# Pruning via Merging: Compressing LLMs via Manifold Alignment Based Layer Merging

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#### Abstract

While large language models (LLMs) excel in many domains, their complexity and scale challenge deployment in resource-limited environments. Current compression techniques, such as parameter pruning, often fail to effectively utilize the knowledge from pruned parameters. To address these challenges, we propose Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA), a novel approach that uses manifold learning and the Normalized Pairwise Information Bottleneck (NPIB) measure to merge similar layers, reducing model size while preserving essential performance. We evaluate MKA on multiple benchmark datasets and various LLMs. Our findings show that MKA not only preserves model performance but also achieves substantial compression ratios, outperforming traditional pruning methods. Moreover, when coupled with quantization, MKA delivers even greater compression. Specifically, on the MMLU dataset using the Llama3-8B model, MKA achieves a compression ratio of 43.75% with a minimal performance decrease of merely 2.82%. The proposed MKA method offers a resource-efficient and performance-preserving model compression technique for LLMs. We make our code available at [https://github.](https://github.com/SempraETY/Pruning-via-Merging) [com/SempraETY/Pruning-via-Merging](https://github.com/SempraETY/Pruning-via-Merging)

### 1 Introduction

Large Language Models (LLMs), such as GPT-4 [\(OpenAI et al.,](#page-10-0) [2024\)](#page-10-0), Llama-3<sup>[2](#page-0-1)</sup>, Llama-2 [\(Tou](#page-10-1)[vron et al.,](#page-10-1) [2023\)](#page-10-1) and Mistral [\(Jiang et al.,](#page-9-0) [2024\)](#page-9-0), have demonstrated remarkable proficiency in language understanding and generation. These models, with billions of parameters trained on trillions of tokens, can handle complex tasks and exhibit emergent abilities [\(Brown et al.,](#page-8-0) [2020;](#page-8-0) [Chowdhery](#page-8-1)

[et al.,](#page-8-1) [2023\)](#page-8-1). While these models have achieved unprecedented success, their growing complexity and scale have brought to the fore significant challenges in terms of computational resources, memory requirements, and energy consumption [\(Bender et al.,](#page-8-2) [2021;](#page-8-2) [Bommasani et al.,](#page-8-3) [2021\)](#page-8-3), raising concerns about their sustainability.

To mitigate these challenges, researchers have developed various model compression techniques in LLM to reduce its parameter size while preserving performance [\(Cheng et al.,](#page-8-4) [2017;](#page-8-4) [Deng et al.,](#page-9-1) [2020;](#page-9-1) [Ganesh et al.,](#page-9-2) [2021;](#page-9-2) [Zhu et al.,](#page-11-0) [2023;](#page-11-0) [Yang](#page-11-1) [et al.,](#page-11-1) [2024\)](#page-11-1). These techniques can be roughly categorized into two main mainstreams [\(Men et al.,](#page-9-3) [2024\)](#page-9-3): quantization [\(Gholami et al.,](#page-9-4) [2021;](#page-9-4) [Li et al.,](#page-9-5) [2024;](#page-9-5) [Dettmers et al.,](#page-9-6) [2022;](#page-9-6) [Gong et al.,](#page-9-7) [2024;](#page-9-7) [Li et al.,](#page-9-5) [2024\)](#page-9-5) and pruning [\(LeCun et al.,](#page-9-8) [1989;](#page-9-8) [Han et al.,](#page-9-9) [2016;](#page-9-9) [Gupta and Agrawal,](#page-9-10) [2022;](#page-9-10) [Ma](#page-9-11) [et al.,](#page-9-11) [2023a\)](#page-9-11). Quantization based methods aid in the reduction of the memory consumption of weights, activations, and KV caches by using the low-precision values with fewer bits instead of the high-precision values. However, the acceleration benefits of quantization are seriously dependent on hardware support [\(Tao et al.,](#page-10-2) [2023\)](#page-10-2) and sometimes require additional fine-tuning to maintain performance [\(Dettmers et al.,](#page-9-12) [2023;](#page-9-12) [Men et al.,](#page-9-3) [2024\)](#page-9-3). Compared to quantization, pruning, especially structural pruning [\(Li et al.,](#page-9-13) [2017\)](#page-9-13), eliminates redundant LLM's parameters to decrease the overall parameter count, and can be applied directly to a trained LLM without retraining and is generally more hardware-friendly than quantization approaches. While effective, pruning usually risks losing valuable model structures and determining how to prune the LLM with minimal disruption to the origin remains an unsolved problem [\(Ma et al.,](#page-9-14) [2023b\)](#page-9-14).

To tackle this issue head-on, we delve into the realm of model merging [\(Wortsman et al.,](#page-10-3) [2022\)](#page-10-3), a powerful technique that seamlessly weaves to-

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<span id="page-0-1"></span><sup>2</sup> <https://github.com/meta-llama/llama3>

<span id="page-1-0"></span>

Figure 1: Manifold-Based Knowledge Alignment and Layer Merging (MKA) framework consists of two main components: (1) The left side illustrates manifold learning for LLM knowledge extraction, where layer activations are transformed into low-dimensional manifolds using the Diffusion Kernel algorithm. (2) The right side depicts the similarity-based layer merging process, employing the NPIB metric to identify layers with aligned knowledge.

gether the strengths and knowledge of multiple models, creating a robust and efficient aggregation. This technique, through averaging the weights of multiple models with the same architecture, can retain essential features without significant additional resources [\(Liu et al.,](#page-9-15) [2024;](#page-9-15) [Wan et al.,](#page-10-4) [2024\)](#page-10-4). Furthermore, by offsetting the biases and errors of individual models, model merging often leads to greatly improved performance [\(Li et al.,](#page-9-16) [2023\)](#page-9-16). Additional, the number of models in the merging process can be gradually and naturally reduced. However, such a useful technology are limited to merging between models currently, and few studies pay attention on merging the same internal structures within a model.

This raises the question of whether model compression could be achieved by reducing the total number of layers through the progressive aggregation of knowledge between layers. To answer this question, we introduce Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA) in this paper. MKA combines manifold learning and layer merging to preserve essential information while significantly reducing LLM parameter size. As illustrated in Figure [1,](#page-1-0) our method mainly comprises two primary components:

*Manifold Learning for LLM Knowledge:* We employ manifold learning techniques to align knowledge across layers by extracting layer activations from a LLM and applying the Diffusion Kernel algorithm [\(Tenenbaum et al.,](#page-10-5) [2000\)](#page-10-5) to learn low-dimensional manifold representations. This approach captures the nonlinear structure in the activation and achieves dimensionality reduction while preserving important activation features, enabling more effective comparison of knowledge patterns across different layers.

*Similarity Alignment Layer Merging:* Following manifold learning, we use the Normalized Pairwise Information Bottleneck (NPIB) measure [\(Tishby et al.,](#page-10-6) [2000\)](#page-10-6) to construct a similarity matrix that quantifies the similarity between layers by maximizing their mutual information while considering the entropy of each layer. Based on this similarity matrix, we select the most similar layer pairs for merging.

To rigorously validate the effectiveness of MKA, we conduct extensive empirical evaluations on a diverse array of benchmark datasets, like MMLU and PIQA, and a wide range of state-of-the-art large language models, including Llama-3 series with 8B and 70B parameters, Llama-2 series with 7B and 13B parameters, and Mixtral-7B. Our experimental results indicate that MKA can maintain good performance while achieving a significant compression ratio, outperforming existing pruning methods and achieving even greater compression when combined with quantization. For example, on the MMLU dataset with Llama3-8B, MKA can achieve a compression ratio of 43.75% with only a 2.82% performance drop.

In summary, the main contributions of this paper

are as follows:

- We introduce MKA, an innovative model compression technique that leverages manifold learning to align and integrate knowledge across layers, achieving significant reductions in model size while preserving performance.
- We develop a manifold-based knowledge alignment approach, utilizing the Diffusion Kernel and Normalized Pairwise Information Bottleneck (NPIB) to effectively capture and align similarities between layers in the parameter space.
- We validate the efficacy of MKA through comprehensive experiments on multiple benchmark datasets and a variety of large language models, demonstrating its capability to achieve substantial compression without compromising model performance.

# 2 Manifold-Based Knowledge Alignment and Layer Merging

Our MKA method relies on the redundancy present in the latter layers of post-training LLMs [\(Gromov](#page-9-17) [et al.,](#page-9-17) [2024\)](#page-9-17). By merging layers with high inputoutput similarity from back to front, we maintain the model's performance while reducing its size. In this section, we first describe the extraction and dimensionality reduction processes for the intermediate states, as high-dimensional intermediate states are challenging to analyze. Then, we propose our layer merging method based on similarity alignment, which aims to maintain performance by aligning intermediate states through merging techniques.

#### 2.1 Manifold Learning for LLM Knowledge

To effectively align knowledge across LLM's layers, MKA employs manifold learning techniques that can capture the intricate nonlinear dependencies within the LLM's internal structure. This approach allows us to compare and align layer activations in a meaningful way, preserving essential information while reducing model complexity.

The process begins with the extraction of layer activations  $H^l$  from a LLM on the dataset  $\omega$  . These activations represent the outputs of each layer given a set of input samples, encapsulating the knowledge learned at different stages. To transform these highdimensional activations into a lower-dimensional space that preserves their essential features and geometric structure, we apply the Diffusion Kernel algorithm [\(Coifman and Lafon,](#page-8-5) [2006\)](#page-8-5). Here are

the key steps involved in this process:

Extracting Layer Activations: For each layer l, we extract the activations  $H<sup>l</sup>$  given input samples. These activations  $H<sup>l</sup>$  are computed using the following equation:

$$
\mathbf{H}^{l} = \text{LayerNorm}\left(\mathbf{H}^{l-1} + \text{MultiHead}\left(\mathbf{H}^{l-1}\right)\right)
$$

$$
+ \text{FeedForward}\left(\mathbf{H}^{l-1}\right) \tag{1}
$$

Constructing the Pairwise Distance Matrix: Next, we calculate the pairwise Euclidean distance matrix D for the activations  $H^l$ . This matrix captures the distances between all pairs of activations, serving as the basis for the manifold learning process.

Applying the Diffusion Kernel: We apply the Diffusion Kernel to transform the distance matrix D into low-dimensional manifold representations  $\Phi_i$ , capturing the intrinsic geometric structure of the data. The kernel function smooths the data, emphasizing the intrinsic geometric structure:

$$
\mathbf{E} = \text{EigVectors}_{d} \left( \text{Diag} \left( \sum_{j=1}^{i} e^{-\left( \frac{\|\mathbf{H}^{i} - \mathbf{H}^{j}\|^{2}}{\sigma_{K}} \right)^{0.5}} \right) - e^{-\left( \frac{\|\mathbf{H}^{i} - \mathbf{H}^{j}\|^{2}}{\sigma_{K}} \right)^{0.5}} \right)
$$
(2)

where  $\sigma_K$  is the kernel bandwidth parameter, and  $EigVectors_d$  refers to the eigenvectors corresponding to the d smallest eigenvalues of the Laplacian matrix L. This transformation captures the essential features and relationships within the activations, enabling effective comparisons across different layers.

#### 2.2 Similarity-based Layer Merging

Building upon the manifold learning representations, MKA employs a similarity-based layer merging approach to identify and fuse layers with highly aligned knowledge. By quantifying the similarity between layers using the Normalized Pairwise Information Bottleneck (NPIB) [\(Tishby et al.,](#page-10-6) [2000\)](#page-10-6) metric, we can determine which layers are most suitable for merging. This process allows us to reduce model size, improve inference speed, and decrease GPU memory consumption.

The layer merging process involves several key steps. First, we construct a similarity matrix using the NPIB metric to compare the knowledge patterns across layers. Next, we introduce an adaptive Algorithm 1 Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA) 1: **Input:** LLM M with Layers  $L_1, L_2, \ldots, L_N$ , Layer Parameters  $\Theta = \theta_1, \theta_2, \ldots, \theta_N$ , Dataset  $\omega$ 2: **Output:** Compressed Model  $\mathcal{M}^*$  with Aligned Knowledge<br>3:  $\mathcal{H} \leftarrow$  ExtractActivations( $\mathcal{M}, \omega$ )  $\triangleright$  Extract  $\triangleright$  Extract activations for each layer on dataset  $\omega$ 4: D ← ComputePairwiseDistances(H) ▷ Compute pairwise Euclidean distance matrix of activations 5: E ← DiffusionKernel(D, σK) ▷ Apply diffusion kernel for manifold learning 6:  $S \leftarrow \text{ComputeNPIB}(\mathbf{E})$ <br>
7:  $\Omega \leftarrow \text{SortLayersBySimilarity}(\mathcal{S})$   $\triangleright$  Sort layers by similarity for merging ⊳ Sort layers by similarity for merging 8: while  $|\Omega| > 1$  do<br>9:  $(L_i, L_j) \leftarrow S_0$  $(L_i, L_i) \leftarrow$  SelectTopLayerPair $(\Omega)$ ⊳ Select top-ranked layer pair based on similarity 10:  $\lambda_m \leftarrow \text{ComputeMergingRatio}(\mathcal{S}, L_i, L_j)$ <br>11:  $\theta_m \leftarrow \lambda_m \cdot \theta_i + (1 - \lambda_m) \cdot \theta_i$  $\triangleright$  Compute adaptive merging ratio 11:  $\theta_m \leftarrow \lambda_m \cdot \theta_i + (1 - \lambda_m) \cdot \theta_j$   $\triangleright$  Merge layer parameters<br>12:  $L_m \leftarrow$  MergeLayer $(L_i, L_i, \theta_m)$   $\triangleright$  Create merged layer using the merged parameters 12:  $L_m \leftarrow \text{MergeLayer}(L_i, L_j, \theta_m)$ <br>13:  $\mathcal{M} \leftarrow \text{ReplaceLayer}(\mathcal{M}, L_i, L_j)$  $\triangleright$  Create merged layer using the merged parameters 13:  $M \leftarrow \text{ReplaceLayer}(\mathcal{M}, L_i, L_j, L_m)$ <br>14:  $\Omega \leftarrow \text{UpdateLayerList}(\Omega, L_i, L_i, L_m)$  $\triangleright$  Update model with the merged layer  $\Omega \leftarrow \text{UpdateLayerList}(\Omega, L_i, L_j, L_m)$  $\triangleright$  Update layer list with the new merged layer 15: end while

$$
\underline{\mathbf{16: return} \mathcal{M}}
$$

weight allocation function to determine the optimal merging ratio for each pair of layers, ensuring that the merged layer retains the most critical features. Finally, we fuse the parameters of the selected layers using the weighted sum and update the model architecture accordingly.

Constructing the Similarity Matrix: To identify layers suitable for merging, we first construct a similarity matrix  $S$  using the Normalized Pairwise Information Bottleneck (NPIB) metric. NPIB quantifies the shared information between layers while normalizing their individual entropies, providing an ideal measure for comparing knowledge patterns across layers:

$$
S_{ij} = \text{NPIB}(\mathbf{E}_i, \mathbf{E}_j)
$$
  
= 
$$
\frac{\sum_{x \in \mathbf{E}_i} \sum_{y \in \mathbf{E}_j} p(x, y) \log \frac{p(x, y)}{p(x)p(y)}}{\sqrt{\sum_{x \in \mathbf{E}_i} p(x) \log p(x) \cdot \sum_{y \in \mathbf{E}_j} p(y) \log p(y)}}
$$
(3)

where  $p(x, y)$  denotes the joint probability distribution of  $\mathbf{E}_i$  and  $\mathbf{E}_j$ , and  $p(x)$  and  $p(y)$  represent the marginal probability distributions of  $\mathbf{E}_i$  and  $\mathbf{E}_j$ , respectively. This similarity matrix helps us determine which layers have the most aligned knowledge representations.

Calculate Weight ratio: To determine the merging ratio  $\lambda_m$  for each pair of layers, we introduce the adaptive weight allocation function  $\Psi$ . This function dynamically adjusts the merging ratio based on the similarity differences between layers, ensuring that the merged layer retains the most

critical features from each original layer:

$$
\lambda_m = \Psi(\bar{s}_i, \bar{s}_j) = \frac{e^{\mathcal{S}_{ij}}}{e^{\mathcal{S}_{ij}} + e^{\mathcal{S}_{ji}}} \tag{4}
$$

The adaptive weight allocation function  $\Psi$  adjusts the merging weights based on the similarity difference between layers. When the similarity difference between two layers is large, Ψ assigns a higher weight to the layer with higher similarity, reducing the weight of the layer with lower similarity. This mechanism ensures that the merged layer better preserves the knowledge from the more similar layer.

Merging Layer Parameters: Once the merging ratio  $\lambda_m$  is determined, we fuse the parameters  $\theta_i$ and  $\theta_i$  of the selected layers using a weighted sum:

$$
\widetilde{\theta}_m = \lambda_m \theta_i + (1 - \lambda_m) \theta_j \tag{5}
$$

The merged layer  $L_m$  is obtained through the function FuseLayer $(L_i, L_j, \theta_m)$ , which constructs a new layer based on the fused parameters  $\widetilde{\theta}_m$ . This new layer integrates the aligned knowledge from the original layers, preserving essential information while reducing redundancy.

Finally, we update the model  $M$  by replacing the original layers  $L_i$  and  $L_j$  with the newly merged layer  $L_m$ , utilizing the function ReplaceLayer( $M, L_i, L_j, L_m$ ). This step ensures that the model's architecture is updated to reflect the compression process, maintaining performance while significantly reducing model size.

<span id="page-4-0"></span>

Figure 2: Comparison of Accuracy (ACC) during merging and pruning on the MMLU dataset. MKA achieves higher compression ratios (approximately 43.5% for Llama3-8B, 45% for Llama3-70B, 40% for Mistral-7B, 31.25% for Llama2-7B, and 57.5% for Llama2-13B) while preserving 90% performance. Please see the appendix [A](#page-11-2) for details.

# 3 Experiments

We conduct a comprehensive set of experiments to evaluate the effectiveness and generalizability of our MKA method across various domains. Moreover, we aim to compare our approach with pruning techniques to assess whether it offers improvements and to investigate if it can be combined with quantization methods to achieve even higher compression ratios.

#### 3.1 Experimental Setup

#### 3.1.1 Datasets

We conduct evaluations using the MKA methods across various benchmark datasets, each specifically designed to test various facets of language comprehension and generation. In detail, MMLU [\(Hendrycks et al.,](#page-9-18) [2020\)](#page-9-18) evaluates broad language understanding across a wide range of domains. PIQA [\(Bisk et al.,](#page-8-6) [2020\)](#page-8-6) is designed to test models on commonsense reasoning in the physical world, aiming to assess NLP models' grasp of everyday physical interactions. HellaSwag [\(Zellers](#page-11-3) [et al.,](#page-11-3) [2019\)](#page-11-3) is a challenge dataset for commonsense natural language inference, consisting of event descriptions with multiple possible continuations, where the task is to select the most plausible one. RACE-H [\(Lai et al.,](#page-9-19) [2017\)](#page-9-19) is a large-scale reading comprehension dataset collected from English exams for Chinese high school students, featuring a high proportion of questions that require reasoning. BoolQ [\(Clark et al.,](#page-8-7) [2019\)](#page-8-7) is a reading comprehension dataset focusing on naturally occurring yes/no questions that often query for complex, non-factoid information and require difficult entailment-like inference to answer correctly.

### 3.1.2 LLMs

In our experiments, we employ the Llama-2 [\(Tou](#page-10-1)[vron et al.,](#page-10-1) [2023\)](#page-10-1), Llama-3, and Mistral-7B [\(Jiang](#page-9-20) [et al.,](#page-9-20) [2023\)](#page-9-20) models, each distinct in their capabilities and configurations: Llama-2: Encompassing models from 7 billion to 70 billion parameters, exhibits superior performance and safety on diverse benchmarks. Llama-3: Featuring models with 8 billion and 70 billion parameters, Llama3 offers state-of-the-art performance and advanced reasoning capabilities. Mistral-7B: a 7-billion-parameter model that surpasses Llama-2 and Llama-1 in performance and efficiency, leveraging grouped-query and sliding window attention mechanisms for optimal inference across lengthy sequences.

#### 3.1.3 Baselines

In this study, we assess the effectiveness of our proposed method, MKA, through two distinct comparative analyses. Firstly, we evaluate MKA directly against several well-established pruning techniques to gauge its standalone efficacy in reducing model size while maintaining performance. Secondly, we extend the comparison to include scenarios where both the traditional pruning methods and MKA are further enhanced through quantization. The baseline methods included in our analysis are: SparseGPT [\(Frantar and Alistarh,](#page-9-21) [2023\)](#page-9-21): An efficient one-shot pruning method that can induce high sparsity levels in large language models with billions of parameters while preserving accuracy, by reducing the pruning problem to a set of large-scale sparse regression instances solved by a novel approximate solver. ShortGPT [\(Men](#page-9-3) [et al.,](#page-9-3) [2024\)](#page-9-3): A pruning method that removes redundant layers from large language models based on a Block Influence metric, which assesses the significance of each layer. Reverse Pruning: A heuristic approach where the importance of layers is considered inversely proportional to their order in the model, prioritizing the retention of earlier layers. SmoothQuant [\(Xiao et al.,](#page-11-4) [2023\)](#page-11-4): SmoothQuant is a training-free post-training quantization solution that enables efficient 8-bit weight and activation quantization for large language models, offering up to 1.56× speedup and 2× memory reduction with minimal accuracy loss. **GPTQ** [\(Frantar et al.,](#page-9-22) [2022\)](#page-9-22): A one-shot weight quantization method that uses approximate second-order information to maintain high accuracy even with severe weight reduction. AWQ [\(Lin et al.,](#page-9-23) [2023\)](#page-9-23): A novel quantization approach that protects salient weights by adjusting per-channel scaling based on activation observations rather than weight Magnitudes.

### 3.2 In what ways does MKA surpass conventional pruning techniques?

We compare the performance of MKA with baseline compression methods on the MMLU dataset using the Llama3-8B, Llama3-70B, Mistral-7B, Llama2-7B, and Llama2-13B models. The evaluation metric is Accuracy (ACC) during merging and pruning. The results are presented in Figure [2.](#page-4-0)

We compare the performance of MKA with baseline compression methods on the MMLU dataset using the Llama3-8B, Llama3-70B, Mistral-7B, Llama2-7B, and Llama2-13B models. The evaluation metrics include Accuracy (ACC) during merging and pruning. The results are presented in Figure [2.](#page-4-0) We can observe that, across all models, our method improves the compression ratio while maintaining performance. Specifically, the com-pression ratio<sup>[3](#page-5-0)</sup> for Llama3-8B reach  $43.5\%$ , for Mistral-7B it reaches 40%, and for Llama2-13B it reaches an impressive 57.5%. Additionally, we observe several phenomena: both methods experience a collapse in model performance, but the model merging method can delay the layer collapse to some extent and stabilize the model's performance very well. Since our strategy is based on Reverse Prune, the scores for the Llama3-8B, Llama2-7B, and Llama2-13B models are very close to the Reverse Prune. Our hypothesis is that the pruning or merging of these models is similar, but model merging can adjust the merging ratio to surpass the effects of pruning. Moreover, for the Llama3-70B and Mistral-7B models, we noticed that the results do not closely match the Reverse Prune.

<span id="page-5-1"></span>

Model	<b>Method</b>	<b>Retained lavers</b> (Compression Ratio)	Acc.				
	Vanilla Model	$32(0.00\%)$	66.29				
	ShortGPT+Smooth	18(85.94%)	26.54				
	ShortGPT+GPTO	18(85.94%)	25.98				
Llama3-8R	ShortGPT+AWO	18(85.94%)	26.22				
	MKA (Ours) + Smooth	$18(85.94\%)$	$64.20 (+37.66)$				
	MKA (Ours) + GPTO	$18(85.94\%)$	$62.98 (+37.00)$				
	$MKA (Ours) + AWO$	$18(85.94\%)$	$61.66 (+35.44)$				
	Vanilla Model	$32(0.00\%)$	63.87				
Mistral-7B	ShortGPT+Smooth	20(84.38%)	24.32				
	ShortGPT+GPTQ	20(84.38%)	23.16				
	ShortGPT+AWO	20(84.38%)	23.96				
	MKA (Ours) + Smooth	20(84.38%)	$56.92 (+32.60)$				
	MKA (Ours) + GPTO	20(84.38%)	$56.12 (+32.96)$				
	$MKA (Ours) + AWO$	20(84.38%)	$55.34 (+31.38)$				
	Vanilla Model	$32(0.00\%)$	46.67				
	ShortGPT+Smooth	16(87.50%)	25.67				
	ShortGPT+GPTO	$16(87.50\%)$	25.82				
Llama <sub>2-7R</sub>	ShortGPT+AWQ	16(87.50%)	26.01				
	MKA (Ours) + Smooth	$16(87.50\%)$	$35.66 (+9.99)$				
	MKA (Ours) + GPTO	$16(87.50\%)$	$35.91 (+10.09)$				
	$MKA (Ours) + AWO$	$16(87.50\%)$	$36.23 (+10.22)$				
	Vanilla Model	40 (0.00%)	55.62				
	ShortGPT+Smooth	20 (87.50%)	25.89				
	ShortGPT+GPTO	20 (87.50%)	25.35				
$Llama2-13R$	ShortGPT+AWQ	20 (87.50%)	23.83				
	<b>MKA</b> (Ours) + Smooth	20 (87.50%)	$46.82 (+20.93)$				
	MKA (Ours) + GPTO	20 (87.50%)	$45.44 (+20.09)$				
	$MKA (Ours) + AWO$	20 (87.50%)	$45.86 (+22.03)$				

Table 1: Performance comparison of MKA and ShortGPT pruning with quantization (SmoothQuant, GPTQ, AWQ) on MMLU using Llama3-8B, Mistral-7B, Llama2-7B, and Llama2-13B. MKA outperforms ShortGPT in accuracy across all models and quantization methods at similar compression ratios with int4. The calculation of the compression ratio only considers the number of hidden layers in the model without considering the embedding layer.

# 3.3 How Does MKA Combined with Quantization Perform Compared to Pruning Combined with Quantization?

We compare the performance of MKA with the baseline pruning method, ShortGPT [\(Men et al.,](#page-9-3) [2024\)](#page-9-3), on the MMLU dataset using the Llama3-8B, Llama3-70B, Mistral-7B, Llama2-7B, and Llama2- 13B models. The results are shown in Table [1.](#page-5-1)

We can see that the pruned models are able to be further quantized and maintain performance with a higher compression ratio. Notably, at a high compression ratio of around 87.50%, MKA significantly outperforms ShortGPT. Additionally, we achieve excellent results using various quantization methods. For example, on Llama3-8B, at a compression ratio of 85.94%, MKA with SmoothQuant achieves 64.20%, far exceeding ShortGPT with SmoothQuant at 37.66%. Similarly, with the GPTQ quantization method, we achieve 62.98%, surpassing ShortGPT's 37.00%, and with AWQ, we achieve 61.66%, exceeding ShortGPT's 35.44%.

<span id="page-5-0"></span><sup>&</sup>lt;sup>3</sup>Note that, the compression ratio is calculated as:  $\left(L_{\text{total}} - \left(\frac{L_{\text{retained}}}{Q}\right)\right) / L_{\text{total}}$ , where  $L_{total}$  is the total number of layers before compression,  $L_{retained}$  is the number of retained layers, and Q is the quantization factor.

			Compression Ratio = $34.375\%$		Compression Ratio = $37.5\%$									
<b>Method</b>	<b>MMLU</b>	PIQA	HellaSwag	<b>RACE-H</b>	<b>BoolQ</b>	<b>MMLU</b>	PIQA	<b>HellaSwag</b>	<b>RACE-H</b>	<b>BoolO</b>				
Vanilla Model	66.29	81.12	74.54	66.07	66.79	66.29	81.12	74.54	66.07	66.79				
SparseGPT	44.45	58.77	32.14	35.06	48.29	41.95	56.23	28.63	37.84	52.40				
<b>ShortGPT</b>	42.95	60.99	33.00	41.68	51.96	44.80	61.70	38.69	40.05	57.09				
<b>MKA</b> (Ours)	64.87	67.79	51.32	55.20	63.36	62.05	66.26	50.16	49.49	63.46				
			Compression Ratio = $40.625\%$					Compression Ratio = $43.75\%$						
<b>Method</b>	<b>MMLU</b>	<b>PIOA</b>	<b>HellaSwag</b>	<b>RACE-H</b>	<b>BoolO</b>	<b>MMLU</b>	<b>PIOA</b>	<b>HellaSwag</b>	<b>RACE-H</b>	<b>BoolO</b>				
Vanilla Model	66.29	81.12	74.54	66.07	66.79	66.29	81.12	74.54	66.07	66.79				
SparseGPT	37.30	59.36	32.16	22.06	60.63	33.11	57.12	29.63	23.14	59.41				

Table 2: Comparison of different methods across MMLU, PIQA, HellaSwag, RACE-H, and BoolQ datasets at different compression ratios.

<span id="page-6-0"></span>MKA (Ours) 63.42 65.61 48.83 55.26 63.58 64.42 65.51 45.10 45.91 62.14

<span id="page-6-1"></span>

Figure 3: Similarity matrices for Llama-3-8B, Llama-3-70B, Mistral-7B, Llama-2-7B, and Llama-2-13B before and after MKA. Later layers show high similarity, supporting layer merging.

# 3.4 MKA vs. Other Pruning Methods on varies benchmarks

We compared the performance of MKA and several other pruning methods on the LLama3-8B model using multiple benchmark datasets at compression ratios of 34.375%, 37.5%, 40.625% and 43.75%. The results are shown in Table [2.](#page-6-0) From the results, merging can retain performance better compared to pruning. Relative to SparseGPT and Short-GPT, our method can achieve better performance retention, with significant improvements across all datasets. For example, at a compression ratio of 34.375% on the MMLU dataset, our method can outperform ShortGPT by 21.92% and SparseGPT by 20.42%. Similarly, on the HellaSwag dataset, our proposed method can surpass ShortGPT by 18.32% and SparseGPT by 18.32%.

# 3.5 Are Inter-Layer Knowledge Alignment Similarity Matrices Consistent Across Different Large Models?

We generate layer similarity heatmaps for different models before and after applying MKA. These heatmaps visualize the knowledge alignment and layer merging effects of MKA on various models. Figure [3](#page-6-1) presents the similarity heatmaps for Llama-3-8B, Llama-3-70B, Mistral-7B, Llama-2-7B, and Llama-2-13B. We observe that the heatmaps for the later layers of each model exhibit high similarity values, indicating that interlayer similarity is consistently high in the later layers across different models. This observation supports our layer merging approach. Additionally, when merging the earlier layers, we notice a collapse of the matrix in the final figure, suggesting that earlier layers have a significant influence on later layers. Thus, simple merging operations on the earlier layers of the model are not feasible.

# 4 Discussion

# 4.1 Extension to Multimodal and Specialized Models

In addition to its application to large language models, the MKA method shows promising potential for broader adoption across a variety of deep learning architectures. This includes Mixture-of-Experts (MoE) [\(Jiang et al.,](#page-9-0) [2024\)](#page-9-0), and Mamba [\(Gu and](#page-9-24) [Dao,](#page-9-24) [2023;](#page-9-24) [Lieber et al.,](#page-9-25) [2024\)](#page-9-25) models, which can exhibit similar redundancies in their process-

<span id="page-7-0"></span>

Figure 4: The similarity matrices of Mixtral-8x7B and the Jamba model.

ing layers.The results show in Figure [4.](#page-7-0) Initial experiments conducted on these diverse architectures have reinforced the viability of our approach. For instance, the similarity matrices generated on jamba [\(Lieber et al.,](#page-9-25) [2024\)](#page-9-25) and Mixtral-8x7B [\(Jiang](#page-9-0) [et al.,](#page-9-0) [2024\)](#page-9-0) applying MKA have shown that Our method can also be generalized to other similar models, but the similarity distributions of jamba and Mixtral-8x7B are slightly different from LLM, and we do not yet know the reason. These experiments further validate the effectiveness of our method across different model types.

### 4.2 Analysis of Similarity Measures

In our evaluation of the Llama3-8B model, we explored several similarity measures: Cosine Similarity, Mahalanobis Distance, Euclidean Distance, t-SNE Similarity, and Autoencoder Similarity. The similarity matrices are shown in Figure [5.](#page-8-8) From the results, we observe that Cosine Similarity, Mahalanobis Distance, and Euclidean Distance display similar distribution patterns with vertical stripes and varied heat values. However, Mahalanobis Distance shows irregular heat values within these stripes, indicating a misalignment with the fused layer data structure. t-SNE Similarity appears random and lacks consistent patterns. For Autoencoder Similarity, the high heat values do not correspond to suitable merging areas or expected highsimilarity regions.

# 4.3 Variations in Accuracy Across Different MMLU Subjects During Layer Merging

We examine the impact of model merging on performance across various academic subjects in the MMLU benchmark. Figure [6](#page-8-9) shows the accuracy changes across subjects such as College Medicine, College Biology, High School Psychology, and College Physics during different stages of merging model layers. From our results, we observe

that High School Psychology maintained a stable accuracy with only minor fluctuations, suggesting a consistent performance and low sensitivity to the merging process. In contrast, College Biology experiences a significant drop in accuracy at the 12.5% merging ratio, followed by a recovery. College Physics exhibits frequent fluctuations in accuracy, pointing to a high sensitivity to layer merging. Conversely, College Medicine experiences a steady increase in performance with only minor variations.

# 5 Conclusion

In this paper, we have proposed Manifold-Based Knowledge Alignment and Layer Merging Compression (MKA), a novel model compression technique specifically designed to efficiently reduce the size of large language models (LLMs) while maintaining their performance. MKA leverage manifold learning techniques to align knowledge across layers and utilizes the Normalized Pairwise Information Bottleneck (NPIB) measure to identify the most similar layers for merging. By capturing the intricate nonlinear dependencies within LLMs and integrating knowledge from similar layers, MKA achieves remarkable compression ratios without sacrificing model accuracy. We have conducted extensive experiments on a diverse set of benchmark datasets and various state-of-the-art LLMs to rigorously evaluate the effectiveness of MKA in preserving model performance while significantly reducing model size. Our empirical results demonstrate that MKA consistently outperforms existing pruning methods and can achieve even higher compression ratios when combined with quantization techniques.

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<span id="page-8-8"></span>

Figure 5: Similarity matrices for various measures in the Llama3-8B model, showing different patterns and effectiveness in capturing layer relationships, with none fully matching the expected merging patterns.

<span id="page-8-9"></span>

Figure 6: ACC changes across different MMLU dataset subjects during merging.

### Limitations

The quality of the manifold learning process in MKA heavily depends on the diversity and representativeness of the layer activations extracted from the input dataset. In our experiments, we used  $\sigma$ value of 8 and selected the first question from the 57-question MMLU dataset to extract activations. We observed that the number of questions sampled can significantly impact the manifold learning results. Ensuring keeping the Condition Number below 2000 is crucial for maintaining the integrity of the learned manifold representations. If the dataset used for extracting activations does not adequately cover the model's operational range, the learned manifold representations might fail to capture the true geometric structure of the data.

The current implementation of MKA has been primarily tested on transformer-based architectures. Although we believe that deep neural networks inherently contain redundancies, the applicability and effectiveness of MKA on other neural network architectures, such as convolutional neural networks (CNNs) or recurrent neural networks (RNNs), have not been thoroughly explored. Future research can investigate these architectures to confirm whether MKA can achieve similar compression benefits across different types of neural networks.

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# <span id="page-11-2"></span>A More Results

Model	<b>Methods</b>		0.03125			0.0625 0.09375 0.125 0.15625 0.1875 0.21875 0.25 0.28125 0.3125 0.34375 0.375 0.40625 0.4375 0.46875 0.5											
	Llama3_8b $\left  \begin{array}{c} \text{ACC} \text{ (Reverse)} \\ \text{ACC} \text{ (Ours)} \end{array} \right $	66.29	$\begin{bmatrix} 66.29 & 66.12 & 66.33 & 66.15 & 66.21 & 65.31 \end{bmatrix}$			$\begin{array}{cccccccc} 66.12 & 66.33 & 66.15 & 66.21 & 65.31 & 64.96 & 62.91 & 64.28 & 65.00 \\ 65.96 & 66.26 & 66.15 & 58.08 & 62.94 & 64.96 & 62.92 & 64.28 & 65.01 \end{array}$					63.99 63.99	64.87 62.05 63.42		64.71 62.04 63.52	64.51 64.42	30.31 29.07 30.29 29.05	
	Llama2_7b $\left  \begin{array}{c} \text{ACC} \text{ (Reverse)} \\ \text{ACC} \text{ (Ours)} \end{array} \right $	46.67	46.67 44.37 46.71	44.45 46.74	46.07	46.09 46.89 46.51 46.93 46.52	46.79 46.84	43.33 43.41	45.90 45.85	45.22 45.09	35.33 35.25	40.67	42.40	40.58 42.33 37.34 37.38	39.26 39.41	39.53 35.65 39.45 35.71	

Table 3: ACC during the compression process of Ours and Reverse Prune on Llama3-8b and Llama2-7b models.

Methods		0.025	0.05 0.075 0.1 0.125 0.15 0.175 0.2 0.225 0.25 0.275 0.3 0.325 0.35 0.375 0.4 0.425 0.45 0.475 0.5									
ACC (Reverse)   55.62 55.24 55.21 55.12 54.44 54.02 55.63 55.27 53.87 53.66 53.17 51.89 51.56 51.56 51.48 50.75 50.28 48.37 45.18 48.59 46.78												
ACC (Ours)	55.62 55.24 55.21 55.12 54.44 54.02 55.63 55.27 53.87 53.66 53.17 51.89 51.56 51.56 51.49 50.75 50.28 48.37 45.18 48.59 46.78											

Table 4: ACC during the compression process of Ours and Reverse Prune on Llama2-13b model.