BPE Gets Picky: Efficient Vocabulary Refinement During Tokenizer Training

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Abstract

Languag[e](#page-0-0) models can greatly benefit from efficient tokenization. However, they still mostly utilize the classical Byte-Pair Encoding (BPE) algorithm, a simple and reliable method. BPE has been shown to cause such issues as undertrained tokens and sub-optimal compression that may affect the downstream performance. We introduce PickyBPE, a modified BPE algorithm that carries out vocabulary refinement during tokenizer training by removing merges that leave intermediate "junk" tokens. Our method improves vocabulary efficiency, eliminates under-trained tokens, and does not compromise text compression. Our experiments show that this method either improves downstream performance or does not harm it.

1 Introduction

Tokenization is a relatively understudied area, but it can greatly impact model performance and efficiency [\(Rust et al.,](#page-11-0) [2021;](#page-11-0) [Hofmann et al.,](#page-10-0) [2022;](#page-10-0) [Ali et al.,](#page-9-0) [2024;](#page-9-0) [Toraman et al.,](#page-11-1) [2023;](#page-11-1) [Petrov et al.,](#page-10-1) [2023;](#page-10-1) [Singh and Strouse,](#page-11-2) [2024;](#page-11-2) [Rajaraman et al.,](#page-11-3) [2024;](#page-11-3) [Shao et al.,](#page-11-4) [2024;](#page-11-4) [Wang et al.,](#page-11-5) [2024\)](#page-11-5). Vocabularies should be efficient, as every additional token in the vocabulary increases the number of embedding parameters, and thus the model size. Each vocabulary item should contribute enough to model performance to justify the use of parameters.

In this paper, we focus on Byte-Pair Encoding (BPE; [Gage,](#page-9-1) [1994;](#page-9-1) [Sennrich et al.,](#page-11-6) [2016\)](#page-11-6) tokenizers. BPE tokenization works by breaking the text down into each of its characters or bytes and then building tokens in the vocabulary through a series of merges. The result of each merge must be stored as a token in the vocabulary. Tokens which are used only to execute merges are sometimes referred to as intermediate "junk" tokens [\(Bostrom and Durrett,](#page-9-2) [2020\)](#page-9-2). An example is shown in Figure [1.](#page-0-1) Interme-

Figure 1: An example of a series of merges to produce the token Kentucky. Pre-merge token frequencies are shown in circles. In the vanilla BPE algorithm, entucky should also be stored in the vocabulary, whereas it is redundant after the merge. In this example, Intersection over Self (IoS) effectively captures the intermediate token, as IoS(entucky) $\geq \mathcal{T} = 0.9$.

diate tokens clutter the vocabulary and are hardly ever used during tokenization.

In addition to efficiency, we consider other model behaviors that may be driven by tokenization. [Land and Bartolo](#page-10-2) [\(2024\)](#page-10-2) recently showed that very low-frequency tokens in the vocabulary may be under-trained by a model. This leads to worse downstream performance and unwanted outputs, such as hallucinations. Under-trained tokens — also called "glitch tokens" [\(Rumbelow](#page-11-7) [and Watkins,](#page-11-7) [2023;](#page-11-7) [Geiping et al.,](#page-9-3) [2024;](#page-9-3) [Li et al.,](#page-10-3) [2024\)](#page-10-3) — can also potentially be exploited to circumvent safety measures through the use of these out-of-distribution items.

Vocabulary trimming, which entails removing items from a tokenizer's vocabulary, has been proposed as a method of decreasing the number of unnecessary tokens, *e.g.*, language- or domainspecific tokens. Trimming has been shown to reduce the number of embedding parameters without degrading downstream performance [\(Ushio et al.,](#page-11-8) [2023;](#page-11-8) Pang and Vulić, [2024\)](#page-10-4). Under-trained token indicators were shown to be correlated with token frequency in the training corpus, where less frequent tokens are more likely to be under-

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trained [\(Land and Bartolo,](#page-10-2) [2024\)](#page-10-2). Vocabulary trimming, thus, is well suited to address the issue of under-trained tokens.

Vocabulary trimming has mostly been implemented as a procedure taking place after tokenizer training [\(Yang et al.,](#page-11-9) [2022;](#page-11-9) [Cognetta et al.,](#page-9-4) [2024\)](#page-9-4). As a result, it is difficult to determine the vocabulary size in advance, as it is not known beforehand how many tokens will be removed by the trimming procedure. Setting a fixed vocabulary size might be important, for example, for increasing training throughput [\(Groeneveld et al.,](#page-10-5) [2024\)](#page-10-5).

In this paper, we introduce $PickyBPE¹$ $PickyBPE¹$ $PickyBPE¹$ — a modified BPE tokenizer that implements vocabulary refinement during tokenizer training. Unlike other trimming procedures, PickyBPE effectively removes intermediate tokens once they become useless and seamlessly creates a vocabulary of the desired size without data-specific heuristics. Our method leads to more efficient usage of a limited vocabulary and, thus, of the embedding parameters. We show that our method leads to equal or better performance on a downstream translation task compared to standard BPE (Section [4\)](#page-4-0). Furthermore, we reduce the number of tokens that are likely to be under-trained (Section [5\)](#page-5-0). This frees up space for higher-quality tokens. Due to the improved quality of the fixed-size vocabulary, PickyBPE does not compromise text compression (Section [6\)](#page-7-0) unlike other trimming methods, which makes it a good candidate for practical use.

2 Related Work

Several common alternatives to BPE tokenization implicitly address the issue of intermediate lowfrequency tokens. For instance, WordPiece tokenization [\(Wu et al.,](#page-11-10) [2016\)](#page-11-10) is based on a series of merges akin to BPE, but along with the frequency of the token pair being merged, it also takes individual token frequencies into account. Thus, the tokenizer is less likely to add merges that would result in redundant tokens. However, this does not guarantee that the tokenizer adds merges in an optimal order, nor does it facilitate the retrospective removal of intermediate tokens that might eventually appear.

Another popular algorithm is Unigram tokenization [\(Kudo,](#page-10-6) [2018\)](#page-10-6) used in SentencePiece [\(Kudo and](#page-10-7) [Richardson,](#page-10-7) [2018\)](#page-10-7). The core of this algorithm is different from BPE-like solutions. Unigram works

by creating a large vocabulary and iteratively pruning it until it reaches the desired size. The pruning is performed according to how much the token removal affects the likelihood of the subword sequence, and takes into account individual token frequencies. Intermediate tokens are also less likely to appear in such a scenario, which might suggest that Unigram tokenization implicitly performs a form of vocabulary trimming.

There also exist several proposed modifications to BPE, which address the issues raised in Section [1.](#page-0-2) BPE-Dropout was proposed to mitigate the issue of rare subwords by dropping merges randomly during tokenizer training [\(Provilkov et al.,](#page-11-11) [2020\)](#page-11-11). This method regularizes BPE training to expose the model to alternate tokenizations of the same strings, making it more robust to noisy input, such as misspellings. BPE-Dropout also helps in reducing the under-training of low-frequency tokens. While it may lead to better training for low-frequency or intermediate tokens, those tokens are never used during model inference. Therefore, this method still leads to unused embedding parameters and ultimately does not improve vocabulary efficiency.

[Sennrich et al.](#page-11-12) [\(2017\)](#page-11-12) use an absolute frequency cut-off to prevent very low-frequency tokens from being added to the vocabulary. Similarly, [Vilar and](#page-11-13) [Federico](#page-11-13) [\(2021\)](#page-11-13) propose a stopping criterion in order to select the optimal vocabulary for BPE. The authors propose a maximum likelihood constraint, a point at which BPE stops adding merges during training if a merge decreases the overall likelihood of the token sequence. Building on this work, [Cognetta et al.](#page-9-4) [\(2024\)](#page-9-4) implement a vocabulary trimming method for BPE. The authors propose removing low-frequency tokens after tokenizer training by manually choosing an absolute threshold value. The choice of threshold, therefore, is specific to a given dataset and vocabulary size. Their method reduces the vocabulary size without significantly reducing downstream translation performance. In some cases, when they show the greatest task improvement, they find an increase of over 13% in sequence length, *i.e.*, text length in number of tokens. Better compression has been shown to correlate with better model performance [\(Gallé,](#page-9-5) [2019;](#page-9-5) [Liang et al.,](#page-10-8) [2023;](#page-10-8) [Goldman et al.,](#page-10-9) [2024\)](#page-10-9) and lead to faster inference time [\(Song et al.,](#page-11-14) [2021;](#page-11-14) [Petrov](#page-10-1) [et al.,](#page-10-1) [2023;](#page-10-1) [Yamaguchi et al.,](#page-11-15) [2024\)](#page-11-15). We argue that a major drawback of the method proposed by [Cognetta et al.](#page-9-4) [\(2024\)](#page-9-4) is worse compression.

In a concurrent work, [Lian et al.](#page-10-10) [\(2024\)](#page-10-10) also iden-

¹ https://github.com/pchizhov/picky_bpe

tify the issue of intermediate ("scaffold") tokens and introduce Scaffold-BPE. The authors propose to identify intermediate tokens when they are below the current range of frequencies during the tokenizer training. Their method does not allow regulating the strength of Scaffold-BPE, unlike our method, which uses a threshold hyperparameter (see Section [3\)](#page-2-0). Additionally, Scaffold-BPE functions by first tokenizing the input text with both the vocabulary and scaffold tokens, then later splitting the scaffold tokens into the minimal valid token sequence. Since this method is a post-processing technique and the final result does not reflect the training process, this inference strategy leads to inaccuracies in tokenization and worse compression (see Appendix [A\)](#page-12-0).

Another contemporaneous work by [Bauwens](#page-9-6) [and Delobelle](#page-9-6) [\(2024\)](#page-9-6) also proposes a method of pruning merges that lead to undesired segmentation and underused vocabulary items. This method differs in two key ways from previous approaches. It allows merges of more than two tokens and uses a semi-supervised method to determine which merges to remove based on manually annotated language-specific morphological segmentations. The latter makes it hard to generalize this method to other languages, especially in multilingual settings.

3 PickyBPE

Our method is a modification of the original BPE algorithm [\(Gage,](#page-9-1) [1994;](#page-9-1) [Sennrich et al.,](#page-11-6) [2016\)](#page-11-6). The intuition behind PickyBPE is that we can iden-

tify intermediate tokens based on their individual frequency and frequency within a larger token. Intermediate tokens should have low frequency outside of the context of the token that contains them. For example, in Figure [1,](#page-0-1) an intermediate token entucky is almost always a part of Kentucky, which is easy to capture by comparing the frequencies of Kentucky and entucky. To formalize this approach, we introduce a measure called *Intersection over Self (IoS)*, which is computed as follows:

$$
IoS(x_1 | x_1, x_2) = \frac{f_p(x_1, x_2)}{f_t(x_1)};
$$
 (1)

$$
IoS(x_2 | x_1, x_2) = \frac{f_p(x_1, x_2)}{f_t(x_2)}.
$$
 (2)

Here x_1 and x_2 are the tokens being merged, f_t is token frequency, and f_p is pair frequency. $\text{LoS}(x_1 | x_1, x_2)$ shows how often token x_1 occurs as part of a pair $\{x_1, x_2\}$ compared to all occurrences of x_1 . If this value is high, *i. e.*, close to 1, x_1 is highly likely an intermediate token, an integral part of a longer, more meaningful token $x_1 + x_2$. Adding $x_1 + x_2$ to the vocabulary makes x_1 redundant and we can consider removing it.

3.1 Algorithm

The training of PickyBPE follows the main steps of the vanilla BPE training. The text is first split into a sequence of characters/bytes, initializing the vocabulary with unique symbols. Optionally, the coverage parameter (we use 0.9999 in our experiments) is used to replace the rarest symbols with <unk>. After that, the algorithm iteratively chooses the most frequent pair of tokens to merge and adds it to the vocabulary. PickyBPE diverges from vanilla BPE in that after each merge when we check

Figure 2: Example of PickyBPE tokenizer training. Token frequencies are shown in the corresponding circles and are updated on merges. Token "ould" is removed only after merging into three common tokens containing it. The corresponding IoS values are visualized on every merge. Once IoS becomes greater than or equal to the threshold \mathcal{T} (0.9 in this example), the token "ould" is removed.

whether we can remove any of the merged tokens according to its IoS value. The pseudocode for a training step is demonstrated in Algorithm [1.](#page-2-1) We integrate the IoS metric into the merging stage. When a pair of tokens is merged, we check whether we can safely remove either of the two tokens from the vocabulary. For this, we introduce a hyperparameter $\mathcal T$, the IoS threshold. If IoS $(x_1 | x_1, x_2) \geq \mathcal T$, we remove x_1 . Thus, $\mathcal T$ regulates the strength of the removal policy: $\mathcal T$ is a positive value ≤ 1 , and the closer it is to 1, the less strict the removing criterion becomes. For instance, $T = 0.9$ means that only the tokens that occur outside of the new merge in no more than 10% of cases will be removed. In an extreme case, $\mathcal{T} = 1$ means that no removals are possible, thus the algorithm becomes the vanilla BPE. Another unique feature of our algorithm is that the merges and removals are stored in the event order array $\mathcal E$ in the chronological order. Preserving the original order of events is crucial for the tokenization step.

The tokenization (inference) step is described in Algorithm [2.](#page-2-2) We first split the input word into a series of in-vocabulary symbols. Then we collect the sets of possible merges and removals in the current tokenization and iteratively greedily choose the earliest possible event using event order \mathcal{E} . The action associated with the chosen event is performed and the sets of possible merges and removals are updated. This process strictly follows the tokenizer

training and avoids compression issues that occur with approximation methods (see Appendix [A\)](#page-12-0).

3.2 Algorithm analysis and justification

The training of PickyBPE takes longer than that of the original vanilla BPE. However, the difference is not drastic. When a token is removed, recalculating the frequencies requires a constant number of operations, which makes the training time depend linearly on the number of events (merges and removals). With threshold $\mathcal T$ values of 0.6 and higher, the proportion of removed tokens generally does not surpass 10% (for details refer to Appendix [E\)](#page-13-0), which makes the number of removals inferior to the number of merges. At the tokenization stage, the inference time depends on the number of events, just as the tokenization time of the vanilla BPE depends on the number of merges. As we show in Appendix [E,](#page-13-0) merges comprise the largest proportion of overall events. Therefore, the removal events do not significantly slow down the inference.

In addition to achieving the primary goal of removing intermediate tokens from the vocabulary, our algorithm has several useful inherent properties. Below, we describe the most notable of those.

Universal threshold. The threshold τ is relative and does not depend on the size of the training corpus or the desired vocabulary. This is one of the advantages of our method compared to the main counterparts, such as [Cognetta et al.](#page-9-4) [\(2024\)](#page-9-4). Furthermore, the removals happen during training, yielding a vocabulary of the desired size that does not require any post-processing.

Variety of intermediate tokens. An intermediate token may be used to form more than one new token, as shown in Figure [2.](#page-3-0) Our algorithm handles these cases, removing the token only after there are few to no words it can be merged into.

Second chances. Any removed token may be added again if it becomes the most frequent at a later point in the order of merges. This is usually the case for tokens removed in the very beginning when the frequencies of new tokens are very high. For example, ("t", "he") is likely to be merged early in tokenizer training because "the" is a frequent word. Since the relative frequency of "he" is lower, "he" may be split into ("h", "e"). But as "he" is still a high-frequency word, it is likely to be merged again. If a previously removed token is restored, it is re-activated to keep its original place in the list of merges. This is essential to the merge order during tokenization.

4 Machine Translation Experiments

To evaluate the downstream performance of our algorithm, we conduct several machine translation (MT) experiments. We train MT models for three translation directions: English–German (EN– DE), German–Estonian (DE–ET), and Ukrainian– Estonian $(UK–ET).²$ $(UK–ET).²$ $(UK–ET).²$ With this choice of language pairs, we aim to cover diverse MT tasks of varying difficulty. German and English are related languages and share the same script. This language pair represents an easier translation task. German and Estonian use the same script, but are much less closely related, belonging to different language families. Translation for this pair should be more difficult. Finally, Ukrainian and Estonian represent the most difficult translation pair in our experiments. These languages are not only distant but also use different scripts.

To train the EN–DE models, we use the training corpus from the WMT16 news translation task [\(Bo](#page-9-7)[jar et al.,](#page-9-7) [2016\)](#page-9-7), with newstest2016 corpus for evaluation. For DE–ET and UK–ET, we use the mixtures of parallel corpora assembled by [Ko](#page-10-11)[rotkova and Fishel](#page-10-11) [\(2024\)](#page-10-11). For the evaluations of

Table 1: Machine translation results with vocabulary size 8192 on newstest2016 set [\(Bojar et al.,](#page-9-7) [2016\)](#page-9-7) for EN–DE, and on FLORES-dev [\(Goyal et al.,](#page-10-12) [2022\)](#page-10-12) for DE–ET and UK–ET. For every threshold \mathcal{T} , we report BLEU [\(Papineni et al.,](#page-10-13) [2002\)](#page-10-13) and COMET [\(Rei et al.,](#page-11-16) [2020\)](#page-11-16) scores. The best scores are highlighted in bold. Other scores that are not statistically significantly different from the best are also highlighted in bold. If none of the scores are significantly better than the rest, nothing is highlighted. ${}^*\mathcal{T} = 1.0$ represents the baseline vanilla BPE without intermediate token removal.

outputs in Estonian, we use the development set of the FLORES benchmark [\(Goyal et al.,](#page-10-12) [2022\)](#page-10-12).

We test our method with several thresholds: 0.6, 0.7, 0.8, and 0.9. We did not consider lower thresholds as they would remove too many useful tokens. For the baseline, we chose vanilla BPE, which we obtained by training our PickyBPE with $\mathcal{T} = 1$ to ensure that the effects are not driven by implementation differences. We use the transformer-iwslt model from fairseq [\(Ott](#page-10-14) [et al.,](#page-10-14) [2019\)](#page-10-14) for all MT tasks. The architecture and training details can be found in Appendix [B.](#page-12-1)

For generation, we use beam search with beam size 5 in all our experiments. We use BLEU [\(Pa](#page-10-13)[pineni et al.,](#page-10-13) [2002\)](#page-10-13) from sacreBLEU [\(Post,](#page-11-17) [2018\)](#page-11-17) and COMET [\(Rei et al.,](#page-11-16) [2020\)](#page-11-16) scores for automatic evaluation. We compute paired t-Test with bootstrapping^{[3](#page-4-2)} to test for statistical significance on performance metrics [\(Koehn,](#page-10-15) [2004\)](#page-10-15).

 2 We also experiment with a different type of writing system on the example of Estonian–Chinese (ET–ZH). Results and discussion of these experiments are presented in Appendix [C.](#page-13-1)

³We evaluate 1000 bootstrap resamples and use t-Test with confidence level 0.95.

Smaller vocabularies. First, we conduct experiments on all three language pairs with a small vocabulary size of 8192. We chose such a restrictive setting to make sure all the tokens are sufficiently trained, as the relatively small training datasets we used (∼1–4M sentence pairs) do not necessitate large vocabularies [\(Sennrich and Zhang,](#page-11-18) [2019\)](#page-11-18). The results are presented in Table [1.](#page-4-3) Overall, the models trained with PickyBPE vocabulary performed comparably to the vanilla BPE, with at least one PickyBPE threshold significantly outperforming it for all three translation directions according to the COMET metric. COMET scores for the DE–ET experiment show that all PickyBPE models were better than the vanilla baseline.

Larger vocabularies. We also tested PickyBPE with larger vocabularies for the EN–DE task. We used two settings: separate vocabularies for input and output, and joint vocabularies. In both cases, we used total vocabulary sizes 16384, 32768, and 65536. The results for these experiments are presented in Table [2.](#page-5-1) As with the smaller vocabulary setting, we see models based on PickyBPE tokenization performing at least on par with the ones based on the vanilla BPE. In most experiments, our method brings downstream improvements, as shown by the values of the COMET metric. We also observe by the BLEU scores that for the largest vocabularies of sizes $32768 + 32768$ and 65536 the performance is generally worse than with the smaller vocabularies, regardless of the tokenization method. This is likely due to the volume of training data being insufficient for such a large vocabulary. However, in this setting PickyBPE still outperforms vanilla BPE according to COMET.

5 Under-Trained Tokens

We also test whether PickyBPE decreases the number of tokens likely to be under-trained. These tokens can be identified by looking for very low L^2 norm of the token embeddings [\(Land and Bar](#page-10-2)[tolo,](#page-10-2) [2024\)](#page-10-2). We plot L^2 norms for $\mathcal{T} = 0.9$ in Figure [3](#page-6-0) and those for the remaining thresholds in Appendix [D.](#page-13-2) There are two groups of low- L^2 norm tokens: the first is the low-frequency tokens, which can be seen in the lower left of Figure [3a.](#page-6-0) According to [Land and Bartolo](#page-10-2) [\(2024\)](#page-10-2), this might indicate under-training. There is also a group of the highestfrequency tokens with low L^2 norms (top left of Figure [3a\)](#page-6-0). We posit that these are general-purpose tokens that occur in a wide variety of contexts, and

Vocabulary	$\mathcal T$	BLEU (\uparrow)	COMET (1)
	$1.0*$	30.7 ± 0.7	0.431
8192	0.9	30.4 ± 0.7	0.431
$^{+}$ 8192	0.8	30.3 ± 0.7	0.430
	0.7	30.3 ± 0.7	0.430
	0.6	30.8 ± 0.7	0.432
	$1.0*$	31.1 ± 0.7	0.433
16384	0.9	31.1 ± 0.7	0.433
$\boldsymbol{+}$ 16384	0.8	31.0 ± 0.7	0.435
	0.7	31.4 ± 0.7	0.435
	0.6	31.1 ± 0.7	0.435
	$1.0*$	29.8 ± 0.7	0.418
32768	0.9	29.6 ± 0.8	0.428
32768	0.8	30.5 ± 0.7	0.430
	0.7	30.4 ± 0.7	0.430
	0.6	28.3 ± 0.8	0.416
	$1.0*$	31.1 ± 0.7	0.436
	0.9	31.2 ± 0.7	0.436
16384	0.8	30.9 ± 0.6	0.434
	0.7	31.1 ± 0.7	0.436
	0.6	31.3 ± 0.7	0.438
	$1.0*$	30.9 ± 0.7	0.435
	0.9	31.1 ± 0.7	0.434
32768	0.8	31.1 ± 0.7	0.437
	0.7	30.9 ± 0.7	0.436
	0.6	30.9 ± 0.7	0.431
	$1.0*$	28.5 ± 0.7	0.421
	0.9	28.4 ± 0.7	0.427
65536	0.8	28.6 ± 0.7	0.425
	0.7	28.0 ± 0.7	0.416
	0.6	28.8 ± 0.7	0.420

Table 2: Machine translation results on EN–DE newstest2016 set [\(Bojar et al.,](#page-9-7) [2016\)](#page-9-7) with larger vocabularies: 8192, 16384, and 32768 for each language separately, and joint vocabularies of sizes 16384, 32768, and 65536. For every threshold $\mathcal T$, we report BLEU [\(Pa](#page-10-13)[pineni et al.,](#page-10-13) [2002\)](#page-10-13) and COMET [\(Rei et al.,](#page-11-16) [2020\)](#page-11-16) scores. The best scores are highlighted in bold. Other scores that are not statistically significantly different from the best are also highlighted in bold. If none of the scores are significantly better than the rest, nothing is highlighted. ${}^*\mathcal{T} = 1.0$ represents the baseline vanilla BPE without intermediate token removal.

thus their representations are less specific. It has long been observed that high-frequency words are

(a) PickyBPE tokens when $\mathcal{T} = 1.0$. The tokens that are present when $\mathcal{T} = 1.0$ but removed when $\mathcal{T} = 0.9$ (orange) are generally infrequent and have low L^2 embedding norms, thus the majority of them are likely to be under-trained [\(Land](#page-10-2) [and Bartolo,](#page-10-2) [2024\)](#page-10-2).

(b) PickyBPE tokens when $\mathcal{T} = 0.9$. The tokens that are present when $\mathcal{T} = 0.9$ but not when $\mathcal{T} = 1.0$ (pink) have frequencies and L^2 norms of the embeddings close to the blob center and thus are less likely to be under-trained [\(Land and](#page-10-2) [Bartolo,](#page-10-2) [2024\)](#page-10-2).

Figure 3: Input embedding vectors for PickyBPE tokens with (a) $\mathcal{T} = 1$ and (b) $\mathcal{T} = 0.9$ for English vocabularies of size 16384 in EN–DE experiments with separate vocabularies. For each token we compute its probability in the training corpus (y-axis), and the L^2 norm of its embedding vector in the trained model (x-axis).

Figure 4: Token frequency distributions for English vocabularies of size 16384 in EN–DE experiments with separate vocabularies for input and output. The left tail becomes less heavy as we decrease the threshold.

vs vanilla BPE τ ⁺ unique tokens vs vanilla BPE + post-trimming 0.9 $168 (2.1\%)$ $115 (1.4\%)$ 0.8 391 (4.8%) 248 (3.0%) 0.7 625 (7.6%) 393 (4.8%) 0.6 869 (10.6%) 588 (7.2%) Table 3: Comparison of tokens from PickyBPE and

unique tokens

unique tokens

vanilla BPE for joint EN–DE vocabularies of size 8192. For each threshold \mathcal{T} , we report the number of tokens that are present in the PickyBPE but not in the vanilla BPE ($\mathcal{T} = 1$) vocabulary with and without lowfrequency token trimming on post-processing.

more likely to have more senses, *i.e.*, meanings [\(Zipf,](#page-12-2) [1945\)](#page-12-2), and thus be more general-purpose.

A large portion of tokens removed by PickyBPE (Figure [3a\)](#page-6-0) are likely to become under-trained. By contrast, the new tokens added by PickyBPE (Fig-ure [3b\)](#page-6-0) have higher L^2 norms and higher probability of occurrence. The high-frequency general tokens are not removed by PickyBPE. We argue that PickyBPE reduces the likelihood of under-trained tokens and thus the risks associated with them, such as increased hallucinations.

We also find that as we lower the threshold for PickyBPE, there is a decrease in the left tail of the token frequency distribution, which represents the low-frequency tokens (Figure [4\)](#page-6-1). Trimming methods that involve an absolute frequency cutoff, such as the one used by [Cognetta et al.](#page-9-4) [\(2024\)](#page-9-4), would completely eliminate the left tail and leave an abrupt drop in the distribution. We observe that PickyBPE preserves the overall distribution and does not eliminate the left tail. This shows that PickyBPE is fundamentally different from posttraining trimming of low-frequency tokens.

Table [3](#page-6-2) shows the difference in the number of tokens present in the PickyBPE but not in the vanilla BPE vocabulary obtained with and without posttrimming. By post-trimming we mean training the vanilla BPE to have a larger vocabulary with further trimming of low-frequency tokens to achieve the desired vocabulary size. To obtain vocabularies

Table 4: Tokenizer evaluation on EN–DE tokenizers with joint vocabularies of size 8192. Compression is reported as corpus token counts of the newstest2016 set relative to the vanilla BPE. 1 indicates the same compression rate. We report the proportion of word-initial tokens out of dropped tokens (the ones present in vanilla BPE, but not in PickyBPE), added tokens (the ones present in PickyBPE, but not in vanilla BPE), and out of the whole vocabulary along with the mean token length in characters. ${}^*\mathcal{T} = 1.0$ represents vanilla BPE.

of equal sizes for a fair comparison, we train the initial vanilla BPE tokenizer so that the number of additional tokens reaches the number of replaced tokens from the corresponding PickyBPE tokenizer. Through the differences in numbers of replaced tokens, we show that PickyBPE is not simply a different implementation of the post-trimming akin to [Cognetta et al.](#page-9-4) [\(2024\)](#page-9-4), but leads to a fundamentally different resulting vocabulary.

6 Features of PickyBPE

Text Compression. Text compression is generally considered to be an important aspect of tokenizer evaluation [\(Gallé,](#page-9-5) [2019;](#page-9-5) [Goldman et al.,](#page-10-9) [2024\)](#page-10-9), and language models that compress more have been shown to perform better [\(Liang et al.,](#page-10-8) [2023;](#page-10-8) [Goldman et al.,](#page-10-9) [2024\)](#page-10-9). We use *corpus token count* (CTC; [Schmidt et al.,](#page-11-19) [2024\)](#page-11-19) to measure compression. CTC, also called sequence length, is the number of tokens needed to represent a given text. The fewer tokens are needed, the better the compression.

Table [4](#page-7-1) shows the changes in compression as a percentage relative to the tokenizer of the same vocabulary size with a threshold of 1, all for EN– DE vocabularies of size 8192. We report additional compression rates in Appendix [F.](#page-13-3) We find that PickyBPE shows no loss in compression. This is an improvement over the method in [Cognetta](#page-9-4) [et al.](#page-9-4) [\(2024\)](#page-9-4), which shows worse compression after vocabulary trimming.

Token Qualities. In addition to the above metrics, we compare the tokens themselves. One quality of interest is the proportion of word-initial tokens, which are stored in the tokenizer with an underscore at the beginning to represent a space

character. [Yehezkel and Pinter](#page-12-3) [\(2023\)](#page-12-3) also notice that their trimming procedure leads to an increased number of word-initial tokens.

In Table [4,](#page-7-1) we also report the percentage of wordinitial tokens among the added and removed tokens as well as overall proportions for the EN–DE vocabulary of size 8192. We report results for the other experiments in Appendix [G.](#page-15-0) We find that dropped tokens are far less likely to be word-initial than added tokens. Therefore, PickyBPE is adding more word-initial tokens than it is removing. As the threshold is lowered, we see slightly fewer wordinitial tokens added to the vocabulary. This might be due to the intensive removals happening with lower thresholds. In the overall rates of word-initial tokens, we see a slight increase as $\mathcal T$ goes down.

Upon inspection of the added tokens, we see that many of the word-initial tokens are also complete words, for example _renovated, _overcoat, _cognition, and _unconventional. Increased rates of word-initial tokens may be indicative of improved token quality.

Many of the tokens removed by PickyBPE were intermediate, much like entucky (Figure [1\)](#page-0-1). These tokens are relatively long and only occur in the context of a longer token that is also present in the vocabulary. Often, these tokens are missing only one or two characters compared to the full word. We find word-initial and word-medial intermediate tokens, *e.g.*, _Chicag, _algorith, roprietary, omenclature (*cf.* 'Chicago', 'algorithm', 'proprietary', 'nomenclature').

Following [Bostrom and Durrett](#page-9-2) [\(2020\)](#page-9-2), we also measure mean token length. They argue that longer mean token length is associated with gold-standard morphologically-aligned tokenization, and thus

		$CTC(\downarrow)$	$%$ Word-	Mean
Method	EN	DE.	initial $($ ^{$\dagger)$}	len (\uparrow)
Unigram	1.143	1.124	75.6	7.73
$\mathcal{T}=1.0$	1.000	1.000	72.2	6.85
$\mathcal{T}=0.9$	0.997	0.998	72.8	6.88
$\mathcal{T}=0.8$	0.996	0.998	73.2	6.91
$\mathcal{T}=0.7$	0.994	0.997	73.6	6.94
$\mathcal{T}=0.6$	0.992	0.996	73.9	6.95

Table 5: Comparing PickyBPE and Unigram [\(Kudo,](#page-10-6) [2018\)](#page-10-6) tokenizers on joint EN–DE vocabularies of size 32768. We report compression as corpus token counts (CTC) on the newstest2016 set relative to those of the vanilla BPE ($\mathcal{T} = 1.0$), percentage of word-initial tokens, and mean token length in characters (denoted in the table by "Mean len").

with better token quality. Additionally, longer tokens on average will lead to increased compression, as a text of a fixed length can be represented with fewer longer tokens. We find that the mean token length slightly, but consistently, increases as we lower the IoS threshold (see Table [4\)](#page-7-1). We report additional mean token length results in Appendix [H.](#page-15-1)

We also compare PickyBPE with Unigram tokenization in Table [5.](#page-8-0) Unigram tokenization seems to yield longer tokens with a higher proportion of word-initial tokens. However, it drastically worsens the compression. We hypothesize that Unigram adds many meaningful full-word tokens which are not optimal for the text compression under the restriction of the vocabulary size.

7 Discussion

We provide a series of experiments that illustrate key properties of PickyBPE. To put these results into perspective, we wish to reiterate two core aspects of the provided experiments: first, there is no universal methodology that could assess tokenizer quality; second, the inefficiencies associated with under-trained tokens discussed by [Land and](#page-10-2) [Bartolo](#page-10-2) [\(2024\)](#page-10-2) depend on the size of vocabulary relative to the size of training data.

Evaluating tokenizers. It is not always clear how to best compare different tokenizers [\(Zouhar et al.,](#page-12-4) [2023\)](#page-12-4). One approach is training models for each tokenizer and evaluating downstream performance, *e.g.*, [Goldman et al.](#page-10-9) [\(2024\)](#page-10-9). However, these results may be driven by confounding factors, such

as differences in compression leading to the model effectively being trained on less text [\(Petrov et al.,](#page-10-1) [2023\)](#page-10-1), and downstream results may also be taskspecific. The second general approach to evaluating tokenizers is to evaluate some quality of the tokenizer's output such as compression, similarity of tokenizer boundaries to morphological boundaries [\(Hofmann et al.,](#page-10-16) [2021\)](#page-10-16), or cognitive plausibility of tokens [\(Beinborn and Pinter,](#page-9-8) [2023\)](#page-9-8). There is no consensus about which metric(s) provide the best overall estimation of tokenizer quality.

Role of under-trained tokens. We achieved better or equal performance on machine translation with small vocabularies compared to the vanilla BPE, which suggests that removing under-trained tokens benefits downstream performance. With larger vocabularies, we also saw improvement from our method judging by the values of the COMET metric. However, the largest vocabulary sizes we experimented with were too large for the rather small datasets we used, which led to degraded overall performance regardless of the tokenizer choice. To see the fair improvement with larger vocabulary sizes, one might consider testing PickyBPE as a tokenizer for an LLM, where vocabulary size will be significantly scaled up together with the size of the training data. In this scenario, we also expect to see the benefits of removing under-trained tokens, which were investigated by [Land and Bartolo](#page-10-2) [\(2024\)](#page-10-2) specifically on the example of LLMs. We leave this exploration for future work.

8 Conclusion

In this paper, we propose PickyBPE, a novel tokenization algorithm that refines the vocabulary during tokenizer training by removing intermediate tokens. Our machine translation experiments show that this algorithm either matches or surpasses the downstream performance shown by vanilla BPE on the same data, which we can extrapolate to larger vocabularies and data given enough training. Our method also mitigates the issue of under-trained tokens, efficiently removing them during tokenizer training, and improves token quality and text compression, filling the freed vocabulary space with higher-frequency and higher-quality tokens. These factors suggest that PickyBPE can be considered for larger models, *e.g.*, LLMs, to improve downstream performance and safety and avoid undesired behavior, *e.g.*, hallucinations.

9 Limitations

PickyBPE behavior depends on the choice of threshold $\mathcal T$. Even though the threshold is relative and mostly intuitive in use, one must consider that with lower thresholds the probability of eliminating useful tokens grows and the behavior becomes less stable. Therefore, it is important to start with safer larger thresholds, analyzing the tokenization using token quality measures.

In this paper, the only downstream task we evaluate our models on is translation. Training a larger language model and evaluating it on other downstream tasks may show different patterns. This may allow us to better understand the contribution of PickyBPE as well as its potential drawbacks.

[Rust et al.](#page-11-0) [\(2021\)](#page-11-0) show that different tasks have variable correlation with tokenizer evaluations like fertility. To the best of our knowledge, there is not enough empirical work to determine which tasks would be most informative for evaluating tokenizer quality. This is an important area for future work.

Our experiments are also limited to a relatively small set of languages. We selected pairs of languages that were typologically varied and used different writing systems, however, most of the languages are spoken in Europe. Our experiments with Chinese did not show any improvements in performance from PickyBPE, which we argue is due to the inherent properties of the writing system (see Appendix [C](#page-13-1) for discussion). In future work, a broader sample of languages could be covered to verify the consistency of the observed trends.

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A Inference options

PickyBPE inference strictly follows the training order of events and executes merges and removals in the same chronological order (Algorithm [2\)](#page-2-2). Concurrent works use a different approach to inference: the input text is first tokenized with a vanilla BPE tokenizer using both active and removed tokens and then the low-frequency [\(Cognetta et al.,](#page-9-4) [2024\)](#page-9-4) or scaffold [\(Lian et al.,](#page-10-10) [2024\)](#page-10-10) tokens are split into the shortest available sequences of valid tokens. The latter approach is suboptimal, as the training events order is likely to be broken.

For example, imagine the token sequence [t, h, e, r, e] on a certain training step. Tokens (h, e) are merged into he (event e_{i_1}). The sequence becomes [t, he, r, e]. Later, token he becomes useless and is removed (event $e_{i_2}, i_2 > i_1$). Thus, the sequence returns to $[t, h, e, r, e]$. It can happen now that tokens (e, r) are merged into a new token er (event $e_{i_3}, i_3 > i_2$). The resulting tokenization is [t, h, er, e]. PickyBPE tokenization will follow event order $e_{i_1},...,e_{i_2},...,e_{i_3}$ and result in [t, h, er, e]. The tokenization when the tokens are removed after the vanilla BPE process will first achieve [t, he, r, e], as it will execute all the available merges. In a simplified example, there are no merges to perform after this step, and the algorithm will move to the removals phase: he will be split, and the resulting tokenization will become [t, h, e, r, e]. Therefore, er will not be merged, as it happened after the removal and contains a part of the removed token.

When repeated several times, the described issue may lead to undesired tokenization results and compromise compression. In Table [6,](#page-12-5) we compare the compression rates of the two methods. The

τ	BPE inference with post-removal	PickyBPE inference
1.0	1.000	1.000
0.9	0.998	0.997
0.8	0.998	0.996
0.7	1.000	0.994
0.6	1.005	0.992

Table 6: Comparison of compression rates (\downarrow) for the vanilla BPE inference followed by splitting undesired tokens and PickyBPE inference by events order for EN– DE vocabularies of size 32768. The compression rates are shown for English.

Parameter	Value
Encoder layers	6
Decoder layers	6
Embedding dim	512
Hidden dim	1024
Attention heads	4
Max tokens in a batch	4096
Optimizer	Adam
Weight decay	$1e-4$
Learning rate (LR)	5e-4
LR Scheduler	inverse sqrt
Warmup steps	4000
Warmup strategy	linear
Precision	fp16

Table 7: transformer-iwslt architecture and training details configuration from fairseq [\(Ott et al.,](#page-10-14) [2019\)](#page-10-14).

compression issues become more pronounced with lower thresholds as more tokens are removed.

Apart from the described inference methods, PickyBPE can use any inference method requiring a fixed vocabulary: for example, greedy left-toright decoding [\(Wu et al.,](#page-11-10) [2016\)](#page-11-10) or recently introduced PathPiece [\(Schmidt et al.,](#page-11-19) [2024\)](#page-11-19).

B Training details

Table [7](#page-12-6) shows the main model and training hyperparameters we used in every machine translation experiment. We trained models with small vocabularies of size 8192 for 20 epochs and the models with larger vocabularies for 25 epochs, each on a single NVIDIA A40 GPU (driver version 555.42.02, CUDA version 12.5).

C Experiments with Chinese

We separately applied PickyBPE to the Chinese data to test the algorithm on a language with a completely different writing system. We used the ET– ZH mixtures of parallel corpora assembled by [Ko](#page-10-11)[rotkova and Fishel](#page-10-11) [\(2024\)](#page-10-11) for training and the development set of the FLORES benchmark [\(Goyal et al.,](#page-10-12) [2022\)](#page-10-12) for evaluation. Because there were over 11,000 unique characters in the Chinese dataset alone, the smallest vocabulary size we could use was 16384, and we used the vocabulary of size 16384 separately for input and output. The results for these experiments are presented in Table [8.](#page-13-4)

The Estonian–Chinese experiment was the only language pair to show no improvement in any benchmark for any threshold setting for PickyBPE compared to vanilla BPE. Crucially, however, there was no drop in performance, but rather performance was stable across all conditions. We argue this is due to inherent language-specific differences introduced by the orthography of Chinese, which meant that our experiment is not able to show any benefits of PickyBPE with Chinese. After adding all individual characters and letters for Chinese and Estonian, there were only a small number of vocabulary items available for the tokenizer to create with merges. PickyBPE mostly operates by removing less frequent merges, which would tend to occur further down in the merge list. In this experimental setting, the tokenizer does not learn merges that would otherwise be later in the merge list, because of the relatively small vocabulary size for Chinese.

D Under-trained tokens inspection

Figure [5](#page-14-0) shows examples of token embedding norm distributions for thresholds 0.6, 0.7, and 0.8. As we lower the threshold, the proportion of removed tokens gets larger. However, there is no change in their nature: we remove mostly infrequent tokens and add more frequent tokens with higher norms that are close to the overall distribution.

E Number of Added/Removed Tokens

Tables [9,](#page-13-5) [10,](#page-15-2) and [11,](#page-15-3) report the number of added/removed tokens for each tokenizer. This is the number of tokens that are present in PickyBPE but not in the corresponding vanilla BPE tokenizer. With the growth of the vocabulary size, the overall partition of such tokens is maintained in a similar manner. It generally does not surpass 10% with the most radical threshold we use (0.6).

Experiment	τ		BLEU (\uparrow) COMET (\uparrow)
	10^*	22.3 ± 0.9	0.428
	0.9	22.0 ± 0.8	0.428
ET-ZH	0.8	22.0 ± 0.9	0.427
	0.7	22.0 ± 0.9	0.428
	06	$22.0 + 0.8$	0.426

Table 8: Machine translation results on FLORESdev [\(Goyal et al.,](#page-10-12) [2022\)](#page-10-12) for the ET–ZH language pair. For every threshold T , we report BLEU [\(Papineni et al.,](#page-10-13) [2002\)](#page-10-13) and COMET [\(Rei et al.,](#page-11-16) [2020\)](#page-11-16) scores on the translation task. For both metrics, the differences in scores were found statistically insignificant. ${}^*{\cal T} = 1.0$ represents the baseline vanilla BPE without intermediate token removal.

Table 9: Numbers of added (removed) tokens at different thresholds for the EN–DE tokenizers used for the translation experiments.

F Compression

In Tables [12,](#page-15-4) [13,](#page-15-5) and [14,](#page-15-6) we show compression metrics as corpus token counts (CTC) for PickyBPE tokenizers relative to the vanilla BPE. We notice that compression is most pronounced in smaller vocabularies, as for the sizes of the datasets that we used larger vocabularies have large redundancy and a larger partition of tokens is allowed to be unused. In each experiment, we compute the CTC metric on the corresponding test sets.

(a) PickyBPE tokens when $\mathcal{T} = 1.0$. The tokens that are present when $\mathcal{T} = 1.0$ but are removed when $\mathcal{T} = 0.8$ (orange) are generally infrequent and have low L^2 embedding norms, thus the majority of them are likely to be undertrained [\(Land and Bartolo,](#page-10-2) [2024\)](#page-10-2).

(c) PickyBPE tokens when $T = 1.0$. The tokens that are present when $\mathcal{T} = 1.0$ but are removed when $\mathcal{T} = 0.7$ (orange) are generally infrequent and have low L^2 embedding norms, thus the majority of them are likely to be undertrained [\(Land and Bartolo,](#page-10-2) [2024\)](#page-10-2).

(e) PickyBPE tokens when $\mathcal{T} = 1.0$. The tokens that are present when $\mathcal{T} = 1.0$ but are removed when $\mathcal{T} = 0.6$ (orange) are generally infrequent and have low L^2 embedding norms, thus the majority of them are likely to be undertrained [\(Land and Bartolo,](#page-10-2) [2024\)](#page-10-2).

(b) PickyBPE tokens when $\mathcal{T} = 0.8$. The tokens that are present when $\mathcal{T} = 0.8$ but not when $\mathcal{T} = 1.0$ (pink) have frequencies and L^2 norms of the embeddings close to the blob center and thus are less likely to be under-trained [\(Land and](#page-10-2) [Bartolo,](#page-10-2) [2024\)](#page-10-2).

(d) PickyBPE tokens when $\mathcal{T} = 0.7$. The tokens that are present when $\mathcal{T} = 0.7$ but not when $\mathcal{T} = 1.0$ (pink) have frequencies and L^2 norms of the embeddings close to the blob center and thus are less likely to be under-trained [\(Land and](#page-10-2) [Bartolo,](#page-10-2) [2024\)](#page-10-2).

(f) PickyBPE tokens when $\mathcal{T} = 0.6$. The tokens that are present when $\mathcal{T} = 0.6$ but not when $\mathcal{T} = 1.0$ (pink) have frequencies and L^2 norms of the embeddings close to the blob center and thus are less likely to be under-trained [\(Land and](#page-10-2) [Bartolo,](#page-10-2) [2024\)](#page-10-2).

Figure 5: Input embedding vectors for PickyBPE tokens with (a, c, e) $\mathcal{T} = 1.0$, (b) $\mathcal{T} = 0.8$, (d) $\mathcal{T} = 0.7$, and (f) $\mathcal{T} = 0.6$ for English vocabularies of size 16384 in EN–DE experiments with separate vocabularies. For each token we compute its probability in the training corpus (y-axis), and the L^2 norm of its embedding vector in the trained model (x-axis).

Vocabulary Size	Threshold	Added / Removed Tokens
	0.9	133
8192	0.8	313
	0.7	506
	06	718

Table 10: Numbers of added (removed) tokens at different thresholds for the DE–ET tokenizers used for the translation experiments.

Vocabulary Size	Threshold	Added / Removed Tokens
8192	0.9 0.8 0.7	107 255 446
	06	605

Table 11: Numbers of added (removed) tokens at different thresholds for the UK–ET tokenizers used for the translation experiments.

Vocabulary	Т		Compression (\downarrow)
size		English	German
	1.0	1.000	1.000
	0.9	0.997	0.996
8192	0.8	0.995	0.993
	0.7	0.994	0.991
	0.6	0.992	0.989
	1.0	1.000	1.000
	0.9	0.996	0.998
16384	0.8	0.994	0.996
	0.7	0.993	0.995
	0.6	0.991	0.993
	1.0	1.000	1.000
	0.9	0.997	0.998
32768	0.8	0.996	0.998
	0.7	0.994	0.997
	0.6	0.992	0.996
	1.0	1.000	1.000
	0.9	0.998	0.998
65536	0.8	0.997	0.998
	0.7	0.997	0.998
	0.6	0.996	0.997

Table 12: Compression for EN–DE tokenizers with different vocabulary sizes reported as corpus token counts (CTC) relative to the vanilla BPE ($\mathcal{T} = 1.0$).

Vocabulary		Compression (\downarrow)	
size		German	Estonian
	1.0	1.000	1.000
	0.9	0.998	0.998
8192	0.8	0.994	0.996
	0.7	0.991	0.993
	06	0.989	0.991

Table 13: Compression for DE–ET tokenizers with a vocabulary size of 8192. The scores are computed as corpus token counts (CTC) relative to the vanilla BPE $({\cal T}=1.0).$

Vocabulary		Compression (\downarrow)	
size		Ukrainian	Estonian
	1.0	1.000	1.000
	0.9	0.998	0.998
8192	0.8	0.996	0.996
	0.7	0.993	0.994
	06	0.992	0.993

Table 14: Compression for UK–ET tokenizers with a vocabulary size of 8192. The scores are computed as corpus token counts (CTC) relative to the vanilla BPE $({\cal T} = 1.0).$

G Word-Initial Tokens

In Tables [15,](#page-16-0) [16,](#page-16-1) and [17,](#page-16-2) we show the proportions of added and removed word-initial tokens for different vocabulary sizes and language pairs. By added tokens we mean the ones present in PickyBPE but not in vanilla BPE, and by removed tokens we mean the ones present in vanilla BPE but not in PickyBPE. In addition, we show the overall proportions of word-initial tokens in the corresponding tokenizers in Tables [18,](#page-16-3) [19,](#page-16-4) and [20.](#page-16-5)

H Token Length

In Tables [21,](#page-17-0) [22,](#page-17-1) and [23,](#page-17-2) we show mean token lengths over different vocabulary sizes that we used in the translation experiments. The token lengths are reported in characters.

Vocabulary			% Word-Initial Tokens
size	T	Dropped	Added
	0.9	43.8	65.5
	0.8	41.1	67.5
8192	0.7	42.0	66.9
	0.6	42.1	64.2
	0.9	43.9	69.6
16384	0.8	43.7	67.1
	0.7	45.3	68.1
	0.6	45.3	65.8
	0.9	46.7	73.3
32768	0.8	44.8	68.3
	0.7	47.5	68.5
	0.6	48.7	67.9
	0.9	50.6	74.6
65536	0.8	49.2	71.0
	0.7	51.5	69.9
	0.6	52.0	69.0

Table 15: Percent of word-initial tokens out of added and removed tokens for the EN–DE tokenizers. Added tokens are relative to the vanilla ($\mathcal{T} = 1.0$) tokenizer of the same vocabulary size and language pair.

Vocabulary	τ		% Word-Initial Tokens
size		Dropped	Added
	0.9	33.1	60.9
	0.8	32.3	63.3
8192	0.7	37.0	60.3
	0.6	40.4	58.4

Table 16: Percent of word-initial tokens out of added and removed tokens for the DE–ET tokenizers. Added tokens are relative to the vanilla ($\mathcal{T} = 1.0$) tokenizer of the same vocabulary size and language pair.

Vocabulary size		% Word-Initial Tokens	
		Dropped	Added
	0.9	31.8	73.6
8192	0.8	33.3	66.3
	0.7	37.4	61.8
	06	39.0	61.3

Table 17: Percent of word-initial tokens out of added and removed tokens for the UK–ET tokenizers. Added tokens are relative to the vanilla BPE ($\mathcal{T} = 1.0$) of the same vocabulary size and language pair.

Vocabulary Size	Threshold	$\%$ Word- Initial Tokens
	1.0	61.5
	0.9	61.9
8192	0.8	62.7
	0.7	63.3
	0.6	63.6
	1.0	68.0
	0.9	68.6
16384	0.8	69.2
	0.7	69.7
	0.6	70.0
	1.0	72.2
	0.9	72.8
32768	0.8	73.2
	0.7	73.6
	0.6	73.9
65536	1.0	75.2
	0.9	75.7
	0.8	76.1
	0.7	76.3
	0.6	76.6

Table 18: Overall proportion of word-initial tokens at different thresholds for the EN–DE tokenizers.

Vocabulary Size	Threshold	$%$ Word- Initial Tokens
8192	1.0 0.9 0.8 0.7 0.6	58.1 58.6 59.4 59.8 60.0

Table 19: Proportion of word-initial tokens at different thresholds for the DE–ET tokenizers.

Table 20: Proportion of word-initial tokens at different thresholds for the UK–ET tokenizers.

Vocabulary Size	Threshold	Mean Token Length (Chars) (\uparrow)
8192	1.0	5.38
	0.9	5.40
	0.8	5.44
	0.7	5.47
	0.6	5.50
16384	1.0	6.19
	0.9	6.21
	0.8	6.24
	0.7	6.26
	0.6	6.28
	1.0	6.85
	0.9	6.88
32768	0.8	6.91
	0.7	6.94
	0.6	6.95
65536	1.0	7.44
	0.9	7.46
	0.8	7.49
	0.7	7.51
	0.6	7.53

Table 21: Mean token length at different thresholds for the EN–DE tokenizers.

Vocabulary Size	Threshold	Mean Token Length (Chars) (\uparrow)
8192	1.0 0.9 0.8 0.7 06	5.35 5.38 5.40 5.41 5.42

Table 22: Mean token length at different thresholds for the DE–ET tokenizers.

Vocabulary Size	Threshold	Mean Token Length (Chars) (\uparrow)
8192	1.0 0.9 0.8 0.7 06	4.84 4.85 4.86 4.88 4.90

Table 23: Mean token length at different thresholds for the UK–ET tokenizers.