE step, the LLM simulates the execution

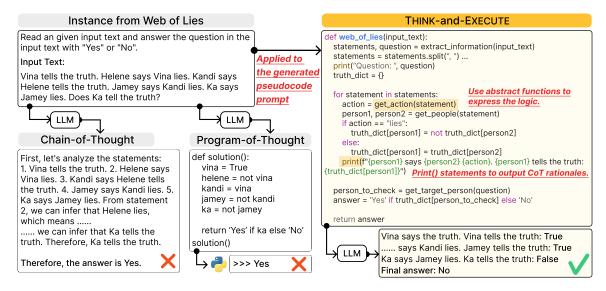


Figure 1: An illustration of THINK-AND-EXECUTE, compared with Zero-shot Chain-of-Thought (Kojima et al., 2022) and Program-of-Thoughts (Chen et al., 2023).

of the task-level pseudocode to follow the logic in it and predicts the output result of the pseudocode.

Through extensive experiments on 7 algorithmic reasoning tasks from Big-Bench Hard (Suzgun et al., 2022), we show the effectiveness of THINK-AND-EXECUTE over the challenging baselines. The superior performance of THINK-AND-EXECUTE over PoT suggests that discovering the common logic for a given task and applying it to each instance would be more helpful than writing instance-specific code for every instance. Noteworthily, simulating the execution of pseudocode is shown to improve LMs' reasoning more than planning with NL, even though they are trained to follow NL instructions. Furthermore, we empirically show that the pseudocode prompt discovered by an LLM can be applied to small LMs (SLMs), such as CodeLlama-7B, to boost their reasoning ability. This indicates the efficiency of THINK-AND-EXECUTE over other code prompting methods that require the LLM to generate instance-specific code every time (e.g., PoT).

To summarize, our contributions are as follows:

- We introduce THINK-AND-EXECUTE, a framework that performs reasoning with a pseudocode that contains the common logical structure of a given task.
- We show that THINK-AND-EXECUTE achieves notable improvements over strong baselines, including Chain-of-Thought and Program-of-Thought prompting, across various algorithmic tasks in Big-Bench Hard.

• We demonstrate that the pseudocode written by an LLM can be transferred to SLMs, showing the efficiency of our approach.

#### **2 THINK-AND-EXECUTE**

In this section, we introduce THINK-AND-EXECUTE and provide a detailed explanation of how LLMs perform reasoning with it. We incorporate an Instructor LM  $\mathcal{I}$  and a Reasoner LM  $\mathcal{R}$ , for THINK and EXECUTE, respectively. Figure 2 shows the overview of our framework.

#### 2.1 THINK: Describing the Underlying Logic of a Task in a Pseudocode Format

The goal for the Instructor LM  $\mathcal{I}$  in this phase is to discover the underlying logic for solving a given task *t*, and generate a prompt describing the logic, which will be further applied to all instances of the task (in EXECUTE). This prompt is constructed with **pseudocode** rather than natural language, which is used in prior work to guide the LM to perform step-by-step reasoning (Kojima et al., 2022; Wang et al., 2023).

**Step 1:** Constructing a meta prompt. To prompt the Instructor LM  $\mathcal{I}$  to generate a task-level pseudocode for the given target task t, we provide  $\mathcal{P}$  of other tasks as demonstrations in a meta prompt.<sup>1</sup> In practice, we construct the meta prompt with 3 randomly sampled tasks (3 example questions, analysis, and  $\mathcal{P}$  for each task) from  $\mathcal{T}$ 

<sup>&</sup>lt;sup>1</sup>We manually annotate  $\mathcal{P}$  for each task in  $\mathcal{T}$  in advance. See Appendix B.1 for examples.

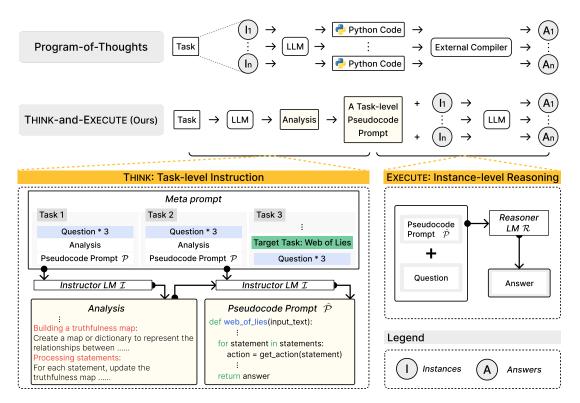


Figure 2: An overview of THINK-AND-EXECUTE. In THINK (Top), an LLM analyzes the given task provided in the meta prompt and generates a pseudocode prompt that describes the necessary logic for solving the task. Then, in EXECUTE (Bottom), the LLM conducts reasoning for each instance by simulating the execution of the pseudocode prompt.

as demonstrations and the target task t (3 example questions without the answers).<sup>2</sup>

Step 2: Analyzing the target task. Given the meta prompt,  $\mathcal{I}$  generates an analysis containing key reasoning logic that is required to solve the target task regardless of the instances (questions). For example, in Figure 2 (Top), the generated analysis points out that *building a truthfulness map* and updating it by *processing statements* are needed to solve the task, *i.e.*, Web of Lies. This step guides  $\mathcal{I}$  to focus on the reasoning process shared among all the instances, which would be crucial in making a task-level prompt.

Step 3: Generating a pseudocode prompt based on the analysis. Next, based on the analysis,  $\mathcal{I}$  writes a prompt  $\mathcal{P}$  in the form of pseudocode, which breaks down the necessary reasoning steps for solving the target task. We choose to use the pseudocode format over the form of natural language plan (Kojima et al., 2022; Wang et al., 2023) for two main reasons: (1) the efficiency of it in describing the logic behind a task (*e.g.*, avoid using repetitive instructions via for loop), and (2) the guidance of what and when to generate rationales via the argument in print () statement and the location within the execution of code. For example, in Figure 2, the  $\mathcal{P}$  contains the statement, print(f"{person1} says {person2} {action}. {person1} tells the truth: {truth\_dict[person1]}"), which instructs the Reasoner LM to generate a rationale that is helpful in keep tracking of the truth map containing the truthfulness of each person, during the execution of  $\mathcal{P}$ . We provide more examples and detailed explanations in Appendix G.

# **2.2** EXECUTE: Simulating the Execution of Pseudocode Prompt for an Instance

The reasoner LM  $\mathcal{R}$  then conducts reasoning with the generated pseudocode prompt  $\mathcal{P}$ , tailoring the logic in  $\mathcal{P}$  for the given instance. Following Wei et al. (2022), we aim to maximize the reasoning abilities of the LM by instructing them to explicitly generate intermediate reasoning steps, known as chain-of-thought (CoT) reasoning.  $\mathcal{R}$  is instructed to predict not only the final output result of the code, but also the intermediate execution outputs as rationales. Specifically,  $\mathcal{R}$  predicts a list of outputs

 $<sup>^{2}</sup>$ We use the questions of the examples instances in the few-shot prompt in Big-Bench Hard.

Reasoner/Method	DL	GS	Nav	СО	TS	SO	WL	Avg
CodeLlama-7B								
Direct Prompting	0.0	9.0	39.0	<u>24.4</u>	4.4	11.2	<u>47.6</u>	19.4
Zero-shot CoT (Kojima et al., 2022)	0.0	16.8	26.0	10.8	20.0	10.4	44.8	18.4
NL Planning	0.0	10.0	<u>52.0</u>	0.4	7.6	<u>18.8</u>	50.4	<u>19.9</u>
Zero-shot PoT (Chen et al., 2023)	0.0	10.0	47.2	23.6	4.4	3.2	45.2	19.1
THINK-AND-EXECUTE	2.0	<u>13.2</u>	70.8	49.6	<u>19.2</u>	22.0	38.8	30.8
CodeLlama-13B								
Direct prompting	0.0	3.2	39.0	28.8	0.0	6.8	37.2	16.4
Zero-shot CoT (Kojima et al., 2022)	0.0	24.8	<u>62.4</u>	28.0	<u>21.6</u>	15.6	44.8	<u>28.2</u>
NL Planning		8.8	24.8	28.8	7.2	17.6	53.6	20.3
Zero-shot PoT (Chen et al., 2023)		16.4	45.6	<u>38.8</u>	10.8	35.6	20.4	24.1
THINK-AND-EXECUTE		<u>18.4</u>	70.4	50.4	25.2	<u>32.4</u>	<u>49.6</u>	36.3
GPT-3.5-Turbo								
Direct prompting	1.0	33.0	57.0	52.4	41.2	20.0	54.0	36.9
Zero-shot CoT (Kojima et al., 2022)	<u>4.4</u>	46.8	73.2	70.4	44.4	37.6	<u>59.2</u>	48.0
NL Planning	1.2	35.6	58.8	46.8	32.0	<u>40.0</u>	50.4	37.8
Zero-shot PoT (Chen et al., 2023)		21.2	77.2	45.6	0.4	28.0	54.0	32.4
Chain-of-Code (Li et al., 2023)		17.6	57.2	26.0	16.8	29.6	46.4	28.1
Plan-and-Solve (Wang et al., 2023)		41.2	<u>84.8</u>	74.8	<u>52.4</u>	37.2	58.0	<u>50.3</u>
THINK-AND-EXECUTE	6.0	<u>41.6</u>	96.8	<u>72.0</u>	68.0	65.6	72.8	60.4

Table 1: Zero-shot performance of THINK-AND-EXECUTE compared with the baselines on seven algorithmic reasoning tasks, including Dyck Languages (DL), Geometric Shapes (GS), Navigate (Nav), Reasoning about Colored Objects (CO), Temporal Sequences (TS), Tracking Shuffled Objectives (SO), and Web of Lies (WL). We curate these tasks from Big-Bench Hard (Suzgun et al., 2022).

 $O = \{o_1, o_2, ..., o_k\}$  of the pseudocode by simulating the execution process of  $\mathcal{P}$ , where  $o_i$  denotes the *i*-th system output from print () statements, and  $\{o_1\}_1^{k-1}$  are CoT rationales toward the final answer  $o_k$ . We assume that tracking intermediate execution results would benefit  $\mathcal{R}$  to keep track of the state of variables while they change over the execution of the code. We enable  $\mathcal{R}$  to mimic the behavior of a compiler with a system message "Generate the expected outputs (from all print() functions) of the code.". The final answer for a given

question is outputted with "print("Final answer:  $\{answer\}$ ")" command as the last system output  $o_k$ .

#### **3** Experimental Setup

#### 3.1 Datasets

We curate seven algorithmic reasoning tasks from Big-Bench Hard (Suzgun et al., 2022), including: dyck languages; geometric shapes; navigate; reasoning about colored objects; temporal sequence;tracking shuffled objectives; web of lies. These are specifically designed to measure the stepby-step reasoning capability of LLMs. Model performance on evaluated in **zero-shot** settings, where we do not provide demonstrations in the prompt. We provide detailed explanations in Appendix A.5.

#### 3.2 Baselines

We consider the following baselines: (1) **Direct prompting**: Directly predicting the answer without generating any rationales. (2) **Zero-shot CoT** (Kojima et al., 2022): A setting where LLMs are evoked to generate the reasoning steps with "*Let's think step by step*", before the answer. (3) **Zeroshot PoT** (Chen et al., 2023): A setting where an LLM generates an instance-specific Python code that can be executed with a Python interpreter. Then, the execution result is used as the final answer. (4) **NL planning**: A variation of THINK-AND-EXECUTE, where the task-level plan is generated in *natural language*, instead of pseudocode.

#### 3.3 Models

For the Reasoner LM  $\mathcal{R}$ , we adopt GPT-3.5-Turbo (OpenAI, 2023), which shows strong performance in various reasoning benchmarks and code generation tasks (Zellers et al., 2019; Cobbe et al., 2021; Muennighoff et al., 2024), as well as the 7B and 13B versions of CodeLlama (Roziere et al., 2023), which are trained on both code and natural language corpora and further fine-tuned to follow natural language instructions. As for the Instructor LM  $\mathcal{I}$ , we choose GPT-3.5-Turbo.

## 4 Results

### 4.1 THINK-AND-EXECUTE Improves Algorithmic Reasoning

We start by comparing our framework with direct prompting and zero-shot CoT (Kojima et al., 2022) in Table 1. We find that zero-shot CoT performs better than direct prompting with average improvements of 11.1% with GPT-3.5-Turbo, respectively, suggesting zero-shot CoT to be a strong baseline. Our THINK-AND-EXECUTE, however, further outperforms both of them significantly regardless of model sizes, which indicates that explicitly generating a plan is a more effective way to improve the LLM's reasoning than simply encouraging LLMs to generate their intermediate reasoning steps.

### 4.2 Task-level Pseudocode Prompts Benefits a Wider Range of Algorithmic Reasoning Tasks than Instance-specific Python Code

In Table 1, PoT shows performance gains in some tasks over direct prompting (*e.g.*, Navigate; Tracking Shuffled Objects) with Python code generated specifically for each instance and the corresponding interpreter output as the answer. However, such improvement is difficult to generalize to all tasks, *e.g.*, 0.4% accuracy in both Dyck Language and Temporal Sequences, with GPT-3.5-Turbo. By contrast, THINK-AND-EXECUTE outperforms PoT and direct prompting in all tasks with GPT-3.5-Turbo. This suggests that making the task-level strategy with pseudocode and applying it to each instance can benefit LLM's reasoning in a wider range of algorithmic reasoning tasks than generating instance-specific Python codes.

# **4.3** The Logic Discovered by an LLM can be Transferred to SLMs

We further explore if the pseudocode prompt written by an LLM (*i.e.*, GPT-3.5-Turbo as the instructor) can be applied to smaller LMs: the CodeLlama family in Table 1. When applying the pseudocode prompts generated by GPT-3.5-Turbo, CodeLlama-7B and -13B significantly outperform direct prompting. Moreover, THINK-AND-EXECUTE with CodeLlama-13B shows compara-

Method	Avg
w/o Analysis	21.8
THINK-AND-EXECUTE	60.4

Table 2: Ablation on Step2 of THINK phase.

ble performance with GPT-3.5-Turbo with PoT and direct prompting.

## 4.4 Pseudocode Better Describes the Logic for Solving a Task than Natural Language

We also compare our approach with NL planning, a variant of ours that utilizes natural language to write the task-level instruction, instead of pseudocode. In practice, we provide human-written NL plans that contain a similar amount of information to  $\mathcal{P}$  in the meta prompt and use it to generate the task-level NL plan for the given task. Surprisingly, although the LMs are fine-tuned to follow natural language instructions, we find that task-level pseudocode prompts can boost their performance more than NL plans (Table 1).

## 4.5 Ablation Studies

Components of the pseudocode prompt. We conduct an ablation study on each component of the pseudocode prompt. For that, we prepare four types of pseudocode prompts: (1) Human-written pseudocode; (2) Human-written prompt w/o comments and semantics by removing the comments that explain the code and replacing variable names with meaningless alphabets, such as X, Y, and Z; (3) Human-written prompt w/ for loop and (4) w/ intermediate print() statements. The results are in Figure 3. Model performance decreases significantly when applying prompts w/o comments and semantics, especially in Temporal Sequences. This implies that semantics play an important role in guiding the LLMs to apply the discovered logic and reasoning with it accordingly. Also, we find that printing out the intermediate execution steps with print() is crucial in reasoning, which is consistent with the finding from Wei et al. (2022).

**Generating the analysis before the pseudocode prompt.** Table 2 shows a notable decrease in model performance when generating pseudocode prompts without conducting the analysis first. This suggests that explicitly generating analysis on the task can elicit a better pseudocode prompt that contains the necessary logic for solving the task.

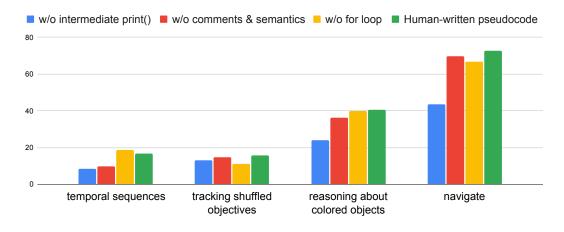


Figure 3: Ablation study of the components of pseudocode prompt using GPT-3.5-Turbo.

Method	Avg
Self-Discover w/ GPT-4	77.9
THINK-AND-EXECUTE w/ GPT-4	81.7

Table 3: Comparison of THINK-AND-EXECUTE and Self-Discover (Zhou et al., 2024) using GPT-4 on Big-Bench Hard. The results of Self-Discover are obtained from the original paper, because the code and prompts are not provided. The full results are in Appendix A.4.

#### 4.6 Comparison with other Baselines

We further compare THINK-AND-EXECUTE with another three baselines: (1) Plan-and-Solve (Wang et al., 2023), where an LLM sequentially generates a natural language plan for solving the given instance, step-by-step reasoning according to the plan, and the final answer; (2) Chain-of-Code (Li et al., 2023), where Python code is generated as a part of intermediate reasoning steps specifically for a given instance; (3) Self-Discover (Zhou et al., 2024), a concurrent work that devises a task-level reasoning structure in a JSON format before inferencing the instance. First, as presented in Table 3 (Left), we find THINK-AND-EXECUTE largely outperforms Plan-and-Solve and Chain-of-Code by 10.9 and 32.3 percentage points in terms of accuracy, respectively. Second, while Self-Discover also incorporate task-level instruction, in Table 3 (Right), our THINK-AND-EXECUTE with pseudocode prompts shows better performance when using GPT-4 (Achiam et al., 2023).<sup>3</sup> These findings indicate that generating (1) task-level instruction with (2) pseudocode can better represent the necessary logic for solving a task and benefit LLM's

algorithmic ability.

#### 5 Analysis

We conduct experiments to address the following research questions:

- **RQ1**: Is task-level pseudocode more helpful than instance-specific pseudocode?
- **RQ2**: Does pre-training on code corpora improve reasoning?
- **RQ3**: How is the quality of the logic discovered by THINK-AND-EXECUTE compared to human-written logic?

#### 5.1 Implementing the Underlying Logic is more Effective than Instance-specific Logic in Pseudocode (RQ1)

We conduct an analysis to check if the improvement of THINK-AND-EXECUTE is contributed by our chosen format for the task-level instruction, *i.e.*, pseudocode. We compare THINK-AND-EXECUTE with a concurrent work, Chain-of-Code (CoC) (Li et al., 2023). In Table 1, THINK-AND-EXECUTE outperforms CoC, showing about 2x improvement in the average score. The main difference between THINK-AND-EXECUTE and CoC is that we use pseudocodes which are generated to express logic shared among the tasks instances, while CoC incorporates pseudocode as part of the intermediate reasoning steps towards the solution of a given instance. Hence, the results indicate the advantages of applying pseudocode for the generation of task-level instruction by re-using them over solely using them as a part of the rationales.

<sup>&</sup>lt;sup>3</sup>We use gpt-4-0613 for GPT-4.

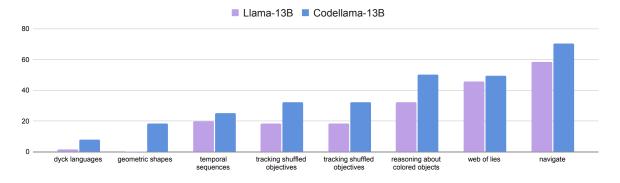


Figure 4: Analysis on the effect of code pre-training on the reasoning capability in applying THINK-AND-EXECUTE. Without pre-training on code corpora the accuracies drop notably.

<b>Reasoner/Method</b>	DL	GS	Nav	CO	TS	SO	WL	Avg
CodeLlama-7B								
Human-written $\mathcal{P}$	2.4	0.0	40.4	29.6	12.0	18.0	52.8	22.2
THINK-AND-EXECUTE	2.0	13.2	70.8	49.6	19.2	22.0	38.8	30.8
CodeLlama-13B								
Human-written $\mathcal{P}$	2.8	14.8	72.8	40.4	16.8	15.6	49.6	30.4
THINK-AND-EXECUTE	8.0	18.4	70.4	50.4	25.2	32.4	49.6	36.3
GPT-3.5-Turbo								
Human-written $\mathcal{P}$	12.4	50.0	86.0	50.8	84.0	32.4	74.4	55.7
THINK-AND-EXECUTE	6.0	41.6	96.8	72.0	68.0	65.6	72.8	60.4

Table 4: Comparison between THINK-AND-EXECUTE and Human-written  $\mathcal{P}$ .

#### 5.2 THINK-AND-EXECUTE Requires Knowledge in Code (RQ2)

To understand whether SLMs acquire the ability to understand the task-level logic written in pseudocode during pre-training on code corpora, we compare the performance of CodeLlama-13B with Llama-13B using THINK-AND-EXECUTE. In Figure 4, CodeLlama-13B shows better reasoning capabilities compared to Llama-13B in all tasks. These results suggest that the improvement from using THINK-AND-EXECUTE could depend on the knowledge of code, which is usually obtained by pre-training with code corpora. Writing code usually involves understanding the logic behind the given problem and expecting the execution results of a code, which resemble the same reasoning process of THINK-AND-EXECUTE.

## 5.3 Models Prefer Pseudocode from THINK-AND-EXECUTE Compared to Human's (RQ3)

To gauge LLMs' capabilities in discerning the underlying logic of a task, we compare THINK-AND-EXECUTE (using GPT-3.5-Turbo as the In-

structor) with human-written pseudocode prompts. The results are shown in Table 4. Using the GPT-3.5-Turbo the Reasoner, THINK-AND-EXECUTE scores 60.4% in terms of accuracy, which is superior to the human-written  $\mathcal{P}$  (with an accuracy of 55.7%). Especially, in the tasks of Navigate and Tracking Shuffled Objectives, pseudocode prompts generated by THINK-AND-EXECUTE elicit better performance. This also holds true when adopting CodeLlama-7B and -13B as the Reasoner, further suggesting the effectiveness of our THINK step over human prompt engineers.

# 5.4 Impact of LLMs' Capability on THINK-AND-EXECUTE

In examining the impact of LLMs' capabilities within our framework, we investigate the influence of both the Reasoner and Instructor components on performance, as depicted in Table 5. Notably, higher accuracy scores are observed when utilizing GPT-3.5-Turbo as Reasoners compared to CodeLlama-13B and CodeLlama-34B. Additionally, the effectiveness of the Instructor also plays a crucial role, with GPT-3.5-Turbo exhibiting the

Reasoner	Instructor				
	CodeLlama-13B	CodeLlama-34B	GPT-3.5-Turbo		
CodeLlama-13B	30.9	33.0	36.4		
CodeLlama-34B	32.5	34.2	39.1		
GPT-3.5-Turbo	33.9	35.9	60.4		

Table 5: Analysis of the effect of the capability of Reasoner and Instructor on the performance. We report the average performance on the 7 tasks.

Method	Generating ${\cal P}$	Reasoning with ${\cal P}$
Chain-of-Code	$N * C_1$	$N * C_2$
Ours	$1 * C_1$	$N * C_2$

Table 6: Number of tokens used by THINK-AND-EXECUTE for each step of pseudocode generation (Think, denoted as  $C_1$ ) and reasoning with pseudocode (Execute, denoted as  $C_2$ ).

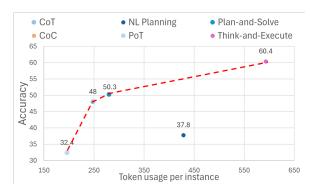


Figure 5: Analysis on the computational efficiency of THINK-AND-EXECUTE on the 7 algorithmic reasoning tasks. The dotted line denotes the Pareto frontier.

highest accuracy scores across all configurations. These results underscore the significance of both the Reasoner and Instructor components in enhancing the performance of THINK-AND-EXECUTE.

# 5.5 THINK-AND-EXECUTE is cost-effective by re-using the generated pseudocode

We analyze the computational efficiency of THINK-AND-EXECUTE. First, we analytically calculate the amount of token usage by breaking our framework into two steps, *i.e.*, Think (Section 2.1) and Execute (Section 2.2). We denote the number of token usage for each step as  $C_1$  and  $C_2$ , respectively. As we show in Table 6, our task-level approach is Ntimes efficient in pseudocode generation, as we reuse the generated prompt for shared task instances.

In addition, we empirically measure the token usage and compare it with task performance. The results are shown in Figure 5. While THINK-AND-

Method	Accuracy
СоТ	8.7
РоТ	12.6
NL Planning	9.7
Chain-of-Code	14.6
Plan-and-Solve	4.9
THINK-AND-EXECUTE	25.7

Table 7: Results on SayCan, a task designed for planning in robotics. The baselines are zero-shot settings.

EXECUTE requires more token usage compared to the baselines, such as CoT and PoT, we would like to highlight that our method remains competitive when considering both performance and cost. When plotting accuracy against cost per instance, our approach sits at the pareto-front, indicating an optimal trade-off between these factors. Thus, we believe THINK-AND-EXECUTE remains a viable option, particularly in scenarios where performance takes precedence over cost.

#### **5.6** Application to Planning in Robotics

We investigate whether THINK-AND-EXECUTE can be applied to real-world tasks that require logical reasoning. As a demonstrative experiment, we apply THINK-AND-EXECUTE on SayCan, where the task is to generate plans (*i.e.*, a sequence of actions) for robots. This task requires LLMs to generate actions that robots can operate, thus it requires meeting some constraints (i.e., action space). We use the same meta prompt and follow the same pipeline as our main experiments in Section 4. We shot the results in Table 7. We find that THINK-AND-EXECUTE generates more accurate plans compared to the baselines by incorporating task-level pseudocode prompts. The results suggest a possibility that Think-and-Execute can be applied to real-world tasks.

#### 6 Related Work

**Chain-of-Thought (CoT) prompting.** CoT prompting evokes LMs to generate intermediate reasoning steps that guide and explain the solution toward the final answer (Wei et al., 2022; Wang et al., 2022; Wu et al., 2023). One common paradigm of this is zero-shot CoT prompting (Kojima et al., 2022). Without specifically designed question-explanation-answer triplets as demonstrations, zero-shot CoT prompting elicits a plausible reasoning path towards the final answer with simple instruction, such as "Let's think step-by-step", eliciting better model performance in tasks that require multi-step reasoning.

In the context of improving zero-shot CoT, Wang et al. (2023) propose to first generate a plan breaking down the target task into smaller subtasks, and then solve each subtask according to the plan. Similar to our approach, a concurrent work (Zhou et al., 2024) devises a task-level reasoning structure that can be applied to each instance (question) of the target task. The most significant distinction between these prior studies and ours is that our THINK-AND-EXECUTE adopts **pseudocode** (as opposed to natural language) to express the necessary logic for solving the task. We demonstrate that our tasklevel pseudocode prompt empowers LMs with better ability of zero-shot reasoning than natural language plans under various settings in Section 5.

**Incorporation of code in reasoning.** With unambiguous syntax and strict structure, programming languages such as Python have been applied to LLM-based systems to improve system performance in solving tasks. For instance, Gao et al. (2023) and Chen et al. (2023) use LLMs to generate Python code for given mathematical questions, and run the generated code on external compilers to obtain/calculate the answers.

Besides, there has been a line of work on improving LLMs' capabilities with pseudocode (Zelikman et al., 2023; Mishra et al., 2023). Concurrently with our work, Li et al. (2023) present chain-of-code (CoC), where pseudocode is also incorporated along with the Python code for solving a given question (instance). While this approach generates instance-specific code as intermediate reasoning steps for each individual instance, our THINK-AND-EXECUTE, by contrast, focus on the task-level pseudocode prompt that can be applied to all instances. We compare CoC and THINK-AND-EXECUTE in Section 4. Another concurrent work (Weir et al., 2024), inspired by our study, delves into training LLMs that are specialized to generate task-level pseudocodes.

### 7 Conclusion

In this paper, we present THINK-AND-EXECUTE, an algorithmic reasoning framework that generates a logic for solving the given task into a pseudocode and performs reasoning by simulating the execution of the pseudocode with language models. Through extensive experiments, we show the effectiveness of THINK-AND-EXECUTE, over the strong baselines. These results underscore not only the usefulness of pseudocode in eliciting language models' reasoning capabilities but also the efficiency of our framework in discovering the high-quality logic behind a given task.

#### 8 Limitations and Discussion

A possible limitation of our approach is that we focus on algorithmic reasoning, as we believe it is the best setting to assess LLMs' capabilities in understanding complex logic and carrying out a sequence of reasoning step, following the logic. However, we believe that THINK-AND-EXECUTE can be applied to other domains of reasoning that require following a long sequence of reasoning steps, such as multi-hop reasoning (Ji et al., 2020) and symbolic reasoning (Madaan and Yazdanbakhsh, 2022). As an example of these tasks, we conduct a demonstrative experiment in Section 5.6 and we find that THINK-AND-EXECUTE also can applied to real-world tasks opening up new possibilities for complex reasoning in diverse practical applications. Lastly, our framework requires a set of human-annotated meta prompts for pseudocode generation, but we believe that the provided meta prompt can be a promising starting point.

#### Acknowledgement

This work was supported by Institute of Information & Communications Technology Planning & Evaluation (IITP) grant funded by the Korean government (MSIT)(No.RS-2020-II201361, Artificial Intelligence Graduate School Program (Yonsei University)) and (No.RS-2021-II212068, Artificial Intelligence Innovation Hub) and (2022-0-00077, RS-2022-II220077, AI Technology Development for Commonsense Extraction, Reasoning, and Inference from Heterogeneous Data). Jinyoung Yeo is the corresponding author.

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#### **A** Experimental Details

#### A.1 Models

We use several LLMs, including GPT-3.5-Turbo (OpenAI, 2023) and GPT-4 (Achiam et al., 2023), which are available via OpenAI API<sup>4</sup>, and opensource LLM, CodeLlama (Roziere et al., 2023) as the Instructor LM  $\mathcal{I}$  and the Reasoner LM  $\mathcal{R}$ .

- GPT-3.5-Turbo: gpt-3.5-turbo-0125
- **GPT-4**: gpt-4-0613
- CodeLlama: CodeLlama encompasses variations of LLaMA2 fine-tuned for code domains using code corpus. This comprehensive collection features models of various sizes (7B, 13B, 34B, and 70B) and diverse types, including the foundation model, Python-focused model, and instruction-following model. In our study, we employ the CodeLlama-Instruct model (7B<sup>5</sup>, 13B<sup>6</sup>).

### A.2 Inference

We use vLLM to improve inference throughput.<sup>7</sup> During our experiments, we adopt temperature sampling with T = 0.0 (*i.e.*, greedy decoding) to efficiently generate outputs. For a task comprising 250 instances, GPT-3.5-Turbo achieves an inference time of 30 seconds. Additionally, utilizing 2 A100 GPUs, CodeLlama achieves inference times of approximately 2 and 5 minutes for 7B and 13B models, respectively.

#### A.3 Evaluation

To extract answers for evaluation, LLMs generate the final answer triggered by the phrase "Final answer: ". Following Suzgun et al. (2022), we provide all multiple-choice options to LLMs as input, then measure accuracy using exact match (EM), which compares the generated output with the ground-truth label. To ensure fair comparison between PoT and other baselines, we also admit the prediction that includes the text of correct choice, *e.g.*, blue, but without a choice tag, *e.g.*, "(A)".

#### A.4 Experimental Results

We provide the full result of comparison with Self-Discover (Zhou et al., 2024).

```
CodeLlama-13b-Instruct-hf
<sup>7</sup>https://github.com/vllm-project/vllm
```

#### A.5 Datasets

We take 7 algorithmic benchmarks from Big-Bench Hard (Suzgun et al., 2022) dataset. All datasets contain 250 examples respectively. We provide the descriptions of each dataset regarding the goals and contexts.

- Dyck Languages (DL): Complete a partially given Dyck-4 sequence by predicting the necessary sequence of closing brackets that are missing at the end.
- Geometric Shapes (GS): Determine the geometric figure formed by following all the instructions in a specified SVG path element containing several commands.
- Navigate (Nav): Evaluate whether a set of directional commands will return a navigator to the starting point.
- Reasoning about Colored Objects (CO): Given a scenario, deduce the color of a specific object placed on a surface, using the provided context for guidance.
- **Temporal Sequences (TS)**: Examine a chronology of a person's daily activities to find when they could fit an additional activity into their schedule.
- Tracking Shuffled Objectives (SO): Ascertain the final positions of several objects after they have been moved from their original locations through a sequence of exchanges. We use the version of the task with 5 objectives.
- Web of Lies (WL): Assess the veracity of a Boolean function presented within a narrative problem to establish its truthfulness.

#### **B** Details of THINK-AND-EXECUTE

# B.1 Human-annotation on the Tasks in the Task Pool

Please see Appendix D for human-written pseudocode prompts.

#### **B.2** Components of a Pseudocode Prompt

We highlight some components of code prompt that would be helpful in describing the underlying reasoning logic.

<sup>&</sup>lt;sup>4</sup>https://openai.com/blog/openai-api <sup>5</sup>https://huggingface.co/codellama/ CodeLlama-7b-Instruct-hf <sup>6</sup>https://huggingface.co/codellama/

Reasoner/Method	DL	GS	Nav	CO	TS	SO	WL $\parallel$ Avg
Self-Discover	<b>77.0</b>	60.0	<b>90.0</b>	79.0	<b>100.0</b>	68.0	71.077.988.482.8
THINK-AND-EXECUTE	55.6	<b>72.8</b>	70.0	<b>96.0</b>	97.2	<b>99.6</b>	

Table 8: Comparison between THINK-AND-EXECUTE and Self-Discover (Zhou et al., 2024) using GPT-4.

- Conditional branch: To allow the reasoning model to take different reasoning paths based on the condition, we use if and else statement to describe the logic.
- Loop: We can efficiently present repetitive instructions that iterate over a list of items by using loops, such as for and while loop.
- Abstraction: In programming, we can encapsulate a complex logic into a single function. Focusing on this, we adopt modular design in constructing pseudocode prompts by encapsulating complex and repetitive process into an abstract function.
- Variables: Variables are essential in programming languages as they store data values to execute instructions. Similarly, in reasoning, keeping track of variables is crucial for maintaining state, passing data, and for general data manipulation tasks.
- **Comments and docstrings**: As human programmers can rely on the assistance of comments to better understand codes, we provide more detailed explanations on the intent of code via comments. Also, comments and docstrings can compensate the limitation when some semantics cannot be directly expressed with programming language.

#### **B.3** Comparison to Related Work

Table 9 summarizes some related approaches to ours.

Method	Granularity of plan/logic	Use of pseudocode	Transferability to SLMs
Plan-and-Solve (Wang et al., 2023)	Instance-level	×	×
Self-Discover (Zhou et al., 2024)	Task-level	×	×
Chain-of-Code (Li et al., 2023)	Intance-level	✓	×
THINK-AND-EXECUTE (this work)	Task-level		<b>V</b>

Table 9: A comparison of THINK-AND-EXECUTE to closely related prior approaches.

### **C** Prompts Used in Our Experiments

# C.1 Meta Prompt for generating an analysis (THINK: Step 2).

```
Generate an explanation, analyzation,
and plan to generate code prompt for
the last task considering the example
task instances. Your plan should show
enough intermediate reasoning steps
towards the answer. Construct the plan
as much as you can and describe the
logic specifically. When constructing
the plan for the code prompt, actively
use 'if else statement' to take
different reasoning paths based on the
condition, 'loop' to efficiently
process the repititive instructions, '
dictionary' to keep track of
connections between important variables
```

```
[Example 1]
Example task instances:
{example_instances_of_task1}
```

```
Output format:
{output_format_of_task1}
```

```
Explanation:
{analysis_of_task1}
```

• • •

```
[Example 4]
Example task instances:
{example_instances_of_target_task}
```

```
Output format:
{output_format_of_target_task}
```

Explanation:

# C.2 Meta Prompt for pseudocode prompt genration (THINK: Step 3).

Generate the code prompt for the last task using the similar style of the example codes. Add enough print() functions following the provided steps in the provided explanation to output intermediate reasoning steps towards the answer and keep track of important variables. Implement the code prompt as much as you can and describe the logic

```
in code following the provided
explanation but do not make a code that
is biased toward a single task example
instance. For example, do not use hard
-coded variables that are obtained from
task instances (e.g., using specific
name of person in the question). The
code prompt must be able to be applied
to various instances of same task. When
returning the final answer, carefully
consider the output format. Especially,
for the multiple choice questions, the
final answer should be one of the
given options. The main function name
should be '{function_name}'. Along with
the main function, you may want to
define some helper functions that might
be helpful for implementing the '{
function_name}'. But you don't have to
explicitly implement the helper
functions, but just define them with
function name and a single-line
explanation in comment. When
constructing the main function, ...
[Example 1]
Task description:
{description_of_task1}
Example task instances and the code
usage:
example_task_instances_and_code_usages_of_targ
Format of the Final answer:
{output_format_of_task1}
Explanation:
{analysis_of_task1}
Code prompt:
{code_prompt_of_task1}
. . .
[Example 4]
Task description:
{description_of_target_task}
Example task instances and the code
                                                  run the code and do not care about 'not
usage:
                                                  implemented error'.
{
example_task_instances_and_code_usages_of_targ
Format of the Final answer:
{output_format_of_target_task}
Explanation:
{analysis_of_target_task}
Code prompt:
```

### C.3 Prompt for NL Planning

```
Generate a plan for the last task
   considering the example task instances.
   Your plan should show enough
   intermediate reasoning steps towards
   the answer. Construct the plan as much
   as you can and describe the logic
   specifically.
   [Example 1]
   Task description:
   {description_of_task1}
   [Example 1]
   Example task instances:
   {example_instances_of_task1}
   Output format:
   {output_format_of_task1}
   Plan:
   {analysis_of_task1}
    . . .
   [Example 4]
   Example task instances: {
   example_instances_of_target_task}
   Output format:
   {output_format_of_target_task}
   Plan:
C.4 Prompt for EXECUTE phase
   {prompt}
   input_text = "{input_text}"
   final_answer = {function_name}(
   input_text)
   print("Final answer:"+ final_answer)
   Generate the expected execution output
   (output from all print() functions) of
   the code. You don't have to actually
```

#### C.5 Prompt for evaluating Direct Prompting

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
```

```
C.6 Prompt for evaluating Zero-shot CoT
```

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
Let's think step by step.
```

#### C.7 Prompt for evaluating Zero-shot PoT

```
You will write python program to solve
the below problem. You will only write
code blocks. Your python promgram must
be executable and returns the right
answer for the problem.
```

Q: {question}

```
# solution using Python:
```

```
def solution():
    """{question}"""
```

### C.8 Prompt for evaluating Plan-and-Solve

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
Let's first understand the problem and
devise a plan to solve the problem.
Then, let's carry out the plan and
solve the problem step by step.
```

## D Human-written Pseudocode Prompts

#### **D.1** Human-written $\mathcal{P}$ of Dyck Languages

```
def complete_dyck_languages(input_text)
:
    # Step 1: Initialize a stack to
keep track of open parentheses and
split the input text to identify and
define all types of open parentheses in
the text.
    stack = []
    character_list = input_text.split()
    open_to_close_parenthesis_dict = {"
(": ")", "<": ">", "{": "}", "[": "]"}
    opening_parenthesis = ["(", "<", "{"; "]"})</pre>
```

```
input and initialize a stack to track
of open parentheses. \nCurrent stack: {
stack}. Parsed characters: {
character_list}")
   # Step 2: Through iteration over
the input characters, identify opening
parentheses among the input characters
and add them to the stack.
   print("Check if a character is an
opening parenthesis while iterating
over the input characters.")
   for char in character_list:
       if char in opening_parenthesis:
                       print(f"
Iteration {i+1}: Current character {
char} is an opening parenthesis.")
           stack.append(char)
           print(f"Thus, we append {
char} to the stack. Current stack after
insertion: {', '.join(stack)}")
       # Step 3: For each open
parentheses, find the corresponding
closing parentheses and close the open
parentheses.
```

print(f"Parse characters in the

else:

```
print(f"Iteration {i+1}:
Current character {char} is not an
opening parenthesis.\n Thus we delete
the last item {stack[-1]} from the
stack\n current stack before deletion:
{" ".join(stack)} -> updated stack
after deletion: {' '.join(stack[:-1])
if stack else 'empty'}")
```

stack.pop() # Remove the last added open parentheses assuming a correct match.

# Step 4: Generate the sequence of closing parentheses based on remaining open parentheses in the stack.

```
print(f"The resulting stack is {'
'.join(stack)}.")
```

```
print(f"We will need to pop out {'
'.join(stack[::-1])} one by one in that
order.")
```

closing\_list = [parentheses\_pairs[
opening] for opening in stack[::-1]]

# Step 5: Output the completed
sequence. Generate the input sequence
concatenated with the generated closing
sequence of parentheses, ensuring a
well-formed structure.
 return " ".join(closing\_list)

#### **D.2** Human-written $\mathcal{P}$ of Geometric Shapes

```
def recognize_shape_from_svg(input_text
):
    # Step 1: Get the SVG path data
from the input text and generate the
extracted SVG path.
```

```
paths = parse_path(input_text)
print("SVG paths:\n ", paths)
```

# Step 2: Initialize a coordinate
map that maps each coordinate with the
other connected coordinates and the
connection type.

coordinate\_map = dict()

```
# Step 3: Update the coordinate map
referring to the each SVG path.
    for i, path in enumerate(paths):
        coordinate_map =
    update_coordinate_map(coordinate_map,
    path)
        print(f"Step {i} - path: {path},
```

updated coordinate map: {coordinate\_map
}")

# Step 4: Conduct calculation to analyze each characteristic of the shape.

```
analysis_results_dict =
analyze_characteristics(coordinate_map)
    print(f"Anlysis results: {
analysis_results_dict}")
```

# Step 5: Identify a geometric shape with reasons using the completed coordinates map and the analysis results.

reason\_for\_the\_decision, name\_of\_the\_shape = identify\_shape\_with\_explanation( coordinate\_map, analysis\_results\_dict) print(f"Reason for the decision: { reason\_for\_the\_decision}") print(f"Thus, the shape of the path is {name\_of\_the\_shape}.")

# Step 6: Find the corresponding
option from the given options and only
output the label of the option as the
final answer to the question.
options = parse\_options(input\_text)

```
print(f"Options: {options}")
answer = None
for option in options:
    if name_of_the_shape in option:
        answer = option[:3]
```

return answer

#### **D.3** Human-written $\mathcal{P}$ of Navigate

```
def ends_up_at_start(input_text):
    # Step 1: Initialize coordinates
and direction by setting the starting
point at (0, 0) and face north.
    cur_x, cur_y = 0, 0
    cur_direction = 0
    # Step 2: Identify and list up
instructions from the input text
```

```
instructions from the input text.
    instructions = parse_instructions(
    input_text)
```

```
# Step 3: Process each instruction
and update the current coordinates and
direction. In order to keep track of
changes, output the instruction,
current and updated coordinates and
direction.
   for i, instruction in enumerate(
instructions):
       new_x, new_y, new_direction =
process_instruction(instruction, cur_x,
cur_y, cur_direction) # process
instruction to calculate new position
and direction
       print(f"Step {i}: {instruction}
- current coordinates: ({cur_x}, {
cur_y}), current direction: {
cur_direction} -> updated coordinates:
({new_x}, {new_y}), updated direction:
{new_direction}")
       cur_x, cur_y, cur_direction =
new_x, new_y, new_direction
   # Step 4: Return "yes" if the final
coordinates are (0, 0). Otherwise,
return "no" as the final answer.
   return 'yes' if cur_x == 0 and
```

```
cur_y == 0 else 'no'
```

# D.4 Human-written $\mathcal{P}$ of Reasoning about Colored Objects

```
def solve_colored_objects(input_text):
   # Step 1: Start by identifying the
objects along with their associated
properties, such as color and spatial
positioning from the input text. Show
the list of objects.
   objects_list = extract_objects(
input text)
  print("Objects and their properties
:", objects_list)
   # Step 2: Identify the specific
question asked. Determine whether the
question is about identifying the color
of a specific object, counting objects
of a certain color, or reasoning about
the spatial arrangement of objects and
output the question type.
   question = extract_question(
input_text)
   print("Question specifics:",
question)
   # Step 3: Identify and list up
available options provided in the input
text.
   options = input_text.split("\n")
[-5:1]
   # Step 4: Process according to the
question type and show what the
question type is:
```

```
# If the question is about
identifying color, identify and ouput
the target object the question is
asking for the color of. Determine and
output its color.
   if question['type'] == '
identify_color':
       print("Question type is =
identify_color")
        print(f"Identifying color for:
{question['details']}")
       target_object = target(
objects_list, question['details'])
       print(f"The question is asking
for the color of : {target_object}")
       pre_answer = extract_color(
target_object, question['details'])
       print(f"Identified color: {
pre_answer}")
   # If the question is about counting
```

objects, identify and ouput the objects, identify and ouput the objects the question is asking for the number of. Go through each object in the list in steps and count each object . Show the counting steps. Output the final number of objects that meet the specified criteria (e.g., a specific color). elif question['type'] == ' count\_objects':

```
print("Question type is =
count_objects")
    print(f"Counting objects for: {
question['details']}")
    print("Total iterations:", len(
objects_list))
    for i, object in enumerate(
objects_list):
```

single\_object\_count =
count\_single\_object(object, question['
details'])

pre\_answer = count\_objects(
objects\_list, question['details'])
 print(f"Objects count: {
 pre\_answer}")

```
# If the question is about spatial
reasoning, identify and ouput the
relative positions the question is
asking for. Arrange the objects from
left to right and output the order.
Determine the relative positions of
objects and output the result.
    elif question['type'] == '
spatial_reasoning':
        print("Question type is =
spatial_reasoning")
        print(f"Applying spatial
reasoning for: {question['details']}")
        arranged_object =
arrange_from_left_to_right(objects_list
```

```
print(f"Arraged objects: {
arranged_object})
        pre_answer = spatial_reasoning(
arranged_object, question['details'])
print(f"Spatial reasoning
result: {pre_answer}")
    # Step 5: Recall the identified
options and match the outcome of Step 4
(the identified color, the count of
objects, or the result of spatial
reasoning) with the provided options to
determine the correct answer.
   answer = find_correct_option(
pre_answer, options)
    # Step 6: Return the final answer
chosen at Step 5.
 return answer
```

#### **D.5** Human-written $\mathcal{P}$ of Temporal Sequences

```
def solve temporal sequences quiz(
input_text):
   # Step 1: Identify statements and
options from the input_text and output
the statements.
   statement_text, option_text =
input_text.split("\nOptions:\n")
   parts = statement_text.split("\n")
   statements = parts[1:-2]
   options = option_text.split("\n")
   print("Statements:", statements)
   # Step 2: Check the start and end
of the possible time.
   print("Start of the possible time:
", parts[0])
   print("End of the possible time: ",
parts[-2])
   # Step 3: Initialize an available
time map with the time slots in the
options and output it. The time slots
are marked as 'free' initially.
   available_time_map = {option[4:]: "
free" for option in options}
   print(f"Initial available time
dictionary: {available_time_map}")
    # Step 4: Sequentially go through
each statement, marking the times when
the individual was seen or known to be
engaged in specific activities. In this
step, you should generate the target
time slots and the updated available
time map according to the statement.
   for i, statement in enumerate(
statements):
       event, time_span =
extract_information(statement)
       print(f"\nStep {i}: {statement}
```

```
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```

```
print(f"current time occupation
: {available_time_map}")
       print(f"Time span to be
occupied: {time_span}")
       available_time_map[time_span] =
 "not available"
       print(f"updated time occupation
: {available_time_map}")
    # Step 5: By checking the available
time map, identify which time slot is
marked as 'free'. For each time slot,
output the time slot is free or not
available.
   for key in available_time_map:
        if available_time_map[key] == "
free".
            print(f"{key} is free.")
            free time = key
        else:
            print(f"{key} is not
available.")
   # Step 6: Review the provided
options and return the one that matches
the identified free time slot in Step
5.
   print(f"Options:\n{option_text}")
    for option in options:
        if free_time in option:
           return option
```

# **D.6** Human-written $\mathcal{P}$ of Tracking Shuffled Objectives

```
def track_swaps(input_text):
```

```
# Step 1: Identify Initial State.
Begin by identifying and outputing the
initial state of all objectives (e.g.,
who holds which ball or who is dancing
with whom) from the input text before
any swaps happen.
```

```
state_dict = find_initial_state(
input_text)
```

print(f"Initial state: {state\_dict}
")

# Step 2: Identify and output the sequences of swaps from the input text. Each swap should be understood in terms of who exchanges with whom.

```
swap_sequences_list =
find_swap_sequences(input_text)
    print("Swap sequences: ",
swap_sequences_list)
    print("Total iterations: ", len(
swap_sequences_list))
```

# Step 3: Carry out the swaps. For each swap in swap sequences, sequentially update and output the current status of objectives by exchanging them between the two participants involved in the swap. for i, sequence in enumerate(

```
swap_sequences_list):
```

```
player1, player2 =
extract_player(sequence)
    state_dict[player1], state_dict
[player2] = state_dict[player2],
state_dict[player1]
    print(f"({i}) {sequence} -> {
state_dict}")
```

Step 4: Understand the Question.
After processing all swaps, identify
what the question is asking for in the
input text and output the question.
 question = extract\_question(
input\_text)
 print("Question:", question)

Step 5: Analyze Options. Examine
and output the provided options in the
input text.
 options = input\_text.split("\n")
[-5:]
 print("Options:", options)

Step 6: Determine the Correct
Option. Using the updated state after
all swaps, determine which option
correctly answers the question and
output the answer.
 answer = find\_correct\_option(
question, options, state\_dict)

return answer

## **D.7** Human-written $\mathcal{P}$ of Web of Lies

```
def evaluate_boolean_word_problem(
input_text):
   # Step 1: Divide the input text
into individual statements and the
final question. Output each statements.
   statements = input_text.split("")
[:-1]
   question = input_text.split("")[-1]
   print("Parsed statements:",
statements)
   # Step 2: Create a Truth Map to
keep track of the assumed truthfulness
of each person mentioned in the
statements. No truth values are
assigned initially.
   truth_map = {statement.split()[0]:
None for statement in statements}
```

# Step 3: Analyze Each Statement. For each statement, first output the statement number and the statement. identify the subject person (who makes the statement), the object person (who the statement is about), and the expected truth value (whether the object person is said to tell the truth or lie). Output the current statement under analysis along with the object person and the expected truth value for

```
clarity.
   for i, statement in enumerate(
statements):
       print(f"({i}): {statement}")
        speaker, target_person,
expected_truth_value_of_target_person =
extract_person_and_truth_value(
statement) # speaker - says
target_person
expected_truth_value_of_target_person
       print(f"{speaker} says : {
target_person} - {
expected_truth_value_of_target_person}"
       print(f"Truth value of {
target_person}: {truth_map[
target_person]}")
        # Step 4: Update the Truth Map
based on the analysis of each statement
. If the statement's claim aligns with
the current assumption about the object
person's truthfulness, mark the
subject person as truthful. Otherwise,
mark them as untruthful. After each
update, print the name of the person
being updated, their determined truth
value, and the updated truth map to
track changes.
       if truth_map[target_person] ==
None: # if the statement does not need
to be checked
           print(f"{
expected_truth_value_of_target_person}
matches {truth_map[target_person]}")
            truth_map[target_person] =
expected_truth_value_of_target_person
       else:
           print(f"{
expected_truth_value_of_target_person}
does not match {truth_map[target_person
1 } ")
            if truth_map[target_person]
expected_truth_value_of_target_person:
# the speaker tells the truth
                truth_map[speaker] =
True
            else: # the speaker lies
                truth_map[speaker] =
False
        print(f"Person to update: {
speaker} - {truth_map[speaker]}")
       print(f"updated truth_map: {
truth_map}")
       print("\n\n")
    # Step 5: Using the completed truth
map, determine the truthfulness of the
person in the final question. Output
the question for reference before
making the determination.
   print("question:", question)
   target_person_in_question =
```

extract\_target\_person\_from\_question(

```
question)
    target_truth_value = truth_map[
target_person_in_question]
    print(f"{target_person_in_question
}: {target_truth_value})
    # Step 6: Based on the evaluation,
output "Yes" if the person in the final
question is determined to tell the
truth, otherwise output "No".
    answer = "Yes" if
target_truth_value else "No"
    return answer
```

## **E** Generated Analyses

### E.1 Generated Analysis of Dyck Languages

```
Explanation:
This task involves completing a
sequence of parentheses to ensure they
are closed properly. The challenge is
to understand the nesting structure of
the parentheses and add the appropriate
closing brackets to match each opening
bracket.
Analyzing the Task:
1. Parentheses Matching: Each opening
parenthesis should have a corresponding
closing parenthesis to ensure the
sequence is valid.
2. Nested Parentheses: The parentheses
can be nested within each other, so it'
s crucial to maintain the correct
nesting structure.
3. Proper Closure: The goal is to add
the necessary closing brackets to
complete the sequence and make sure all
parentheses are closed properly.
Constructing the Code Prompt:
1. Parsing Input: Extract the sequence
of parentheses from the input text.
2. Stack Implementation: Use a stack
data structure to keep track of the
opening parentheses that need closing.
3. Iterating Over the Sequence: Iterate
over each character in the sequence
and push opening parentheses onto the
stack.
4. [Important] Closing Parentheses:
When encountering a closing parenthesis
, pop the corresponding opening
parenthesis from the stack to ensure
```

5. Generating Output: After processing the entire sequence, the stack should be empty if all parentheses are closed

proper closure.

properly. If not, add the necessary closing brackets to match the remaining opening brackets.

6. Returning the Result: Output the generated closing brackets as a string, separated by spaces, to complete the sequence.

#### E.2 Generated Analysis of Geometric Shapes

#### Explanation:

This task involves analyzing SVG path elements to determine the shape that is being drawn. The path elements consist of a series of commands that define the movements and curves in the SVG image. By understanding these commands and their implications, we can identify the shape being drawn.

#### Analyzing the Task:

1. SVG Path Commands: The SVG path element contains commands like M (move to), L (line to), A (arc), etc., each of which contributes to the overall shape being drawn.

2. Interpreting Path Commands: Each command in the path element corresponds to a specific action, such as moving to a point, drawing a line, or creating an arc. Understanding these commands is crucial to identifying the shape.

3. Recognizing Geometric Shapes: Different combinations of path commands result in different geometric shapes like circles, triangles, rectangles, etc. We need to match the commands to the shapes they represent.

Constructing the Code Prompt: 1. Parsing SVG Path Element: Extract the path commands from the SVG path element provided in the task. This involves splitting the string and identifying each command.

2. Processing Path Commands: Iterate over each command in the path element and execute the corresponding action. This involves:

- Moving to a new point (M command).
- Drawing a line to a point (L command)
- Drawing an arc (A command).Other commands as necessary.

3. [Important] Tracking Coordinates: Keep track of the coordinates as the path commands are executed. This involves updating the current position based on the commands.

4. Determining the Shape: After processing all commands, analyze the resulting path to determine the shape being drawn. This can be done by comparing the final path with the characteristics of known shapes.

5. Matching with Provided Options: Compare the identified shape with the options provided in the task to select the correct answer.

6. Returning the Result: Return the identified shape as the output in the specified format ('(A)', '(B)', '(C)', ...).

By following these steps and accurately interpreting the SVG path commands, we can determine the shape being drawn and select the correct option from the given choices.

#### E.3 Generated Analysis of Navigate

#### Explanation:

This task involves following a series of instructions related to movement and direction to determine if the final position is the same as the starting point. The challenge lies in accurately tracking the movements and rotations to deduce the final position.

Analyzing the Task:

1. Movement Tracking: Keep track of the steps taken in each direction (forward , backward, left, right) to determine the final position.

2. Directional Changes: Account for any rotations (turning left or right) that may alter the orientation during movement.

3. Spatial Reasoning: Apply logical reasoning to calculate the final position based on the cumulative effect of the movements and rotations.

Constructing the Code Prompt: 1. Extracting Instructions: Parse the input text to extract the sequence of movements and rotations.

2. Processing Movements: - Initialize variables to track the current position (x, y coordinates) and orientation (direction faced).

- Iterate over each instruction, updating the position and orientation accordingly.

3. [Important] Determining the Final Position:

 Calculate the final position based on the cumulative effect of movements and rotations.

- Check if the final position matches the starting point to determine if the participant returns to the starting point.

4. Matching with Options: Compare the final position with the starting point to determine if the participant returns to the starting point.

5. Returning the Final Answer: Output ' Yes' if the participant returns to the starting point, 'No' otherwise.

#### E.4 Generated Analysis for Reasoning about Colored Objects

#### Explanation:

This task involves identifying specific attributes of items based on their descriptions and positions relative to each other. The task requires careful reading of the descriptions and analyzing the spatial relationships between the items.

Analyzing the Task: The task involves interpreting the descriptions of items and their spatial relationships to answer specific questions. This task does not require variable tracking but rather a free format reasoning approach to extract the necessary information and make logical deductions.

Constructing the Code Prompt:

1. Parse the descriptions: Extract the descriptions of items and their colors from the input text.

2. Identify the spatial relationships: Determine the positions of items relative to each other based on the descriptions provided.

3. [Free format reasoning] Derive the answer with explanation: Analyze the descriptions and spatial relationships to answer the specific question posed in the task. Use a function like ' derive\_answer\_with\_explanation' to provide both the reasoning and the correct answer.

4. Match the answer with the options: Compare the derived answer with the given options and select the correct one. 5. Return the final answer: Output the final answer in the specified format.

By following these steps, the task can be effectively solved by reasoning through the descriptions and spatial relationships of the items provided in the task instances.

# E.5 Generated Analysis of Temporal Sequences

#### Explanation:

This task involves determining the possible time intervals during which a person could have visited a specific location based on the given schedule of events throughout the day. The goal is to identify the time frames that are not conflicting with other activities.

#### Analyzing the Task:

 Establishing the Timeline: Understanding the sequence of events and the times at which they occurred is crucial for determining the available time slots.

2. Identifying Conflicting Activities: Recognizing the time intervals during which the person was engaged in other activities that would prevent them from visiting the specified location.

3. Determining Possible Visitation Times: By eliminating conflicting time intervals, the remaining time slots represent the possible visitation times .

Constructing the Code Prompt: 1. Extracting Event Information: Parse the given schedule of events to extract the times at which each activity occurred. This may involve creating a data structure to store this information.

 Identifying Conflicting Time Intervals: Determine the time intervals during which the person was occupied with other activities that would prevent them from visiting the specified location.

3. [Important] Calculating Available Time Slots: By subtracting the conflicting time intervals from the total day duration, identify the time frames during which the person could have visited the specified location.

4. Matching with Options: Compare the possible visitation times with the provided options to determine the

correct answer.

5. Returning the Correct Option: Return the letter corresponding to the time interval that matches the calculated possible visitation times.

This task involves a logical deduction process based on the given schedule of events to determine the feasible time intervals for visiting the specified location. By systematically analyzing the timeline and eliminating conflicting activities, the correct answer can be identified. The solution should provide a clear and accurate assessment of the available time slots for the visitation.

### E.6 Generated Analysis of Tracking Shuffled Objectives

Explanation:

This task involves tracking the positions or gifts of individuals as they swap with each other in a sequence of exchanges. The challenge is to keep track of the swaps accurately and determine the final position or gift of a specific individual at the end of the sequence.

Analyzing the Task:
1. Initial Assignments: Understanding
the starting positions or gifts of each
individual is crucial for tracking the
swaps accurately.

 Pairwise Swaps: Identifying the pairs of individuals who swap positions or gifts at each step in the sequence.

 Tracking Changes: Keeping a record of the swaps and updating the positions or gifts of individuals accordingly.

Constructing the Code Prompt: 1. Initialize Positions or Gifts: Set up a dictionary mapping each individual to their initial position or gift.

 Define Swap Pairs: Create a list of tuples representing the pairs of individuals who swap positions or gifts at each step.

3. [Important] Process Swaps: Iterate over the swap pairs, update the positions or gifts of the individuals involved in each swap. Use an if-else statement to handle different swap scenarios.

4. Determine the Final Position or Gift : After processing all swaps, identify the final position or gift of the specified individual.

5. Match and Output the Answer: Parse the options from the input text, find the corresponding option from the given options, and only output the label of the option as the final answer to the question.

#### E.7 Generated Analysis of Web of Lies

#### Explanation:

This task involves determining the truthfulness of a statement made by one individual based on the statements made by others in a chain. The task requires understanding the relationships between truth-tellers and liars and applying logical reasoning to determine the final answer.

#### Analyzing the Task:

1. Establishing Truth Relationships: Each person's statement about another person can be categorized as either true or false. This forms the basis of determining who tells the truth and who lies.

 Propagating Truthfulness: By analyzing the statements in a sequential manner, the truthfulness of each person can be deduced based on the statements made by others.

3. Identifying the Final Question: The task usually asks whether a specific person tells the truth or not based on the chain of statements.

Constructing the Code Prompt: 1. Parsing Statements: Extract the statements made by each person from the input text. This involves identifying who is talking about whom and whether they are telling the truth or lying.

2. Establishing Truth Relationships: Create a dictionary to store the truthfulness of each person based on the statements made by others. This dictionary will be updated as the statements are processed.

3. [Important] Analyzing Statements: Iterate over each statement and update the truthfulness of the individuals involved based on the logic that if A says B lies, then A is telling the truth if B is a liar, and vice versa. This step involves logical reasoning and updating the truth dictionary.

4. Extracting the Final Question: Identify the specific question asked in

```
the input text regarding the truthfulness of a particular person.
```

5. Determining the Answer: Based on the final truthfulness of the person in question as determined by the logic and the statements provided, select 'Yes' if the person tells the truth and 'No' if they do not.

By following these steps and applying logical reasoning to the statements provided, the code can accurately determine whether the specified individual tells the truth or not.

## F Generated Pseudocode Prompts

#### F.1 Generated $\mathcal{P}$ of Dyck Languages

```
def complete_dyck_languages(input_text)
:
   # Step 1: Parse the input text to
extract the sequence of parentheses.
   parentheses_sequence =
extract_parentheses(input_text)
   print("Parentheses sequence:",
parentheses_sequence)
   # Step 2: Initialize a stack to
keep track of opening parentheses that
   stack = []
   # Step 3: Iterate over each
character in the sequence to handle
opening and closing parentheses.
   for i, char in enumerate(
parentheses_sequence):
        if char in ['(', '[', '{', '<'
]:
            stack.append(char)
           print(f"Step ({i}) - Pushed
 {char} to stack")
        elif char in [')', ']', '}', '>
']:
            if len(stack) == 0:
               print(f"Step ({i}) - No
matching opening bracket for {char}")
            else:
               opening_bracket = stack
.pop()
               print(f"Step ({i}) -
Matched {opening_bracket} with {char}")
   # Step 4: Check if the stack is
empty after processing the entire
sequence.
    if len(stack) > 0:
       print("Remaining unmatched
brackets in stack:", stack)
       # Step 5: Generate the
necessary closing brackets to match the
remaining opening brackets.
       closing_brackets =
generate_closing_brackets(stack)
```

```
print("Generated closing
brackets:", closing_brackets)
else:
    print("All brackets are
properly matched.")
```

```
# Step 6: Return the generated
closing brackets as the final answer.
return closing_brackets
```

### **F.2** Generated $\mathcal{P}$ of Geometric Shapes

```
def recognize_shape_from_svg(
svg_path_element):
   # Step 1: Parse the SVG path
element to extract the path commands.
Output the extracted path commands.
   path_commands =
extract_path_commands(svg_path_element)
   print("Extracted path commands:",
path_commands)
   # Step 2: Process each path command
to execute the corresponding action.
Keep track of the coordinates as the
commands are executed.
   current_position = (0, 0)
   for command in path_commands:
       action, coordinates =
process path command(command,
current_position)
       print(f"Executing command: {
command} - Action: {action} - New
coordinates: {coordinates}")
       current_position = coordinates
   # Step 3: Determine the shape based
on the processed path commands. This
involves analyzing the final path drawn
   identified_shape = identify_shape(
path_commands)
   print("Identified shape:",
identified_shape)
   # Step 4: Match the identified
shape with the provided options to
select the correct answer.
   options = extract_options(
svq_path_element)
   answer = match_shape_with_options(
identified_shape, options)
   # Step 5: Return the identified
shape as the final answer.
  return answer
```

## **F.3** Generated $\mathcal{P}$ of Navigate

```
def ends_up_at_start(input_text):
    # Step 1: Extract the sequence of
movements and rotations from the input
text.
```

```
instructions = extract_instructions
(input text)
   print("Instructions:", instructions
   # Step 2: Initialize variables to
track the current position and
orientation.
   x, y = 0, 0
   orientation = "N"
   print(f"Initial position: ({x}, {y
}), Orientation: {orientation}")
    # Step 3: Process each instruction
to update the position and orientation
accordingly.
   for instruction in instructions:
       x, y, orientation =
process_instruction(instruction, x, y,
orientation)
       print(f"Instruction: {
instruction} -> Position: ({x}, {y}),
Orientation: {orientation}")
    # Step 4: Determine the final
position after following all
instructions.
    final_position = (x, y)
   print("Final Position:",
final_position)
    # Step 5: Check if the final
position matches the starting point to
determine if the participant returns to
the starting point.
    if final_position == (0, 0):
        return 'Yes'
    else:
       return 'No'
```

# F.4 Generated $\mathcal{P}$ for Reasoning about Colored Objects

```
def solve_colored_objects(input_text):
   # Step 1: Extract the descriptions
of items and their colors from the
input text.
   items = parse_items(input_text)
   print("Items on the surface:\n",
items)
    # Step 2: Determine the positions
of items relative to each other based
on the descriptions provided.
   spatial_relationships =
analyze_spatial_relationships(items)
   print("Spatial relationships
between items:\n",
spatial_relationships)
   # Step 3: Derive the answer with
explanation by analyzing the
descriptions and spatial relationships.
```

question = identify\_question(

input\_text)

```
print("The question is:", question)
   reason, answer =
derive_answer_with_explanation(items,
spatial_relationships, question)
   print("Reasoning for the answer:",
reason)
    # Step 4: Compare the derived
answer with the given options and
select the correct one.
   options = extract_options(
input_text)
   print("Answer options:\n", options)
    final_answer = None
    for option in options:
       if answer in option:
            final_answer = option[:3]
            break
    # Step 5: Return the final answer.
    return final_answer
```

### **F.5** Generated $\mathcal{P}$ of Temporal Sequences

```
def solve_temporal_sequences_quiz(
input_text):
   # Step 1: Extract event information
from the input text to understand the
timeline of activities throughout the
day.
   events list = extract events(
input_text)
   print ("Events and their timings:",
events list)
   # Step 2: Identify conflicting time
intervals when the person was engaged
in other activities that would prevent
them from visiting the specified
location.
   conflicting_intervals =
find_conflicting_intervals(events_list)
   print("Conflicting time intervals:"
 conflicting_intervals)
   # Step 3: Calculate the available
time slots by subtracting conflicting
intervals from the total day duration.
   available_intervals =
calculate_available_intervals(
conflicting_intervals)
   print("Available time intervals for
visitation:", available_intervals)
   # Step 4: Match the available time
slots with the provided options to
determine the correct answer.
   options = input_text.split("\n")
[-5:]
   # Step 5: Return the correct option
corresponding to the time interval
that aligns with the calculated
possible visitation times.
   answer = find_correct_option(
```

available\_intervals, options)

return answer

# F.6 Generated $\mathcal{P}$ of Tracking Shuffled Objectives

```
def track_swaps(input_text):
    # Step 1: Initialize Positions or
   initial assignments =
extract_initial_assignments(input_text)
   print("Initial assignments:",
initial_assignments)
    # Step 2: Define Swap Pairs
    swap_pairs = extract_swap_pairs(
input_text)
    print("Swap pairs:", swap_pairs)
    # Step 3: Process Swaps
    final_assignments =
initial_assignments.copy()
    for pair in swap_pairs:
        if pair[0] in final_assignments
and pair[1] in final_assignments:
            temp = final_assignments[
pair[0]]
            final_assignments[pair[0]]
= final_assignments[pair[1]]
            final_assignments[pair[1]]
= temp
        print(f"After swapping {pair
[0] } and {pair[1] }: {final_assignments}
")
    # Step 4: Determine the Final
Position or Gift
   final_person =
identify_final_person(input_text)
   final_position = final_assignments[
final person]
   print(f"The final position or gift
of {final_person} is: {final_position}"
    # Step 5: Match and Output the
Answer
   options = extract_options(
input_text)
   print("Options:", options)
    answer = None
    for option in options:
        if final_position in option:
            answer = option[:3]
    return answer
```

## **F.7** Generated $\mathcal{P}$ of Web of Lies

```
statements, question = input_text.
split("?")
   statements = statements.split(". ")
   print("Statements:", statements)
   print("Question:", question)
    # Step 2: Initialize a truth
dictionary to keep track of who tells
the truth and who lies.
    truth_dict = {}
    # Step 3: Process each statement to
update the truth dictionary based on
the logic provided.
   for statement in statements:
       person1, action, person2 =
statement.split(" ")
       if action == "lies":
            truth_dict[person1] = not
truth_dict[person2]
       else:
           truth_dict[person1] =
truth_dict[person2]
       print(f"{person1} says {person2
} {action}. {person1} tells the truth:
{truth_dict[person1]}")
    # Step 4: Determine the
truthfulness of the person in question
based on the truth dictionary.
   person_to_check = question.split("
") [-2]
   answer = 'Yes' if truth_dict[
person_to_check] else 'No'
   return answer
```

## G Qualitative Analysis

We conduct a qualitative analysis by comparing the outputs of our approach (THINK-AND-EXECUTE) with those of the baseline methods. This comparison is presented across Tables10,11,12,13,14,15, and 16.

Example Instance	Complete the rest of the sequence, making sure that the parentheses are closed properly. Input: ( { { } } }
Ground truth Answer	)
Method	Output
Direct Prompting	Final answer: { } ) (Wrong)
Zero-shot Prompting	Step 1: ( { { } } ) Step 2: ( { { } } ) Therefore, the answer is } ( <b>Wrong</b> )
РоТ	<pre>def solution():     stack = []     sequence = "( { { } } "</pre>
	<pre>for char in sequence: if char == "(" or char == "{": stack.append(char) elif char == ")" and stack[-1] == "(": stack.pop() elif char == "}" and stack[-1] == "{": stack.pop()</pre>
	<pre>for char in stack: if char == "(": sequence += ")" elif char == "{": sequence += "}"</pre>
	return sequence solution() >> ( { { } } ) (Wrong)
NL Planning	<pre>Step 1: Opening brackets in the input sequence: ( { {    Step 2: Corresponding closing brackets:    ( -&gt; )    { -&gt; }    { -&gt; }    Step 3: Closing brackets in order: ) } }</pre>
	Final answer: ) } } (Wrong)
Ours	Bracket sequence: ['(', '{', '}', '}'] Step 0 - bracket: ( Updated stack: ['('] Step 1 - bracket: { Updated stack: ['(', '{'] Step 2 - bracket: { Updated stack: ['(', '{'] Step 3 - bracket: } Updated stack: ['(', '{'] Step 4 - bracket: } Updated stack: ['('] Rest of sequence: ) Stack is not empty. The sequence is not properly balanced.

Table 10: A comparison of results for Dyck Languages between the baseline methods and THINK-AND-EXECUTE.

Example Instance	This SVG path element <pre>path d="M 38.00,62.00 L 48.00,60.00 L 51.00,49.00 L 54.00,60.00 L 65.00,62.00 L 54.00,64.00 L 51.00,74.00 L 48.00,64.00 L 38.00,62.00"/&gt; draws a Options: (A) circle (B) heptagon (C) hexagon (D) kite (E) line (F) octagon (G) pentagon (H) rectangle (I) sector (J) triangle</pre>
Ground truth Answer	(F) octagon
Method	Output
Direct Prompting	Final answer: (C) hexagon (Wrong)
Zero-shot Prompting	The given SVG path forms a shape with 8 sides, which is a hexagon. Therefore, the answer is (C) hexagon. ( <b>Wrong</b> )
РоТ	def solution(): return "C) hexagon"
	solution() »> C) hexagon (Wrong)
NL Planning	Step 1: Identify the SVG Path Element. The given SVG path element is <pre><pre>cpath d="M 38.00,62.00 L 48.00,60.00 L 51.00,49.00 L 54.00,60.00 L 65.00, 62.00 L 54.00,64.00 L 51.00,74.00 L 48.00,64.00 L 38.00,62.00"/&gt;</pre></pre>
	Step 2: Analyze the Path Data. The path data commands used are 'M' for move to and 'L' for line to. The sequence of points mentioned are (38.00,62.00), (48.00,60.00), (51.00,49.00), (54.00,60.00), (65.00,62.00), (54.00,64.00), (51.00,74.00), (48.00,64.00), (38.00,62.00).
	<ul><li>Step 3: Determine the Shape. Based on the sequence of points and movements, the shape drawn appears to be a kite.</li><li>Step 4: Match with Options. The shape drawn matches with option (D) kite.</li></ul>
	Step 5: Output the Correct Option. Final answer: (D) kite ( <b>Wrong</b> )
Ours	Extracted path commands: ['M 38.00,62.00', 'L 48.00,60.00', 'L 51.00,49.00', 'L 54.00,60.00', 'L 65.00,62.00', 'L 54.00,64.00', 'L 51.00,74.00', 'L 48.00,64.00', 'L 38.00,62.00'] Executing command: M 38.00,62.00 - Action: Move to (38.00, 62.00)
	- New coordinates: (38.00, 62.00) Executing command: L 48.00,60.00 - Action: Draw line to (48.00, 60.00) - New coordinates: (48.00, 60.00)
	Executing command: L 51.00,49.00 - Action: Draw line to (51.00, 49.00) - New coordinates: (51.00, 49.00) Executing command: L 54.00,60.00 - Action: Draw line to (54.00, 60.00)
	- New coordinates: (54.00, 60.00) Executing command: L 65.00,62.00 - Action: Draw line to (65.00, 62.00)
	- New coordinates: (65.00, 62.00) Executing command: L 54.00,64.00 - Action: Draw line to (54.00, 64.00) - New coordinates: (54.00, 64.00)
	Executing command: L 51.00,74.00 - Action: Draw line to (51.00, 74.00) - New coordinates: (51.00, 74.00) Executing command: L 48.00,64.00 - Action: Draw line to (48.00, 64.00)
	<ul> <li>New coordinates: (48.00, 64.00)</li> <li>Executing command: L 38.00,62.00 - Action: Draw line to (38.00, 62.00)</li> <li>New coordinates: (38.00, 62.00)</li> <li>Identified shape: octagon</li> <li>Final answer: (F) octagon (Correct)</li> </ul>

Table 11: A comparison of results for Geometric Shapes between the baseline methods and THINK-AND-EXECUTE.

Example Instance	If you follow these instructions, do you return to the starting point? Take 3 steps. Turn around. Take 5 steps. Turn right. Take 1 step. Take 1 step.
Ground truth Answer	Yes
Method	Output
Direct Prompting	Final answer: no (Wrong)
Zero-shot Prompting	First, take 3 steps. Then, turn around and take 5 steps in the opposite direction. After that, turn right twice and take 1 step followed by another step. Therefore, the answer is no. ( <b>Wrong</b> )
PoT	def solution(): x = 0 y = 0 direction = 0 # 0: North, 1: East, 2: South, 3: West # Take 3 steps for _ in range(3): if direction == 0: y += 1 elif direction == 1: x += 1 elif direction == 2: y -= 1 else: x -= 1 # Turn around direction = (direction + 2) % 4 # Take 5 steps  return $x == 0$ and $y == 0$ solution() >> True (Wrong)
NL Planning	Final answer: No (Wrong)
Ours	Instructions: ['Take 3 steps', 'Turn around', 'Take 5 steps', 'Turn right', 'Turn right', 'Take 1 step', 'Take 1 step'] Initial position: (0, 0), Orientation: N Instruction: Take 3 steps -> Position: (0, 3), Orientation: N Instruction: Turn around -> Position: (0, 3), Orientation: S Instruction: Take 5 steps -> Position: (0, -2), Orientation: S Instruction: Turn right -> Position: (0, -2), Orientation: N Instruction: Turn right -> Position: (0, -2), Orientation: N Instruction: Take 1 step -> Position: (0, -1), Orientation: N Instruction: Take 1 step -> Position: (0, 0), Orientation: N Final Position: (0, 0) Final answer: Yes ( <b>Correct</b> )

Table 12: A comparison of results for Navigate between the baseline methods and THINK-AND-EXECUTE.

Example Instance	On the floor, there is one mauve cat toy, two purple cat toys, three grey cat toys, two mauve notebooks, three grey notebooks, three burgundy cat toys, and one purple notebook. If I remove all the notebooks from the floor, how many grey objects remain on it? Options: (A) zero (B) one (C) two (D) three (E) four (F) five (G) six (H) seven (I) eight (J) nine (K) ten (L) eleven (M) twelve (N) thirteen (O) fourteen (P) fifteen (Q) sixteen
Ground truth Answer	(D) three
Method	Output
Direct Prompting	Final answer: (C) two (Wrong)
Zero-shot Prompting	First, let's count the number of grey objects on the floor before removing the notebooks: - Three grey cat toys - Three grey notebooks Total grey objects before removing notebooks: 3 (grey cat toys) + 3 (grey notebooks) = 6 grey objects Now, let's remove the notebooks from the floor: - Two mauve notebooks - Three grey notebooks - One purple notebook Total notebooks removed: 2 (mauve notebooks) + 3 (grey notebooks) + 1 (purple notebooks) - 6 notebooks Now, let's calculat how many grey objects remain on the floor after removing the notebooks: Total grey objects before removing notebooks: 6 grey objects Total notebooks 6 notebooks Grey objects remaining on the floor: 6 (total grey objects) - 6 (notebooks removed) = 0 grey objects Therefore, the answer is (A) zero (Wrong)
PoT	def solution(): # Total number of grey objects on the floor total_grey_objects = 3 + 3
	# Removing notebooks from the floor removed_notebooks = 2 + 3
	<pre># Number of grey objects remaining on the floor remaining_grey_objects = total_grey_objects - removed_notebooks</pre>
	return remaining_grey_objects
	solution() »> 1 (Wrong)
NL Planning	Step 1: - Mauve cat toy - Purple cat toys - Grey cat toys - Mauve notebooks - Grey notebooks - Burgundy cat toys - Purple notebook Step 2: - The question ask about the number of grey objects remaining on the floor after removing all the notebooks. Step 3: - There are three grey cat toys and three grey notebooks on the floor. Step 4: - After removing all the notebooks, there are three grey cat toys remaining. Step 5: - The answer to the question is (C) two. Final answer: (C) two (Wrong)
Ours	Items on the surface: 'mauve cat toy': 1, 'purple cat toy': 2, 'grey cat toy': 3, 'mauve notebook': 2, 'grey notebook': 3, 'burgundy cat toy': 3, 'purple notebook' 1 Spatial relationships between items: 'mauve cat toy': ['floor'], 'purple cat toy': ['floor'], 'grey cat toy': ['floor'], 'mauve notebook': ['floor'], 'grey notebook' ('floor'], 'purple notebook': ['floor'], 'purple notebook': ['floor'], 'purple notebook': ['floor'], 'purple notebook': ['floor'], 'grey cat toy': ['floor'], 'mauve notebook': ['floor'], 'grey notebook': ['floor'], 'purple notebook': ['floor'],

Table 13: A comparison of results for Reasoning about Colored Objects Shapes between the baseline methods and ours.

Example Instance	Today, Jason went to the movies. Between what times could they have gone? We know that: Jason woke up at 10am. Linda saw Jason getting a coffee at the cafe from 10am to 3pm. Jennifer saw Jason walking towards the Statue of Liberty from 6pm to 7pm. Sean saw Jason buying a phone at the electronics store from 7pn to 10pm. The movies was closed after 10pm. Between what times could Jason have gone to the movies? Options: (A) 3pm to 6pm (B) 10am to 3pm (C) 7pm to 10pm (D) 6pm to 7pm.
Ground truth Answer	(A) 3pm to 6pm
Method	Output
Direct Prompting	Final answer: (C) 7pm to 10pm (Wrong)
Zero-shot Prompting	Jason could have gone to the movies between 7pm to 10pm, as the movies were closed after 10pm. Therefore, the answer is (C) 7pm to 10pm ( <b>Wrong</b> )
PoT	def solution(): possible_times = []
	<pre># Jason could have gone to the movies between 3pm to 6pm if 3 &lt;= 6: possible_times.append("3pm to 6pm")</pre>
	# Jason could have gone to the movies between 10am to 3pm if 10 <= 3:
	possible_times.append("10am to 3pm") # Jason could have gone to the movies between 7pm to 10pm
	if 7 <= 10: possible_times.append("7pm to 10pm")
	# Jason could have gone to the movies between 6pm to 7pm if 6 <= 7: possible_times.append("6pm to 7pm")
	return possible_times
	solution() »> ['3pm to 6pm', '7pm to 10pm', '6pm to 7pm'] (Wrong)
NL Planning	Step 1:         - Jason woke up at 10am.         - Linda saw Jason at the cafe from 10am to 3pm.         - Jennifer saw Jason walking towards the Statue of Liberty from 6pm to 7pm.         - Sean saw Jason at the electronics store from 7pm to 10pm.         - The movies was closed after 10pm.         Step 2:         - The specific question is about the time range for Jason to have gone to the movies.         Step 3:         - Timeline:         - 10am: Jason walking towards the Statue of Liberty         - 7pm to 17pm: Jason at the cafe         - 6pm to 7pm: Jason at the electronics store         - After 10pm: Movies closed         Step 4:         - Events placed on the timeline accordingly.         Step 5:         - Possible time range for Jason to the movies is after 10pm.         Step 5:         - Comparison results:         - Option (A) 3pm to 6pm: Not possible         - Option (B) 10am to 3pm: Not possible         - Option (D) 6pm to 7pm: Not possible         - Option (D) 7pm to 10pm: Possible         - Option (D) 7pm to 10pm: Possible         - Option (D) 6pm to 7pm: Not possible         - Option (D) 6p
Ours	Events and their timings: [('Jason woke up', '10am'), ('Linda saw Jason getting a coffee at the cafe', '10am to 3pm'), ('Jennifer saw Jason walking towards the Statue of Liberty', '6pm to 7pm'), ('Sean saw Jason buying a phone at the electronics store', '7pm to 10pm')] Conflicting time intervals: [('10am', '3pm'), ('6pm', '7pm'), ('7pm', '10pm')] Available time intervals for visitation: [('3pm', '6pm')] Final answer: (A) 3pm to 6pm (Correct)

Table 14: A comparison of results for Temporal Sequences between the baseline methods and THINK-AND-EXECUTE.

Example Instance	Alice, Bob, Claire, Dave, and Eve are playing a game. At the start of the game, they are each holding a ball: Alice has a orange ball, Bob has a black ball, Clair has a pink ball, Dave has a white ball, and Eve has a red ball. As the game progresses, pairs of players trade balls. First, Alice and Dave swap balls. Then, Bol and Claire swap balls. Then, Claire and Dave swap balls. Then, Dave and Bob swap balls. Finally, Alice and Eve swap balls. At the end of the game, Claire ha the Options: (A) orange ball (B) black ball (C) pink ball (D) white ball (E) red ball
Ground truth Answer	(A) orange ball
Method	Output
Direct Prompting	Final answer: (D) white ball (Wrong)
Zero-shot Prompting	1. After Alice and Dave swap balls: Alice has a white ball, Bob has a black ball, Claire has a pink ball, Dave has an orange ball, Eve has a red ball.
	<ol> <li>After Bob and Claire swap balls:</li> <li></li> <li>After Alice and Eve swap balls:</li> <li>Alice has a red ball,</li> <li>Bob has an orange ball,</li> <li>Claire has a black ball,</li> <li>Dave has a pink ball,</li> <li>Eve has a white ball.</li> <li>Therefore, the answer is (B) black ball (Wrong)</li> </ol>
PoT	def solution(): balls = {"Alice": "orange", "Bob": "black", "Claire": "pink",
	<pre>"Dave": "white", "Eve": "red"} # Define the swaps swaps = [("Alice", "Dave"), ("Bob", "Claire"), ("Claire", "Dave"), ("Dave", "Bob"), ("Alice", "Eve")]</pre>
	<pre># Perform the swaps for swap in swaps:     temp = balls[swap[0]]     balls[swap[0]] = balls[swap[1]]     balls[swap[1]] = temp</pre>
	<pre># Return the ball color Claire has at the end return [key for key, value in balls.items() if value == "pink"][0]</pre>
	solution() »> Dave (Wrong)
NL Planning	Step 1: Alice - orange ball Bob - black ball Claire - pink ball Dave - white ball Eve - red ball Step 2: 1. Alice and Dave swap balls 2. Bob and Claire swap balls 2. Bob and Claire swap balls
	3. Claire and Dave swap balls         4. Dave and Bob swap balls         5. Alice and Eve swap balls         Step 3:         Alice - white ball         Bob - pink ball         Claire - black ball         Dave - black ball         Eve - orange ball
	Step 4: Final book assignment for Claire: black ball Step 5: Options: Step 6: Final answer: (B) black ball ( <b>Wrong</b> )
Ours	Initial assignments: 'Alice': 'orange ball', 'Bob': 'black ball', 'Claire': 'pink ball', 'Dave': 'white ball', 'Eve': 'red ball' Swap pairs: (('Alice', 'Dave'), ('Bob', 'Claire'), ('Claire', 'Dave'), ('Dave', 'Bob'), ('Alice', 'Eve')] After swapping Alice and Dave: 'Alice': 'white ball', 'Bob': 'black ball', 'Claire': 'pink ball', 'Dave': 'orange ball', 'Eve': 'red ball'  After swapping Alice and Eve: 'Alice': 'red ball', 'Bob': 'black ball', 'Claire': 'orange ball', 'Dave': 'pink ball', 'Eve': 'red ball' The final position or gift of Claire is: orange ball Options: [('(A) orange ball', '(B) black ball', '(C) pink ball', '(D) white ball', '(E) red ball'] Final answer:(A) (Correct)

Table 15: A comparison of results for Tracking Shuffled Objectives between the baseline methods and THINK-AND-EXECUTE.

Example Instance	Vina tells the truth. Helene says Vina lies. Kandi says Helene tells the truth. Jamey says Kandi lies. Ka says Jamey lies. Does Ka tell the truth?
Ground truth Answer	No
Method	Output
Direct Prompting	Final answer: Yes (Wrong)
Zero-shot Prompting	First, let's analyze the statements:         1. Vina tells the truth.         2. Helene says Vina lies.         3. Kandi says Helene tells the truth.         4. Jamey says Kandi lies.         5. Ka says Jamey lies.         From statement 2, we can infer that Helene lies, which means Vina actually tells the truth.         From statement 3, we can infer that Kandi tells the truth.         From statement 4, we can infer that Jamey lies.         From statement 5, we can infer that Jamey lies.         From statement 5, we can infer that Kandi tells the truth.         Therefore, Ka tells the truth.         Therefore, Ka tells the truth.
PoT	def solution(): vina = True helene = not vina kandi = vina jamey = not kandi ka = not jamey return ka solution() »> True (Wrong)
NL Planning	Step 1:         - Vina tells the truth.         - Helene says Vina lies.         - Kandi says Helene tells the truth.         - Jamey ays Kandi lies.         - Kandi says I-alment tells the truth.         - Maney says Kandi lies.         - Kandi says I-alment tells the truth.         - Maney says Kandi lies.         - Ka says Jamey lies.         Step 2:         Person       Trute-telling status         Helene       False         Kandi True       Jamey False         Ka a       False         Step 3:
Ours	Statements: ['Vina tells the truth', 'Helene says Vina lies', 'Kandi says Helene tells the truth', 'Jamey says Kandi lies', 'Ka says Jamey lies'] Question: Does Ka tell the truth Vina says the truth. Vina tells the truth: True Helene says Vina lies. Helene tells the truth: False Kandi says Helene tells the truth. Kandi tells the truth: False Jamey says Kandi lies. Jamey tells the truth: True Ka says Jamey lies. Ka tells the truth: False Final answer: No (Correct)

Table 16: A comparison of results for Web of lies between the baseline methods and THINK-AND-EXECUTE.