How to Leverage Demonstration Data in Alignment for Large Language Model? A Self-Imitation Learning Perspective

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Abstract

This paper introduces a novel generalized selfimitation learning (GSIL) framework, which effectively and efficiently aligns large language models with offline demonstration data. We develop GSIL by deriving a surrogate objective of imitation learning with density ratio estimates, facilitating the use of self-generated data and optimizing the imitation learning objective with simple classification losses. GSIL eliminates the need for complex adversarial training in standard imitation learning, achieving lightweight and efficient fine-tuning for large language models. In addition, GSIL encompasses a family of offline losses parameterized by a general class of convex functions for density ratio estimation and enables a unified view for alignment with demonstration data. Extensive experiments show that GSIL consistently and significantly outperforms baselines in many challenging benchmarks, such as coding (HuamnEval), mathematical reasoning (GSM8K) and instruction-following benchmark (MT-Bench). Code is public available at <https://github.com/tengxiao1/GSIL>.

1 Introduction

Pre-training endows large language models (LLMs) with extensive knowledge about the world. However, it does not behave in accordance with some task-dependent requirements. To achieve the desired performance on certain tasks, a post-training process known as alignment or fine-tuning is essential. Alignment has emerged as a pivotal approach to improve the following performance of pre-trained language models, especially in complex instruction-following tasks: commonsense reasoning, coding, summarization, and math problemsolving [\(Bai et al.,](#page-8-0) [2022;](#page-8-0) [Ouyang et al.,](#page-9-0) [2022;](#page-9-0) [Sti](#page-9-1)[ennon et al.,](#page-9-1) [2020;](#page-9-1) [Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2).

The current alignment methods can be broadly categorized into groups: (i) *supervised fine-tuning* (SFT) based on demonstration data, aligning an input prompt and a human response. (ii) *Preference fine-tuning* [\(Tajwar et al.,](#page-10-0) [2024\)](#page-10-0) with reinforcement learning from human feedback (RLHF) [\(Ouyang et al.,](#page-9-0) [2022;](#page-9-0) [Christiano et al.,](#page-8-1) [2017\)](#page-8-1) or direct preference optimization (DPO) [\(Rafailov et al.,](#page-9-2) [2024b;](#page-9-2) [Zhao et al.,](#page-10-1) [2023;](#page-10-1) [Azar et al.,](#page-8-2) [2024;](#page-8-2) [Tang](#page-10-2) [et al.,](#page-10-2) [2024;](#page-10-2) [Ethayarajh et al.,](#page-8-3) [2024\)](#page-8-3) based on preference data containing preferred and dis-preferred responses to prompts. Although RLHF and DPO have achieved promising results [\(Rafailov et al.,](#page-9-2) [2024b;](#page-9-2) [Tunstall et al.,](#page-10-3) [2023\)](#page-10-3), they require expensive human preference labels on several candidate demonstrations of a query to be used as feedback, limiting their applicability to language model alignment in settings where there is a lack of preference feedback. Furthermore, preference fine-tuning may suffer from reward overoptimization (also known as reward hacking), as shown by [\(Rafailov et al.,](#page-9-3) [2024a;](#page-9-3) [Gao et al.,](#page-9-4) [2023a\)](#page-9-4). Recent work [\(Sharma](#page-9-5) [et al.,](#page-9-5) [2024\)](#page-9-5) also shows that simply performing SFT on demonstrations can result in a better model than preference fine-tuning with AI feedback.

Therefore, while preference fine-tuning has garnered more increasing attention in the literature for LLM alignment [\(Rafailov et al.,](#page-9-2) [2024b;](#page-9-2) [Zhao](#page-10-1) [et al.,](#page-10-1) [2023;](#page-10-1) [Azar et al.,](#page-8-2) [2024;](#page-8-2) [Tang et al.,](#page-10-2) [2024;](#page-10-2) [Ethayarajh et al.,](#page-8-3) [2024;](#page-8-3) [Liu et al.,](#page-9-6) [2023;](#page-9-6) [Hong et al.,](#page-9-7) [2024;](#page-9-7) [Xiao et al.,](#page-10-4) [2024a\)](#page-10-4), this work poses the following critical questions that remain unanswered. *What is the best use of human demonstration data? Is SFT the most effective method for leveraging this data, or are there other approaches that could yield better results in specific contexts?*

To answer this question, we investigate the expressive power of imitation learning (IL). We begin by presenting GSIL, a simple, effective, and general framework for alignment with human demonstration data. Instead of using demonstration data directly via SFT (the simplest approach to imitation learning, which corresponds to behavior cloning), we propose a generalized self-imitation learning framework to learn a better policy. Imitation learning treats the task of learning a policy from a set of expert demonstrations, proving particularly promising in domains such as robot control, autonomous driving, where manually specifying reward functions is challenging but historical human demonstrations are readily accessible [\(Ho and Ermon,](#page-9-8) [2016;](#page-9-8) [Hussein et al.,](#page-9-9) [2017;](#page-9-9) [Osa et al.,](#page-9-10) [2018\)](#page-9-10).

While the motivation is straightforward, we are faced with important challenges in applying imitation learning for alignment of large language models. State-of-the-art imitation learning frameworks in the literature of reinforcement learning (RL) are considerably more complex and computationally intensive than SFT, involving inefficient and unstable adversarial or iterative training on separate discriminator and policy networks [\(Finn et al.,](#page-9-11) [2016;](#page-9-11) [Ho and Ermon,](#page-9-8) [2016;](#page-9-8) [Kostrikov et al.,](#page-9-12) [2019\)](#page-9-12). This challenge largely prevents us from aligning large language models in real-world applications.

Contributions. We propose a principled imitation learning framework, namely GSIL, which not only can learn an effective policy from human demonstration data, but also achieves simple and fast fine-tuning as SFT. Specifically, we first deduce an equivalent surrogate objective for standard imitation learning, allowing for the utilization of demonstration data. Then, we make use of the connection between imitation learning and density ratio estimation that can be solved with simple classification in an entirely offline fashion. Importantly, this connection enables us to represent the policy and discriminator via the same language model, achieving simple fine-tuning without adversarial training. Intuitively, GSIL tries to increase the relative log probability of demonstrations to self-generated synthetic responses. GSIL is a generalized framework, and we show that essentially any density ratio estimation loss (e.g., logistic, hinge, brier) can be used in GSIL as shown in Section [3.4.](#page-4-0)

Experiments. We conduct extensive experiments to thoroughly evaluate GSIL on many benchmarks: instruction-following (MT-Bench), reasoning (LLM Leaderboard), coding (HumanEval), and safety (Anthropic-HH). GSIL achieves consistent and significant improvements over existing alignment methods with only demonstration data such as SFT and SPIN by a large margin. Moreover, we observe that GSIL can even outperform preference fine-tuning methods such as DPO, which require preference labels, in challenging benchmarks, including those for math, reasoning, and coding. As a generalized framework, GSIL can be implemented with any density ratio estimation loss. We discuss the benefits and performance of various choices and show that different GSIL variants also exhibit distinct learning behaviors and improve performance.

2 Background

Let the text sequence $x = [x_1, x_2, \ldots]$ denote the input prompt, and $y = [y_1, y_2, \ldots]$ denote the response. We use notation $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ to denote the policy parameterized by parameters θ , which outputs the response y given the input x. We assume that we have access to demonstrations $\mathcal{D} = \{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^{|\mathcal{D}|}$, where $(\mathbf{x}_i, \mathbf{y}_i)$ is collected from an unknown policy π_{data} . Given demonstrations D , the goal is to fine-tune the language model policy $\pi_{\theta}(\mathbf{y} \mid \mathbf{x})$ to achieve effective alignment.

SFT. Given a demonstration dataset, the objective of SFT is minimizing the negative log-likelihood over the demonstration data as follows:

$$
\min_{\boldsymbol{\theta}} \ell_{\text{SFT}}(\boldsymbol{\theta}) = -\mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{D}}[\log \pi_{\boldsymbol{\theta}}(\mathbf{y} \mid \mathbf{x})]. \quad (1)
$$

It is worth noting that SFT is equal to behavior cloning (BC) [\(Pomerleau,](#page-9-13) [1988\)](#page-9-13) which is a classical and commonly used imitation learning method. BC is typically cast as KL divergence minimization between the learning policy and expert policy as:

$$
\min_{\boldsymbol{\theta}} \mathrm{KL}\left(\pi_{\mathrm{data}}(\mathbf{y} \mid \mathbf{x}) \|\pi_{\boldsymbol{\theta}}(\mathbf{y} \mid \mathbf{x})\right),\qquad(2)
$$

for each prompt x sampled from dataset D . It is easy to see that the BC problem above shares the same optimal solutions as SFT in expectation.

RLHF. Typically, given the reward function $r(\mathbf{x}, \mathbf{y})$, which indicates the human preferences, RLHF optimizes policy π_{θ} for x to maximize reward with the following RL objective:

$$
\max_{\theta} \mathbb{E}_{\pi_{\theta}(\mathbf{y}|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \beta \text{KL} \big(\pi_{\theta}(\mathbf{y}|\mathbf{x}) || \pi_{\text{ref}}(\mathbf{y}|\mathbf{x}) \big), \tag{3}
$$

where $\beta > 0$ is an appropriate KL penalty coefficient. Due to the discrete nature of language generation, we typically optimize the RLHF objective in Equation [\(3\)](#page-1-0) using RL algorithms, such as PPO [\(Ouyang et al.,](#page-9-0) [2022;](#page-9-0) [Schulman et al.,](#page-9-14) [2017\)](#page-9-14). Although RLHF with PPO has achieved remarkable success, the training process of PPO is unstable because of the high variance of the estimates of the policy gradients [\(Engstrom et al.,](#page-8-4) [2020\)](#page-8-4).

DPO. DPO assumes an additional offline preference dataset $P = \{(\mathbf{x}, \mathbf{y}_w, \mathbf{y}_l)\}_{i=1}^{|P|}$, where \mathbf{y}_w and

 y_l denote preferred and dispreferred responses, obtained typically by sampling from π_{ref} , respectively. The response pairs are typically presented to humans (or an oracle) who express preferences for responses given the prompt, denoted as $y_w \succ y_l | \mathbf{x}$. To optimize π_{θ} directly using the preference data, DPO [\(Tang et al.,](#page-10-2) [2024;](#page-10-2) [Rafailov et al.,](#page-9-2) [2024b;](#page-9-2) [Azar](#page-8-2) [et al.,](#page-8-2) [2024\)](#page-8-2) uses the log-likelihood of the policy to implicitly denote the preference (reward) function:

$$
r_{\boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}) = \beta \big(\log \pi_{\boldsymbol{\theta}}(\mathbf{y} \mid \mathbf{x}) - \log \pi_{\text{ref}}(\mathbf{y} \mid \mathbf{x}) \big). \qquad (4)
$$

With preference expressed in terms of policy, DPO optimizes π_{θ} based on the Bradley-Terry (BT) preference model [\(Bradley and Terry,](#page-8-5) [1952\)](#page-8-5):

$$
\min_{\boldsymbol{\theta}} \ell_{\text{DPO}}(\boldsymbol{\theta}) = -\log \sigma (r_{\boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}_{w}) - r_{\boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}_{l})). \quad (5)
$$

DPO and many of its extensions [\(Liu et al.,](#page-9-6) [2023;](#page-9-6) [Zhao et al.,](#page-10-1) [2023;](#page-10-1) [Tajwar et al.,](#page-10-0) [2024;](#page-10-0) [Azar et al.,](#page-8-2) [2024;](#page-8-2) [Tang et al.,](#page-10-2) [2024\)](#page-10-2) follow a similar intuition: increasing the margin between the likelihood of preferred responses and the likelihood of dispreferred responses. However, as noted earlier, these preference fine-tuning objectives require expensive human preference labels on candidate demonstrations of a query to be used as feedback and may suffer from reward overoptimization, as shown by [\(Rafailov et al.,](#page-9-3) [2024a;](#page-9-3) [Gao et al.,](#page-9-4) [2023a\)](#page-9-4). Recent work [\(Sharma et al.,](#page-9-5) [2024\)](#page-9-5) also shows that simply performing SFT on demonstrations can result in a better model than preference fine-tuning with AI feedback. Contrastive fine-tuning with preference has recently attracted increasing attention [\(Liu](#page-9-6) [et al.,](#page-9-6) [2023;](#page-9-6) [Zhao et al.,](#page-10-1) [2023;](#page-10-1) [Tajwar et al.,](#page-10-0) [2024;](#page-10-0) [Azar et al.,](#page-8-2) [2024;](#page-8-2) [Ethayarajh et al.,](#page-8-3) [2024;](#page-8-3) [Xiao and](#page-10-5) [Wang,](#page-10-5) [2021;](#page-10-5) [Wang et al.,](#page-10-6) [2023;](#page-10-6) [Xiao et al.,](#page-10-7) [2024b;](#page-10-7) [Yuan et al.,](#page-10-8) [2024b\)](#page-10-8). Nevertheless, the question of the best use of human demonstration data remains largely unexplored. Is SFT the best way to align large language models from demonstration data?

In this paper, we make the first attempt to answer this question by proposing GSIL, a family of imitation learning losses, which enables a unified view of alignment from offline demonstrations.

3 The Proposed Method

In this section, we begin by formally introducing the imitation learning formulation for language model alignment and transforming it into an equivalent form, which can effectively use the demonstration data and conduct alignment efficiently.

Figure 1: Illustration of different characteristics of KL divergence. SFT exhibits mass-covering behavior by minimizing forward KL, while our GSIL exhibits modeseeking behavior by minimizing reverse KL.

3.1 The Overall Objective for GSIL

We formulate the objective of imitation learning as minimizing the reverse KL-divergence between π_{θ} and the demonstration distribution π_{data} [\(Kostrikov et al.,](#page-9-12) [2019;](#page-9-12) [Fu et al.,](#page-9-15) [2018\)](#page-9-15):

$$
\min_{\theta} \ell_{\text{GSIL}}(\theta) = \text{KL}\big(\pi_{\theta}(\mathbf{y} \mid \mathbf{x}) \| \pi_{\text{data}}(\mathbf{y} \mid \mathbf{x})\big)
$$

$$
= \mathbb{E}_{\pi_{\theta}(\mathbf{y} \mid \mathbf{x})} \Big[\log \frac{\pi_{\theta}(\mathbf{y} \mid \mathbf{x})}{\pi_{\text{data}}(\mathbf{y} \mid \mathbf{x})} \Big], \quad (6)
$$

where GSIL finds the model parameters by minimizing the reverse KL divergence, instead of optimizing the forward KL divergence in SFT as shown in Equation [\(2\)](#page-1-1). In theory, while minimizing these two divergences theoretically leads to the same optimal solution π_{θ^*} , achieving this in practice requires full data coverage and infinite model expressive ability that are rarely met. Consequently, in practical settings, minimizing either KL divergence results in learned policies that exhibit different properties, as discussed in [\(Murphy,](#page-9-16) [2012\)](#page-9-16). Specifically, forward KL KL($\pi_{\text{data}}||\pi_{\theta}$) promotes mass-covering behavior, whereas reverse KL KL(π_{θ} || π_{data}) encourages mode-seeking behavior [\(Tajwar et al.,](#page-10-0) [2024;](#page-10-0) [Nachum et al.,](#page-9-17) [2016;](#page-9-17) [Agarwal et al.,](#page-8-6) [2019;](#page-8-6) [Xiao et al.,](#page-10-9) [2021\)](#page-10-9) as shown in Figure [1.](#page-2-0) Thus, forward KL encourages all responses in datasets to have equal probability, leading to an overestimation of the long tail of the target distribution, whereas reverse KL sharpens the probability mass on certain high-quality regions. Alignment commits to generating a certain subset of high-quality responses, which is achieved more effectively by minimizing the reverse KL, a shown by the recent work [\(Tajwar et al.,](#page-10-0) [2024\)](#page-10-0).

In Section [4,](#page-5-0) we empirically demonstrate the results of optimizing these two divergences in practice and show the superiority of optimizing reverse KL divergence, especially on reasoningheave downstream tasks such as math problemsolving, code generation, and logical reasoning.

However, performing mode-seeking is generally more challenging than mass-covering. Directly optimizing Equation [\(6\)](#page-2-1) hardly leverages demonstration data effectively, especially since the data policy π_{data} is always unknown. In the RL literature, these challenges have been addressed through adversarial training [\(Ho and Ermon,](#page-9-8) [2016;](#page-9-8) [Fu et al.,](#page-9-15) [2018\)](#page-9-15). These methods involve learning a reward function from demonstrations using complex and unstable adversarial training, which can be difficult to implement and adapt for LLM alignment.

In this paper, we propose a straightforward alternative that leverages demonstration data without necessitating the learning of a reward function via adversarial training. We observe that optimizing the objective [\(6\)](#page-2-1) with respect to π_{θ} requires the log density ratio $\log \frac{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})}{\pi_{\theta}(\mathbf{y}|\mathbf{x})}$ between the data distribution and the current optimization policy. To circumvent this chicken-and-egg problem, we reformulate the imitation learning objective in Equation [\(6\)](#page-2-1) into the following surrogate objective:

$$
\max_{\theta} \mathbb{E}_{\pi_{\theta}(\mathbf{y}|\mathbf{x})} \left[\log \frac{\pi_{\text{data}}(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})} - \log \frac{\pi_{\theta}(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})} \right] =
$$

$$
\mathbb{E}_{\pi_{\theta}(\mathbf{y}|\mathbf{x})} \left[r(\mathbf{x}, \mathbf{y}) \right] - \text{KL} \left(\pi_{\theta}(\mathbf{y} \mid \mathbf{x}) || \pi_{\theta_t}(\mathbf{y} \mid \mathbf{x}) \right), (7)
$$

where $r(\mathbf{x}, \mathbf{y}) \triangleq \log \frac{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})}$ can be viewed as an auxiliary reward function. Equations [\(6\)](#page-2-1) and [\(7\)](#page-3-0) are equivalent by adding and subtracting the same $\mathbb{E}_{\pi_{\theta}(\mathbf{y}|\mathbf{x})}[\log \pi_{\theta_t}(\mathbf{y}|\mathbf{x})]$ and $\pi_{\theta_t}(\mathbf{y}|\mathbf{x})$ can be the initial reference policy π_{ref} or the optimization policy in the last iteration used to sample the data. Interestingly, we find that even when only demonstration data is available, this objective takes a form similar to that used in the RLHF objective [\(3\)](#page-1-0). The primary difference lies in the reward being the estimated log density ratio, which is often not readily accessible in real-world applications. The optimization of this objective, involving the density ratio $r(\mathbf{x}, \mathbf{y})$, is not straightforward. We will demonstrate how to efficiently optimize it by effectively utilizing offline human demonstration data.

3.2 Density Ratio Estimation

Before delving into the problem [\(7\)](#page-3-0), we first describe how to calculate the auxiliary reward function in terms of the density ratio. In the tabular setting, we can directly compute $\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})$ and $\pi_{data}(\mathbf{y} \mid \mathbf{x})$. However, in a high-dimensional language domain, estimating the densities separately and then calculating their ratio hardly works well due to error accumulation. A simple alternative

is to estimate the log ratio via learning a classifier (discriminator) s^* with logistic regression.

$$
\min_{s} \ell_{\text{DRE}}(s) = - \mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})} [\log \sigma(s(\mathbf{x}, \mathbf{y}))]
$$
(8)

$$
- \mathbb{E}_{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})} [\log(1 - \sigma(s(\mathbf{x}, \mathbf{y}))],
$$

where we view data samples as arising from data distribution over binary labels, where $\pi_{data}(\mathbf{y}|\mathbf{x})$ and $\pi_{\theta_t}(\mathbf{y}|\mathbf{x})$ are the densities of the classconditional distribution. Thus, the log density ratio are related to the optimal classifier probabilities via following Bayes' rule [\(Bickel et al.,](#page-8-7) [2009\)](#page-8-7):

$$
\log\left(\frac{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})}\right)^{\beta} = \log\frac{P(c=0)P(c=1|\mathbf{x}, \mathbf{y})}{P(c=1)P(c=0|\mathbf{x}, \mathbf{y})}
$$

$$
= \log\left(\frac{1}{\alpha}\frac{\sigma(s^*(\mathbf{x}, \mathbf{y}))}{1 - \sigma(s^*(\mathbf{x}, \mathbf{y}))}\right),\tag{9}
$$

where $\sigma(x) = \frac{1}{1+e^{-x}}$ is the sigmoid function that converts predicted scores into probabilities, and $\frac{P(c=1)}{P(c=0)}$ is the constant ratio between the priors of two classes. For simplicity, we heuristically introduce a hyperparameter $\alpha = \frac{P(c=1)}{P(c=0)}$ to denote the prior weight. Later, in our experiments, we will find it helpful to consider the class prior weight to the alignment process. $0 < \beta < 1$ introduced here is a power scaling parameter to control the tradeoff between bias and variance, which interpolates between the uniform importance weights and the default weights [\(Grover et al.,](#page-9-18) [2019\)](#page-9-18). While Equation[\(9\)](#page-3-1) uses logistic regression for density ratio estimation, we can similarly derive expressions under arbitrary binary discrimination losses, resulting in different GSIL variants, as shown in Section [3.4.](#page-4-0)

3.3 Generalized Self-Imitation Learning

The objective [\(7\)](#page-3-0) with the discriminator for density ratio estimation can efficiently utilize the demonstration data. However, policy learning with the RLstyle objective [\(7\)](#page-3-0) is as challenging as in RLHF, and the computational costs for both density ratio estimation and policy learning are significantly higher than those of standard SFT. This makes them difficult to implement and use on large-scale problems, such as fine-tuning language models. We propose a simpler alternative that directly optimizes the imitation learning objective without needing RL training or a discriminator. The key idea is to leverage a specific discriminator parameterization, enabling a direct extraction of optimal policy, without an RL loop. Specifically, the optimal policy in [\(7\)](#page-3-0) has a closed form as shown in [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2):

$$
\pi^*(\mathbf{y} \mid \mathbf{x}) = \frac{1}{Z(\mathbf{x})} \pi_{\theta_t}(\mathbf{y} \mid \mathbf{x}) \exp(r(\mathbf{x}, \mathbf{y})), \quad (10)
$$

where $Z(\mathbf{x}) = \sum_{\mathbf{y}} \pi_{\theta_t}(\mathbf{y}|\mathbf{x}) \exp(r(\mathbf{x}, \mathbf{y})) = \sum_{\mathbf{x}} \pi_{\text{data}}(\mathbf{y}|\mathbf{x}) = 1$, meaning that the optimal $\mathbf{y} \, \pi_{\text{data}}(\mathbf{y}|\mathbf{x}) = 1$, meaning that the optimal $\pi^*(y|\mathbf{x})$ is forced to be self-normalized! This characteristic, determined by the reward definition in [\(7\)](#page-3-0), is beneficial as it allows GSIL theoretically generalize to broader classes of loss functions beyond the pairwise BT preference model used in DPO [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2) and SPIN [\(Chen et al.,](#page-8-8) [2024\)](#page-8-8) (see Section [3.4\)](#page-4-0). Combing Equations [\(9\)](#page-3-1) and [\(10\)](#page-4-1) with some simple algebra gives us:

$$
\beta \log \frac{\pi^*(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})} = \log \left(\frac{1}{\alpha} \frac{\sigma(s^*(\mathbf{x}, \mathbf{y}))}{1 - \sigma(s^*(\mathbf{x}, \mathbf{y}))} \right)
$$

\n
$$
\Rightarrow s^*(\mathbf{x}, \mathbf{y}) = \beta \log \frac{\pi^*(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})} + \log \alpha.
$$
 (11)

With this reparameterization, we can express the density ratio estimation in terms of only the optimal policy π^* and the sampling policy π_{θ_t} as:

$$
\ell_{\text{DRE}}^{*} = -\mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})} [\log \sigma(\beta \log \frac{\pi^{*}(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_{t}}(\mathbf{y} \mid \mathbf{x})} + \gamma)] -
$$

$$
\mathbb{E}_{\pi_{\theta_{t}}(\mathbf{y}|\mathbf{x})} [\log(1 - \sigma(\beta \log \frac{\pi^{*}(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_{t}}(\mathbf{y} \mid \mathbf{x})} + \gamma))], \qquad (12)
$$

where we define $\gamma = \log \alpha$ without loss of generality. Now, we have the probability of density ratio probability in terms of the optimal policy rather than the discriminator model, we can formulate the following maximum likelihood objective for a parameterized policy [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2):

$$
\ell_{\text{GSIL}}(\boldsymbol{\theta}) = -\mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})} \left[\log \sigma(\beta \log \frac{\pi_{\boldsymbol{\theta}}(\mathbf{y} \mid \mathbf{x})}{\pi_{\boldsymbol{\theta}_t}(\mathbf{y} \mid \mathbf{x})} + \gamma) \right]
$$

$$
-\mathbb{E}_{\pi_{\boldsymbol{\theta}_t}(\mathbf{y}|\mathbf{x})} \left[\log(1 - \sigma(\beta \log \frac{\pi_{\boldsymbol{\theta}}(\mathbf{y} \mid \mathbf{x})}{\pi_{\boldsymbol{\theta}_t}(\mathbf{y} \mid \mathbf{x})} + \gamma)) \right], \quad (13)
$$

where the gradient of this objective takes the form of the difference between two parts, one related to the demonstration data and the other related to data self-generated by the policy. Interestingly, this optimization also provides actionable and theoretical insights into a self-improvement pattern: *we iteratively generate syntactic data from the model itself, improving the policy by contrasting these self-generated data with real demonstration data.*

3.4 Generalizations and Extensions

A central insight of this work is to frame imitation learning as a supervised binary classification between real demonstration data and self-generated

Table 1: Summary of various loss functions of GSIL: $\ell_{\text{GSIL}}(\boldsymbol{\theta}) = \mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})}[\ell_1(f_{\boldsymbol{\theta}})] + \mathbb{E}_{\pi_{\boldsymbol{\theta}_t}}[\ell_{-1}(f_{\boldsymbol{\theta}})]$ as a function of the difference of log ratio f_{θ} = $\beta \log \frac{\pi_{\theta}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})} + \gamma$ (please refer to Figure [10](#page-12-0) in the Appendix for the visualization of losses).

Loss	$\ell_1(f_\theta)$	$\ell_{-1}(f_\theta)$
Logistic	$\log(1+e^{-f_{\theta}})$	$\log(1+e^{f\theta})$
Hinge	$\max(0, 1 - f_{\theta})$	$\max(0, 1 + f_{\theta})$
Brier	$(e^{-f_{\theta}}/(1+e^{-f_{\theta}}))^{2}$	$(1/(1+e^{-f_{\theta}}))^2$
Exponential	$e^{-f_{\theta}/2}$	$e^{f\theta/2}$
KLIEP LSIF	$-f_{\theta}$ $-e^{f_{\theta}}$	$\rho^f \theta$ $\frac{1}{2}e^{2f_{\theta}}$

syntactic data from the model itself. The discussion in Section [3.2](#page-3-2) suggests that any binary losses for density ratio estimation can be used in GSIL. Existing density ratio estimation losses can be cast in the following general form [\(Buja et al.,](#page-8-9) [2005;](#page-8-9) [Gneiting](#page-9-19) [and Raftery,](#page-9-19) [2007;](#page-9-19) [Sugiyama et al.,](#page-10-10) [2012\)](#page-10-10):

$$
\min_{s} \ell_{\text{DRE}}(s) = \mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})} [\ell_1(s(\mathbf{x}, \mathbf{y}))]
$$

$$
+ \mathbb{E}_{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})} [\ell_{-1}(s(\mathbf{x}, \mathbf{y}))]. \tag{14}
$$

Let s^* be the optimal in the above estimation loss, following Section [3.2,](#page-3-2) the auxiliary reward in terms of density ratio can be written as follows:

$$
r(\mathbf{x}, \mathbf{y}) = \frac{1}{\beta} \log \left(\alpha \frac{\sigma \left(s^*(\mathbf{x}, \mathbf{y}) \right)}{1 - \sigma \left(s^*(\mathbf{x}, \mathbf{y}) \right)} \right). \tag{15}
$$

As shown in [\(11\)](#page-4-2), we can express the score function s in terms of its corresponding optimal policy:

$$
s^*(\mathbf{x}, \mathbf{y}) = \beta \log \frac{\pi^*(\mathbf{y} \mid \mathbf{x})}{\pi_{\theta_t}(\mathbf{y} \mid \mathbf{x})} + \gamma,
$$
 (16)

where $\gamma = \log \alpha$. With this alternative reparameterization, the general loss in [\(14\)](#page-4-3) can be rewritten with respect to the parametrized policy π_{θ} as:

$$
\min_{\boldsymbol{\theta}} \ell_{\text{GSIL}}(\boldsymbol{\theta}) = \mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})} [\ell_1(f_{\boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}))]
$$

$$
+ \mathbb{E}_{\pi_{\boldsymbol{\theta}_t}(\mathbf{y}|\mathbf{x})} [\ell_{-1}(f_{\boldsymbol{\theta}}(\mathbf{x}, \mathbf{y}))], \quad (17)
$$

where $f_{\theta}(\mathbf{x}, \mathbf{y}) \triangleq \beta \log \frac{\pi_{\theta}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})} + \gamma$. Table 1 summarizes some notable density estimation methods developed over decades, including classification losses such as Hinge [\(Cortes and Vapnik,](#page-8-10) [1995\)](#page-8-10), Brier [\(Gneiting and Raftery,](#page-9-19) [2007\)](#page-9-19), Exponential [\(Freund and Schapire,](#page-9-20) [1995\)](#page-9-20), and mean matching losses such as KLIEP and LSIF [\(Sugiyama](#page-10-10) [et al.,](#page-10-10) [2012\)](#page-10-10), each loss mapping into an alignment algorithm in our GSIL framework. Intuitively, these

Figure 2: The reward dynamics for SPIN and GSIL w/ Logistic on UltraFeedback show increasing margins between the rewards of real demonstrations and selfgenerated data. In SPIN, however, the rewards for real data drop below zero, while in GSIL, they continue to increase and stay positive. Results for other losses in the GSIL framework are provided in Figure [5](#page-7-0) in Section [4.](#page-5-0)

losses increase the likelihood of responses in the demonstration while promoting a decrease in the likelihood of synthetically self-generated data.

Comparison to SPIN. We discuss the connection between our framework with the recently proposed self-play fine-tune (SPIN) algorithm [\(Chen et al.,](#page-8-8) [2024\)](#page-8-8), which is motivated from a two-player game perspective. Specifically, SPIN optimizes the following pair-wise losses based on the Bradley-Terry model on the demonstration data:

$$
\mathbb{E}_{\pi_{\text{data}}, \pi_{\theta_t}} \big[-\log \sigma(f_{\theta}(\mathbf{x}, \mathbf{y}) - f_{\theta}(\mathbf{x}, \mathbf{y}')) \big], \quad (18)
$$

where $f_{\theta}(\mathbf{x}, \mathbf{y}) \triangleq \beta \log \frac{\pi_{\theta}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})}$. SPIN and its theoretical guarantee rely on explicit assumptions about the Bradley-Terry model, which essentially only maximizes the gap between the likelihoods of the true and generated responses, as in the case of DPO. Recent works [\(Pal et al.,](#page-9-21) [2024;](#page-9-21) [Yuan et al.,](#page-10-11) [2024a;](#page-10-11) [Tajwar et al.,](#page-10-0) [2024\)](#page-10-0) show that the likelihood of the chosen response can continue to decrease during preference fine-tuning with DPO as long as the relative difference in likelihoods between the chosen and rejected responses remains large.

In this paper, we further investigate this implication in SPIN with fine-tuning on the demonstration data. Figure [2](#page-5-1) shows that the likelihood of true responses in the demonstration counterintuitively continues to decrease, although it remains higher than the likelihood of the generated response in SPIN. An undesirable consequence of this behavior is that the learned policy may increase the likelihood of unknown out-of-distribution responses [\(Tajwar et al.,](#page-10-0) [2024\)](#page-10-0), instead of maximizing the likelihood of the chosen response, which is important in many practical applications of large language models, e.g., reasoning, coding, and mathematical problem solving, as shown in [\(Pal et al.,](#page-9-21) [2024;](#page-9-21) [Yuan et al.,](#page-10-11) [2024a\)](#page-10-11) and our experiments.

4 Experiments

In this section, we present the main experimental results, highlighting the superior performance of GSIL on various benchmarks and ablation studies.

4.1 Experiment Setup

Data. We evaluate GSIL on two widely used datasets for alignment: the UltraFeedback binarized dataset [\(Tunstall et al.,](#page-10-3) [2023\)](#page-10-3) and the Anthropic-HH dataset [\(Bai et al.,](#page-8-0) [2022\)](#page-8-0). Note that while these datasets provide paired chosen and rejected response, we only utilize the chosen response to form the demonstration dataset. The details of datasets are in Appendix [A.1.](#page-10-12)

Evaluation. We evaluate methods fine-tuned on the UltraFeedback on various benchmarks: (ARC [\(Clark et al.,](#page-8-11) [2018\)](#page-8-11), Winogrande [\(Sakaguchi](#page-9-22) [et al.,](#page-9-22) [2021\)](#page-9-22)), math reasoning (GSM8K [\(Cobbe](#page-8-12) [et al.,](#page-8-12) [2021\)](#page-8-12)) and coding (HumanEval [\(Chen et al.,](#page-8-13) [2021\)](#page-8-13)). We also use the most popular instructionfollowing benchmark: MT-Bench [\(Zheng et al.,](#page-10-13) [2024\)](#page-10-13) for assessing alignment performance. The Anthropic-HH dataset is used for dialogue generation to produce helpful and harmless responses [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2). For Anthropic-HH, we treat GPT-4 [\(Achiam et al.,](#page-8-14) [2023\)](#page-8-14) pairwise win-rates over chosen demonstration as the evaluation metric (see Appendix [A.2](#page-10-14) for details). Models. For training on Anthropic-HH , we use Pythia-2.8b [\(Biderman et al.,](#page-8-15) [2023\)](#page-8-15) as our base model following [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2).

For fine-tuning of the UltraFeedback Binarized dataset, we the Zephyr-7b-sft [\(Tunstall et al.,](#page-10-3) [2023\)](#page-10-3) as our base model rigorously following previous works [\(Tunstall et al.,](#page-10-3) [2023;](#page-10-3) [Chen et al.,](#page-8-8) [2024\)](#page-8-8). Baselines. We primarily compare our methods with the standard SFT and recently proposed SPIN [\(Chen et al.,](#page-8-8) [2024\)](#page-8-8) which also only utilize the demonstration data. For details of the implementation, please refer to Appendix [A.3.](#page-12-1)

4.2 Comparison on Benchmarks

Table [2](#page-6-0) compares the performance of GSIL against fine-tuning methods with demonstration data on UltraFeedback. As shown in the table, all variants of GSIL achieve remarkable improvements over SFT, particularly notable on challenging benchmarks. While SPIN can also enhance performance over the SFT model, GSIL, despite its simplicity, achieves the best overall performance on all benchmarks. These consistent and significant improve-

Models	ARC	TruthfulOA	Winogrande	GSM8K	HumanEval	MT-Bench
SFT	58.28	40.35	76.40	28.13	26.82	6.25
SPIN	57.00	53.98	77.03	28.63	31.70	6.47
GSIL w/ KLIEP	57.68	56.11	76.95	30.71	35.97	6.84
GSIL w/ LSIF	58.79	56.59	77.01	30.40	31.09	6.68
GSIL w/ Hinge	57.85	55.13	76.64	30.63	32.31	6.58
GSIL w/ Brier	58.19	58.76	77.11	28.81	32.92	6.85
GSIL w/ Exponential	57.03	57.19	77.31	30.52	34.32	6.71
GSIL w/ Logistic	57.76	55.43	77.43	31.84	36.58	6.89

Table 2: We train all methods on Zephyr-7b-sft with UltraFeedback. GSIL significantly improves SFT and SPIN on challenging benchmarks: TruthfulQA (Factuality), GSM8K (Math), and HumanEval (Code), and MT-Bench.

different trade-offs are imposed by different losses. Figure 3: Results on MT-Bench with regard to different types of questions. We can observe GSIL shows significant gains in reasoning, math, and coding tasks and

ments highlight the robustness and effectiveness of GSIL. Notably, GSIL with logistic loss outperforms SPIN by 3.2 points in GSM8K (Math) and by 4.9 points in HumanEval (Code). We hypothesize that these improvements over SPIN can be attributed to the non-decreasing likelihood of real demonstrations in GSIL; as the likelihood of real samples decreases, it results in suboptimal performance, especially in mathematical reasoning and coding tasks where the chosen responses are very likely ground-truth answers. While almost all losses in our GSIL offer a significant improvement over SFT and SPIN, Logistic loss and Brier loss perform best in challenging tasks, making them worth considering as the initial attempts in practice. In Figure [3,](#page-6-1) we detail the model performances on MT-Bench with regard to different types of question.

We also compare the performance of GSIL, SPIN, and SFT on MT-Bench, which evaluate the models' versatile conversational abilities across a diverse set of queries based on GPT-4. From the table, we observe that GSIL significantly boosts the performance, which demonstrates the effectiveness of GSIL on the instruction-following task.

Figure 4: The win rates, computed by GPT-4, in comparison to the chosen responses for Anthropic-HH one-step dialogue. Here, we utilize logistic loss for our GSIL as we observe similar performance across different losses.

4.3 Comparison on Safety Alignment

To further evaluate the effectiveness of GSIL on safety alignment, we use the Anthropic-HH dataset, which contains 170k dialogues between a human and an automated assistant. Each transcript ends with a pair of responses generated by a large (although unknown) language model, along with a preference label denoting the human-preferred response in terms of harmlessness and helpfulness. Again, we only use the chosen responses as the demonstration data to train our policy. Figure [4](#page-6-2) shows the win rates computed by GPT-4 over the chosen responses in the test set. Remarkably, GSIL aligns better with human preferences than the base model, SFT, and SPIN, achieving win rates of approximately 60% against the chosen responses. Additionally, we provide examples generated by both SPIN and GSIL in Tables [5](#page-13-0) and [6](#page-13-1) in Appendix D.1. These examples indicate that GSIL shows strong promise in terms of aligning language models and can ensure that the generated responses are not only high-quality but also safe and harmless.

4.4 Ablation Studies and Further Analysis

Training Dynamics. We also investigated the reward patterns during the training process of GSIL.

Figure 5: The training dynamics of real rewards of demonstration data and margins show that, for all our objectives, the margins between the rewards of real demonstrations and self-generated data keep increasing. Additionally, the rewards of real data continue to increase and remain positive.

Figure 6: Comparison between GSIL (Logistic) and DPO with UltraFeedback. GSIL even significantly outperforms DPO, which requires preference feedback.

Table 3: The results of iterative self-play strategy: GSIL (Logistic) generates its training data from its previous iterations. We found that GSIL consistently improve along with the iterative alignment iteration.

Models	TruthfulOA		GSM8K HumanEval MT-Bench	
SFT	40.35	28.13	26.82	6.25
SPIN	53.98	28.63	31.70	6.47
GSTI Iter1	55.43	31.84	36.58	6.89
GSTI Iter2	56.73	31.95	39.27	6.91
GSTI Iter3	57.81	30.51	42.15	6.97

Figures [2](#page-5-1) and [5](#page-7-0) presents the reward patterns of GSIL and SPIN on the UltraFeedback dataset. We observe that the rewards of the generated data keep decreasing, and the margins between the real and generated responses keep increasing. However, the rewards of the real responses continue to decrease in the case of SPIN, whereas they do not decrease in the case of GSIL. These results verify our motivation and the effectiveness of GSIL in reasoning, math, and coding tasks, which require maintaining the likelihood of real demonstration data.

The Impact of β and γ . We investigate how the parameters β and γ in GSIL affect performance on benchmarks in Figure [7.](#page-7-1) We find that β is crucial: a small β typically enhances model performance, while a large β keeps the policy too close to the reference policy, leading to suboptimal outcomes. Conversely, an increase in weight γ consistently improves accuracy across benchmarks, suggesting that a greater focus on demonstration data boosts

Figure 7: Performance on GSM8K under various β and γ . See Figures [8](#page-11-0) and [9](#page-11-1) in the Appendix for more results.

performance. The distinct impacts of β and γ stem from their roles in our GSIL: β scales the log probability and γ applies an additional prior weight (e^{γ}) to real demonstration data (see Equation [\(9\)](#page-3-1)).

Training with More Iterations. We investigate the impact of conducting additional training iterations: GSIL w/ Logistic is iteratively trained with selfplay generated data collected from the model in the previous iteration. Interestingly, from Table [3,](#page-7-2) we can find that even one additional iteration of GSIL can improve performance, and GSIL generally shows steady performance gains across iterations, outperforming other baselines. However, training for more iterations leads to a slight decrease in GSM8K performance, possibly due to overfitting.

5 Conclusions

In this paper, we propose GSIL, a simple and generalized framework for language model alignment with offline demonstration data from an imitation learning perspective. By aligning the auxiliary reward function with the optimal policy, GSIL eliminates the need for adversarial training, achieving simple and fast fine-tuning. Importantly, GSIL enables a unified view on imitation learning on demonstration data and sheds light on connecting a rich literature on density ratio estimation to the designs of offline alignment with only demonstration data. Extensive experiments show that our algorithms consistently outperform existing approaches such as SFT and SPIN across various benchmarks, including MT-Bench and Open LLM Leaderboard.

6 Limitations and Broader Impacts

First, despite the empirical success and rigorous derivation, our GSIL introduces an additional shift hyperparameter. It would be interesting to explore how to determine the optimal shift automatically. In addition, GSIL is an alignment algorithm that uses only demonstration data and does not leverage human preference data. Future work could explore the integration of GSIL with preference fine-tuning methods to further improve model performance. We hope that this work can serve as a foundation for further exploration of imitation learning in the context of LLM alignment with demonstration data.

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A Experimental Details

A.1 The Details of Datasets

UltraFeedback Binarized^{[1](#page-10-15)} [\(Cui et al.,](#page-8-16) [2023;](#page-8-16) [Tun](#page-10-3)[stall et al.,](#page-10-3) [2023\)](#page-10-3) contains 62k prompts in the training set, each accompanied by four model completions from various open and proprietary models. GPT-4 assigns scores to each completion based on criteria such as helpfulness and honesty. Binary preferences are constructed by selecting the response with the highest mean score as the chosen response and one of the remaining three at random as the rejected response. In our experiments, we use only the chosen responses as demonstration data to train the policy with GSIL.

Anthropic-HH 2 2 [\(Bai et al.,](#page-8-0) [2022\)](#page-8-0) comprises 170k dialogues between a human and an automated assistant, used for assessing single-turn dialogue performance. Each dialogue includes a human query paired with model responses rated for helpfulness and harmlessness. Following DPO [\(Rafailov et al.,](#page-9-2) [2024b\)](#page-9-2), the preferred responses from this dataset were used for the supervised Fine-Tuning (SFT) phase, aligning the initial model behavior with desirable conversational outcomes. Similarly, in our experiments, we use only the chosen responses as demonstration data to train the policy with GSIL.

A.2 Downstream Task Evaluation

To examine how alignment methods affect downstream performance, we evaluate methods fine-tuned on the UltraFeedback Binarized dataset across the following tasks: ARC [\(Clark](#page-8-11)

¹ [https://huggingface.co/datasets/](https://huggingface.co/datasets/HuggingFaceH4/ultrafeedback_binarized) [HuggingFaceH4/ultrafeedback_binarized](#page-8-11)

² [https://huggingface.co/datasets/Anthropic/](https://huggingface.co/datasets/Anthropic/hh-rlhf) [hh-rlhf](#page-8-11)

For the following dialogue history to a chatbot, which response is more helpful and harmless?

Dialogue history: {dialogue history} Response 1: {Response 1} Response 2: {Response 2} [FIRST provide a one-sentence comparison of the two responses and explain which you](#page-8-11) feel is more helpful and harmless. SECOND, on a new line, state only "1" or "2" to indicate which response is more helpful and harmless. Your response should use the format: Comparison: < one-sentence comparison and explanation> More helpful: <"1" or "2">

Table 4: Prompt for GPT-4 evaluation for the dialogue generation task on the Anthropic-HH dataset. {dialogue history }, {Response 1}, and {Response 2} are placeholders.

[et al.,](#page-8-11) [2018\)](#page-8-11), TruthfulQA [\(Lin et al.,](#page-9-23) [2021\)](#page-9-23), Winogrande [\(Sakaguchi et al.,](#page-9-22) [2021\)](#page-9-22), and GSM8K [\(Cobbe et al.,](#page-8-12) [2021\)](#page-8-12). We use the version of the Language Model Evaluation Harness library 3 [\(Gao et al.,](#page-9-24) [2023b\)](#page-9-24) suggested by the Hug-

3 [https://github.com/EleutherAI/](https://github.com/EleutherAI/lm-evaluation-harness/tree/b281b0921b636bc36ad05c0b0b0763bd6dd43463) [lm-evaluation-harness/tree/](https://github.com/EleutherAI/lm-evaluation-harness/tree/b281b0921b636bc36ad05c0b0b0763bd6dd43463) [b281b0921b636bc36ad05c0b0b0763bd6dd43463](https://github.com/EleutherAI/lm-evaluation-harness/tree/b281b0921b636bc36ad05c0b0b0763bd6dd43463) gingFace Open LLM Leaderboard. The details are:

ARC (25-shot): This task is called the AI2 reasoning challenge and uses a set of grade-school science questions for commonsense reasoning evaluation.

Winogrande (5-shot): This task is an adversarial and difficult Winograd benchmark at scale, for commonsense reasoning.

Figure 10: Illustration of various loss objectives in our GSIL on demonstration data: $\ell_1(f_{\theta})$ and self-generated data: $\ell_{-1}(f_{\theta})$ for our imitation learning loss: $\ell_{\text{GSIL}}(\theta) = \mathbb{E}_{\pi_{\text{data}}(\mathbf{y}|\mathbf{x})}[\ell_1(f_{\theta})] + \mathbb{E}_{\pi_{\theta_t}}[\ell_{-1}(f_{\theta})]$ as a function of the difference of log ratio $f_{\theta} = \beta \log \frac{\pi_{\theta}(\mathbf{y}|\mathbf{x})}{\pi_{\theta_t}(\mathbf{y}|\mathbf{x})} + \gamma$ between the optimizing policy and reference policy.

TruthfulQA (0-shot): This is a dataset of questions specifically designed to evaluate a model's ability to provide truthful, factual, and accurate responses. It focuses on challenging the common tendency of AI models to generate plausible but false answers, thereby testing their capability to discern and adhere to truthfulness in their responses. This dataset plays a critical role in assessing the reliability and trustworthiness of AI-generated information. TruthfulQA is technically a 6-shot task in the Harness because each example is prepended with 6 Q/A pairs, even in the 0-shot setting.

GSM8K (5-shot): This is a dataset of high-quality linguistically diverse grade school math word problems. Numerical reasoning tasks within this dataset typically comprise a descriptive component followed by a culminating question. Answering this question requires multi-step mathematical calculations based on the context of the description.

HumanEval^{[4](#page-12-2)}: This dataset released by OpenAI includes 164 programming problems with a function signature, docstring, body, and several unit tests. They were handwritten to ensure not to be included in the training set of code generation models. We report Pass@1 in our experiments.

MT-Bench 5 : This is a benchmark for assessing chat LLMs' general and multi-turn abilities. It contains a set of challenging multi-turn openended questions covering topics such as writing, role-playing, math, coding, and more. The modelgenerated answers are judged by GPT-4 via a scalar score (from 1 to 10).

Anthropic-HH: To further evaluate the effectiveness of GSIL on safety alignment, we use the Anthropic-HH dataset, which includes 17K interactions between humans and virtual assistants. The model is optimized to deliver useful answers across a range of queries while deliberately avoiding any harmful content. We prompt GPT-4 for zero-shot pair-wise evaluation (see Table [4\)](#page-11-3), which has been shown to be consistent with human judgments.

A.3 Implementation Details

The experiments with Pythia-2.8b are run on 4 A100 GPUs using bf16 precision, while those with Zephyr-7b-sft are run on 8 A100 GPUs. The batch size is 128, and we use the AdamW optimizer with a learning rate of 5e-7. We linearly warm up the learning rate from 0 to 5e-7 in 150 steps. To ensure a fair comparison, we perform a thorough hyperparameter tuning for all methods compared in our experiments. For SPIN and our methods, β is searched from $\{0.01, 0.1, 1\}$. The shift parameter γ in our GSIL is searched from $\{0, 1, 2\}.$

⁴ <https://github.com/openai/human-eval>

⁵ [https://github.com/lm-sys/FastChat/tree/main/](https://github.com/lm-sys/FastChat/tree/main/fastchat/llm_judge) [fastchat/llm_judge](https://github.com/lm-sys/FastChat/tree/main/fastchat/llm_judge)

Table 5: GPT-4 chooses GSIL (Logistic) over SPIN. Responses to a prompt from the Anthropic-HH test set.

Table 6: GPT-4 chooses GSIL over SPIN. Responses to a prompt from the Anthropic-HH test set.