# AlignedCoT: Prompting Large Language Models via Native-Speaking Demonstrations

Zhicheng Yang<sup>1</sup> Yinya Huang<sup>4</sup> Jing Xiong<sup>6</sup>

Liang Feng<sup>5</sup> Xiaodan Liang<sup>6,7</sup> Yiwei Wang<sup>3</sup> Jing Tang<sup>1,2\*</sup>

<sup>1</sup>The Hong Kong University of Science and Technology (Guangzhou)

<sup>2</sup>The Hong Kong University of Science and Technology <sup>3</sup>University of California, Merced

<sup>4</sup>City University of Hong Kong <sup>5</sup>Chongqing University

<sup>6</sup>Shenzhen Campus of Sun Yat-sen University <sup>7</sup>MBZUAI

yangzhch6@gmail.com, wangyw.evan@gmail.com, yinya.huang@hotmail.com,

xiongj69@mail2.sysu.edu.cn, xdliang328@gmail.com, jingtang@ust.hk

## Abstract

Large Language Models prompting, such as using in-context demonstrations, is a mainstream technique for invoking LLMs to perform highperformance and solid complex reasoning (e.g., mathematical reasoning, commonsense reasoning), and has the potential for further human-machine collaborative scientific findings. However, current LLMs are delicate and elusive in prompt words and styles. And there is an unseen gap between LLM understanding and human-written prompts. This paper introduces AlignedCoT, an LLM-acquainted prompting technique that includes proficient "native-speaking" in in-context learning for the LLMs. Specifically, it achieves consistent and correct step-wise prompts in zero-shot scenarios by progressively probing, refining, and formatting the LLM chain of thoughts so that free from handcrafted few-shot demonstrations while maintaining the prompt quality. We conduct experiments on mathematical reasoning and commonsense reasoning. We find that LLMs with AlignedCoT perform significantly superior to them with human-crafted demonstrations. We further apply AlignedCoT for rewriting the GSM8K training set, resulting in a GSM8K-Align dataset. We observe its benefits for retrieval augmented generation. The code and data can be found at https://github.com/yangzhch6/AlignedCoT.

## 1 Introduction

Rapidly increasing capabilities of large language models (LLMs) lead to remarkable advances in various NLP tasks (Devlin et al., 2019; Radford and Narasimhan, 2018; Raffel et al., 2020). However, as LLMs scale up, the computational load of fine-tuning LLMs becomes generally unaffordable. Meanwhile, in-context learning (ICL) methods exhibit competing performance with fine-tuning (Brown et al., 2020; Wei et al., 2022b; Kojima

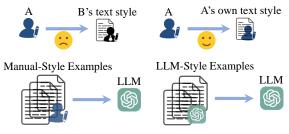


Figure 1: A human/machine (A) tends to accept words in her own style (A's own text style) rather than other people's (B's text style). In this work, we investigate efficient CoT demonstrations by resorting to LLM-learned text habits (an LLM-style).

et al., 2022). ICL saves the high costs of training LLMs and enjoys high interpretability from the produced reasoning steps. These advantages make ICL emerge as a new popular paradigm for NLP, where LLMs make predictions based on in-context demonstrations.

A core question in ICL is the selection of effective demonstrations. Wei et al. (2022b) proposes chain-of-thought (CoT) prompting with a sequence of short sentences describing intermediate reasoning steps toward final answers. Originating from CoT, a line of ICL research (Liu et al., 2022; Rubin et al., 2022; Su et al., 2023; Fu et al., 2023; Ye et al., 2023; Li et al., 2023a) compose few-shot prompts by selecting examples that are relevant to the input question. The other line of work (Wang et al., 2023b; Li et al., 2023b) improves LLMs by increasing prompt diversity by sampling reasoning paths multiple times. Furthermore, another works (Yao et al., 2023; Long, 2023; Hao et al., 2023; Zhang et al., 2023a) propose to mimic human cognitive processes. However, CoT's text style, specifically LLMs' familiarity and proficiency in language use while thinking, and its effect on LLM complex reasoning performances, remain underexplored.

An intuition is that it is more natural for humans to speak in their own style than to imitate others. As illustrated in Figure 1, a similar situa-

<sup>\*</sup>Corresponding author: Jing Tang.

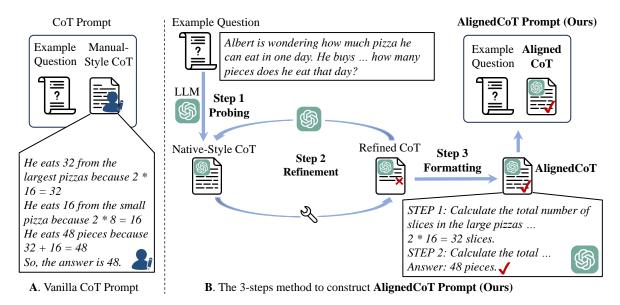


Figure 2: **A**. Existing few-shot demonstrations are conventionally dataset samples or human crafts ("Manual-Style"). As a result, an LLM tends to copy the "Manual-Style" format mechanically. **B**. The proposed AlignedCoT prompt has zero-shot CoTs with correct and in LLM-acquainted format ("Native-Style"). The AlignedCoT is obtained via three steps: (1) Probing LLM's native style in zero-shot scenarios; (2) Refining the generated CoT to correct errors in the first step; (3) Formatting the generated CoTs in the first two steps.

tion for LLMs as they may perform better when prompted with their native-style CoT rather than imitating other styles. However, current CoTs are often human-crafted or come from static dataset samples, resulting in LLMs mimicking the given demonstrations and without their own thinking process. Contrastively, LLMs can benefit from a zero-shot manner by generating CoTs in their own "native-style" thinking process, which elicits the stored knowledge learned from training (pretraining, SFT, RLHF).

To investigate such "native-style" thinking processes, this paper proposes Aligned Chain-of-Thought (AlignedCoT) Prompting. AlignedCoT aims to improve LLM reasoning by aligning the conventional few-shot CoTs to a "native-style" zero-shot CoT. From the perspective of generalization, the alignment mitigates the disparity between the training and inference; reduces the requirement for extensive model generalization capabilities; and results in performance enhancements.

The proposed AlignedCoT operates in steps, as shown in Figure 2. (1) Using each question in the few-shot prompt to query the LLM and generate its native-style CoT in a zero-shot scenario. (2) Refining the generated CoT to correct any errors. (3) Unifying the CoT text formats, including the format of the final answer and the format of the solution steps. We then construct the few-shot prompt using the native-style CoT obtained in the aforementioned three steps to query the LLM.

The contributions of this paper are as follows:

- We propose a novel and effective prompting method named AlignedCoT, which aligns the CoT text style in few-shot examples to the native style of Large Language Models to improve their reasoning capability.
- We evaluate AlignedCoT through extensive experiments, including baseline comparisons and ablation studies. The experimental results show that AlignedCoT achieves significant performance improvements and can be easily integrated with other in-context learning methods.
- We apply AlignedCoT to overwrite the GSM8K dataset and provide the GSM8K-Align dataset. Empirical results show that GSM8K-Align can effectively improve the performance of retrieving augmented methods.

## 2 Related Work

**Emergent Abilities and Multi-Step Reasoning.** As the amount of computation and data in language models continues to grow, advanced capabilities emerge (Kaplan et al., 2020; Wei et al., 2022a). The ability of in-context learning (ICL), that is, to solve the corresponding tasks according to the given few-shot examples, is something that language models are particularly skilled at when scaled up to a certain size (Shin et al., 2020; Liu et al., 2023). Specifically, multi-step reasoning tasks such as math problem solving (Cobbe et al., 2021; Yang et al., 2022a,b; Ling et al., 2017; Wang et al., 2017) and Commonsense Reasoning (Suzgun et al., 2023; bench authors, 2023; Geva et al., 2021; Talmor et al., 2019) witness significant performances growth from larger models, compared to plain tasks such as emotion classification (Shin et al., 2020). Moreover, few-shot prompting a language model could outperform itself fine-tuned with a full training set. In this work, we further investigate the leverage of prompting an LLM for eliciting advanced reasoning capabilities.

Chain-of-Thought Reasoning. Chain-of-thought prompting (Wei et al., 2022b) shows that prompting LLMs with intermediate reasoning steps can greatly improve multi-step reasoning ability. Based on this prominent work, further works show that CoT can be improved by various approaches. Wang et al. (2023b) propose self-consistency which conducts majority voting by sampling different reasoning paths. Least-to-Most prompting (Zhou et al., 2023) guides the LLMs to first decompose the original question into small parts and then solve it. Tree-of-Thought (Yao et al., 2023; Long, 2023) further supports chain-of-thought by solving complex problems in a tree search process. Reasoning via Planning (Hao et al., 2023) repositions LLM as both a world model and an inference model, and combines the Monte Carlo Tree Search algorithm to search in a huge inference space. It is further observed (Kojima et al., 2022) that LLMs are decent zero-shot reasoners and can generate intermediate reasoning steps by simply adding "Let's think step by step" before each answer. Our work sits in the context of CoT reasoning and proposes a new method to improve reasoning ability in LLMs by aligning CoT text style in few-shot examples to LLM's native style with correct reasoning steps in zero-shot scenarios.

**Demonstration Design of In-Context Learning.** Due to the sensitivity of LLMs to prompts, tasks, and datasets (Zhao et al., 2021; Lu et al., 2022; Su et al., 2022), designing prompts and the selection of good examples for in-context learning in few-shot scenarios is a fundamental question (Liu et al., 2022). The vanilla CoT (Wei et al., 2022b) prompts LLMs with 8 manually written examples. Based on this, PAL (Gao et al., 2023) converts these examples into programming language statements. Complex CoT (Fu et al., 2023) selects examples with the most complex reasoning steps from the training set, which improves multi-step reasoning. The other line of work uses retrieval-based methods to extract the most similar and relevant examples in the training set. Liu et al. (2022) retrieves semantically similar examples with a test query to formulate its corresponding prompt. EPR (Rubin et al., 2022) uses an unsupervised retriever to obtain a set of candidate examples. CEIL (Ye et al., 2023) leverages contrastive learning to obtain preferred examples. DQ-Lore (Xiong et al., 2023) leverages Dual Queries and Low-rank approximation Re-ranking for sample selection. The demonstrations in these works are either from the original training set or handcrafted by humans. In this paper, we propose AlignedCoT, which leverages LLM to generate correct and unified few-shot demonstrations on their own.

Additionally, Auto-CoT (Zhang et al., 2023b) divides the training set into k categories and then selects k samples that are closest to the cluster center, and then allows the LLM to automate its own demonstrations. Nori et al. (2023); Zhao et al. (2023) generates self-explanations as in-context exemplars for medical QA. Wang et al. (2023a) built a data-generation pipeline named SP-CoT for opendomain question-answering (OPQA) consisting of carefully constructed data generation and composition steps by hand, but is difficult to transfer to other data fields. The aforementioned works are limited to specific domains and only discuss generating demonstrations by LLMs themselves. This paper further delves into error handling in demonstrations and the impact of "native-style" CoTs on LLMs performance.

# 3 AlignedCoT Prompting

Figure 2 shows the proposed AlignedCoT. The main purpose of AlignedCoT is to achieve LLM's native-style CoTs without following human-written few-shot demonstrations. Specifically, the native-style CoTs are preferred to be zero-shot CoTs and at the same time have consistent formats and correct steps as stronger substitutions to the few-shot handcrafts. To achieve this, AlignedCoT builds an effective alignment between the two with the following steps: Probing LLM's native style in

zero-shot scenarios (§3.1), refining the generated CoT to correct errors in the first step (§3.2), and unifying the format of the generated CoTs in the first two steps (§3.3). The obtained AlignedCoT is then applied by replacing the CoT demonstrations in the original few-shot prompt to query LLMs.

### 3.1 Probing Native-Style of LLM

As shown in Figure 2.A, the chain-of-thought text in the few-shot examples is generally handcrafted (Wei et al., 2022b). We consider the text style of handcrafted CoTs as a "manual-style". Compared with the few-shot scenarios in existing works (which directly use handcrafted examples), LLM does not need to imitate the CoT text that is inconsistent with its own language style in zero-shot scenarios. We refer to the CoT text style generated by LLM in zero-shot scenarios as "native-style". When prompting Large Language Models (LLMs) with "manual-style" CoTs, LLMs will follow the formatted demonstrations, which may not fully exploit the LLM's learning capabilities.

To bridge this gap, we introduce the first step of our AlignedCoT Prompting method, which involves Probing LLM's native-style Chain-of-Thought (CoT) in zero-shot scenarios. As illustrated in Figure 2.B, in order to acquire the CoT with native style, we use the magic phrase "Let's think step by step" proposed by Kojima et al. (2022) to query LLMs for each example in a given fewshot prompt to generate a CoT that resembles the way it naturally responds to the input question.

However, the generated native-style CoTs are not always correct. To deal with the errors and inconsistency, we need to proofread the generated content against the ground truth answer in the dataset.

### 3.2 Refining CoTs

The second critical phase of our AlignedCoT Prompting involves the process of refining the CoTs generated in the previous step. This phase is to rectify the inaccuracies in the initially generated content. The ultimate goal is to ensure that the CoTs adhere to the highest standards of accuracy, enabling more precise reasoning and response generation by Large Language Models.

The refining process is initiated by identifying and addressing the first encountered error or irrationality in the CoT text. Subsequently, we harness the capabilities of LLMs to iteratively correct the text, moving forward and completing the answer from the initially modified error position. An ex-

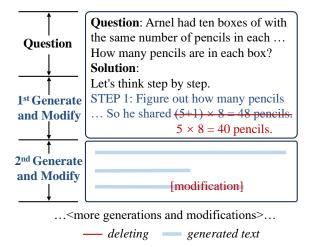


Figure 3: The illustration of our refining process. The modifications in red are annotated manually. We modify the first error each time and then query the LLM to complete the text behind the last modified error.

ample of this process is shown in Figure 3. This iterative approach is executed in the same zeroshot scenario of §3.1, ensuring that the entire text is rectified while preserving the native style of the LLM's expression. Note that our approach to refinement is designed with a focus on minimalist text modification, which ensures that the generated CoTs are not only error-free but also in harmony with the inherent stylistic nuances of the LLM.

#### **3.3 Unifying the Format of CoTs**

A crucial aspect that deserves meticulous attention is the consistency of the answer text format and punctuation marks across different examples. This consistency plays a pivotal role in ensuring optimal model performance, as it enables the model to understand and respond to the input queries.

To unify the format of each example, we undertake a manual examination of the generated CoTs from the previous steps. During this evaluation, we focus on two aspects: the format of the answer text and the punctuation marks of solution steps. By meticulously inspecting and revising these elements, we ensure that each CoT conforms to a standardized style, making them more interpretable and consistent in their presentation. This approach guarantees that the standardized CoTs maintain a natural and coherent flow, thus enhancing their utility in subsequent reasoning and response generation tasks.

Model	Prompt	GSM8K	AQUA	SVAMP*	AddSub	SingleEQ	Penguins	Avg
	CoT w/o AlignedCoT	77.1	54.7	82.8	93.1	96.0	78.1	80.3
	CoT w/ AlignedCoT (Ours)	78.7	57.1	84.8	94.9	97.6	87.7	83.5
	Δ	<b>+1.6</b> ↑	<b>+2.4</b> ↑	<b>+2.0</b> ↑	<b>+1.8</b> ↑	<b>+1.6</b> ↑	<b>+9.6</b> ↑	<b>+3.2</b> ↑
	Auto-CoT w/o AlignedCoT	78.6	50.4	81.6	92.7	96.5	80.1	80.0
GPT-3.5-turbo	Auto-CoT w/ AlignedCoT (Ours)	79.8	52.0	82.3	93.9	96.5	84.9	81.6
	Δ	<b>+1.2</b> ↑	<b>+1.6</b> ↑	<b>+0.7</b> ↑	<b>+1.2</b> ↑	<b>+0.0</b> ↑	<b>+4.8</b> ↑	<b>+1.6</b> ↑
	Complex CoT w/o AlignedCoT	79.6	55.5	82.9	93.1	96.9	81.5	81.6
	Complex CoT w/ AlignedCoT (Ours)	82.4	57.9	85.1	95.2	98.0	86.3	84.2
	Δ	<b>+2.8</b> ↑	<b>+2.4</b> ↑	<b>+2.2</b> ↑	<b>+2.1</b> ↑	<b>+1.1</b> ↑	<b>+4.8</b> ↑	<b>+2.6</b> ↑

Table 1: Answer accuracy (%) of GPT-3.5-Turbo, we compare the performance with or without using our AlignedCoT.  $\Delta$  indicates performance improvement.

Model	Prompt	GSM8K	AQUA	SVAMP*	Penguins	Avg
	CoT w/o AlignedCoT	93.1	72.8	94.1	96.6	89.2
	CoT w/ AlignedCoT (Ours)	94.4	75.6	94.8	98.6	90.9
	$\Delta$	+1.3↑	<b>+2.8</b> ↑	<b>+0.7</b> ↑	<b>+2.0</b> ↑	<b>+1.7</b> ↑
CDT 4	Auto-CoT w/o AlignedCoT	93.1	72.4	93.9	97.9	89.3
GPT-4	Auto-CoT w/ AlignedCoT (Ours)	94.2	73.6	94.4	97.9	90.0
	$\Delta$	<b>+1.1</b> ↑	<b>+1.2</b> ↑	<b>+0.5</b> ↑	<b>+0.0</b> ↑	<b>+0.7</b> ↑
	Complex CoT w/o AlignedCoT	94.4	73.6	94.2	98.6	90.2
	Complex CoT w/ AlignedCoT (Ours)	95.6	74.8	94.6	99.3	91.1
	Δ	<b>+1.2</b> ↑	<b>+1.2</b> ↑	<b>+0.4</b> ↑	<b>+0.7</b> ↑	<b>+0.9</b> ↑

Table 2: Answer accuracy (%) of GPT-4.  $\Delta$  indicates performance improvement.

## **4** Experiments

In this section, we first discuss our experimental setting in §4.1. In §4.2 and §4.6, we not only show AlignedCoT's superior performance in multi-step reasoning but also demonstrate that AlignedCoT helps LLM find logical paradoxes better. Furthermore, we conduct ablation study, case study, and more in-depth analysis in §4.4 and §4.7.

### 4.1 Experimental Setup

**Datasets and Language Models.** We evaluate our AlignedCoT on GSM8K (Cobbe et al., 2021), AQUA (Ling et al., 2017), SVAMP(Patel et al., 2021), AddSub (Hosseini et al., 2014), SingleEQ (Koncel-Kedziorski et al., 2015), and Penguins (Suzgun et al., 2023). We choose these datasets because we focus on the multi-step reasoning ability of large language models. Specifically, there are 7.4k training instances and 1.3k test instances in GSM8K, all samples have manually labeled intermediate problem-solving steps. AQUA is a larger mathematical dataset with more difficult samples that are annotated with rationales by human annotators. AddSub and SingleEQ require the model to have basic computational capabilities. Penguins contain questions referring to different objects (e.g., Find the name of the oldest penguin).

SVAMP and SVAMP\*. SVAMP is a challenging dataset created by applying carefully chosen variations over examples sampled from existing datasets. However, some questions have logical incorrectness. For example: "A waiter had 12 While 15 customers left he customers. got 14 new customers", where the number of customers leaving is actually higher than the number of existing customers, which is impossible to happen. Specifically, we first manually go over and fix the logical paradoxes in the original SVAMP dataset. There are 7.1% of the entire dataset that have such logical paradoxes. We then have a fixed dataset, denoted as SVAMP\*. We use the fixed SVAMP\* for experiments. The dataset will be released later.

Language Models and Prompts.. Our experiments are conducted on GPT-3.5-Turbo (OpenAI, 2022) and GPT-4 (OpenAI, 2023) (both use the 0613 version) via the OpenAI API key. Our

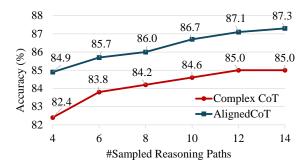


Figure 4: In the case of sampling diverse reasoning paths on GSM8K, our AlignedCoT also outperforms Complex CoT.

AlignedCoT focuses on converting the CoT text style of examples in the given few-shot prompt, it neither requires special sample selection methods nor changes the processes of the prompting methods. In our experiments, we choose the original CoT prompt proposed by Wei et al. (2022b), the complex CoT prompt proposed by Fu et al. (2023), and the prompt extracted by Efficient Prompt Retriever (EPR) (Rubin et al., 2022) as the baselines. Following (Kojima et al., 2022), we add "Let's think step by step" before the reasoning chains for all baselines to improve the performance. We show all the prompts we acquired in the Appendix.

**Compared Methods.** We compare AlignedCoT with previous CoT methods. All methods use greedy decoding (i.e. temperature is set to 0). The Standard Prompt (Wei et al., 2022b) is humancrafted without intermediate reasoning steps, Auto-CoT (Zhang et al., 2023b) constructs prompt from a sample pool, and the CoT Prompt (Wei et al., 2022b) includes manually designed intermediate steps. The Complex CoT (Fu et al., 2023) as a strong baseline consists of the examples with the most complex intermediate reasoning steps. In Complex Prompt, intermediate steps are taken from the source dataset, if the source data does not have intermediate steps, they are manually annotated.

#### 4.2 Main Results

Tables 1 and 2 demonstrate the results. Note that AddSub and SingleEQ do not serve as benchmarks for GPT-4 since GPT-4 already achieves close to 100% accuracy on these datasets with CoT prompt. In general, the proposed AlignedCoT effectively improves reasoning abilities in LLMs. LLMs with CoT empowered by our AlignedCoT show an average of +3.2% and +1.7% performance improvements for GPT-3.5-turbo and GPT-4, respectively.

Model	Complex CoT	AlignedCoT
GPT-3.5-Turbo	15.5	18.3
GPT-4	28.2	78.9

Table 3: Logical error recognition rate of GPT-3.5-Turbo and GPT-4. Results are calculated on 7.1% logically incorrect questions as introduced in Section 4.1.

Probing	Refining	Formatting	Answer Accuracy
×	×	×	79.6
	×	×	80.5 (+0.7)
$\checkmark$		×	81.5 (+1.7)
$\checkmark$	×	$\checkmark$	80.9 (+1.1)
$\checkmark$	$\checkmark$	$\checkmark$	82.4 (+2.8)

Table 4: Ablation study of different steps in AlignedCoT. Backbone: GPT-3.5-Turbo (OpenAI, 2022). Dataset: GSM8K (Cobbe et al., 2021).

Moreover, AlignedCoT can work with other CoT methods and have positive synergistic effects. For example, GPT-4 with Auto-CoT empowered by AlignedCoT results in an average improvement of 0.9%. GPT-3.5 with Complex CoT empowered by AlignedCoT improves on average 2.6%, and achieves 4.8% gain on the Penguins dataset.

We further follow the Self-Consistency method (Wang et al., 2023b) to compare Complex CoT with our proposed AlignedCoT in the case of sampling multiple reasoning paths with temperature set to 0.7, as shown in Figure 4. We evaluate the answer accuracy of gpt-3.5-turbo on GSM8K. According to the experimental results, the overall performance of our AlignedCoT significantly exceeds that of Complex CoT.

### 4.3 AlignedCoT for Logical Pitfalls

To further investigate the capability of AlignedCoT for detecting intermediate logical errors, as a qualified counterpart of handcrafted demonstrations, we conduct experiments on the 7.1% flaw questions on the original SVAMP, as described in Section 4.1. The results are shown in Table 3. And some examples are demonstrated in Figure 5. The logical error recognition rate of GPT-3.5-Turbo with AlignedCoT is 18.3%, and the GPT-4 counterpart reaches 78.9%, significantly outperforming Complex CoT. The results suggest that AlignedCoT helps LLMs to better spot logical incorrectness in questions.

<b>Example Question 1</b> Marco and his dad went strawberry picking. Together their strawberries weighed 4 pounds. Marco's strawberries weighed 19 pounds. How much more did his strawberries weigh than his dad's?	<b>Example Question 2</b> A farmer had 175 tomatoes and 77 potatoes in his garden. If he picked 172 potatoes. How many tomatoes and potatoes does he have left?
<b>CoT Output</b> Let's think step by step. Marco and his dad's strawberries together weighed 4.0 pounds. Marco's strawberries weighed 19.0 pounds. Therefore, Marco's strawberries weighed 19.0 - 4.0 = 15.0 pounds more than his dad's. Answer: 15.0	<b>CoT Output</b> Let's think step by step. The farmer started with 175 tomatoes. He picked 172 tomatoes, so he now has 175 - 172 = 3 tomatoes left. The farmer did not pick any potatoes, so he still has 77 potatoes. Therefore, the farmer has 3 tomatoes + 77 potatoes = 80 tomatoes and potatoes left. Answer: 80.0
AlignedCoT Output Let's think step by step. First, let's calculate how much Marco's dad's strawberries weighed. The total weight of the strawberries was 4 pounds, and Marco's strawberries weighed 19 pounds. So, his dad's strawberries weighed 4 pounds - 19 pounds = -15 pounds. However, since weight cannot be negative, this means that there was a mistake in the problem. Marco's strawberries cannot weigh more than the total weight of the strawberries. Therefore, the problem is incorrect and cannot be solved.	AlignedCoT Output         Let's think step by step.         First, let's calculate how many potatoes the farmer has left after he picked some.         He had 77 potatoes and picked 172 potatoes.         However, he can't pick more potatoes than he has. So, there seems to be a mistake in the question. The number of potatoes picked should be less than or equal to the number of potatoes the farmer had.         Please check the question again.

Figure 5: Two cases of logical error detection. The text in brown is GPT-4's reasoning process for discovering logical incorrectness.

Method	Prompt	GSM8K
СоТ	w/o AlignedCoT	28.1
01	w/ AlignedCoT (Ours)	29.0 (+0.9)
Complex CoT	w/o AlignedCoT	28.7
Complex Cor	w/ AlignedCoT (Ours)	29.8 (+1.1)

Table 5: Llama2-7b-chat with AlignedCoT results.

## 4.4 Ablation Study

Table 4 shows a closer analysis of the impact of each step in AlignedCoT: Probing, Refining, and Formatting. The deletion of all probing, refining, and formatting results in the baseline Complex CoT (Fu et al., 2023), whereas the inclusion of all three is the full AlignedCoT. Experiments use GPT-3.5-Turbo (OpenAI, 2022) as the backbone and are on GSM8K (Cobbe et al., 2021). The results show that solely the first step (Probing) leads to performance improvement of +0.7%. Adding the Refining or Formatting step on top of the Probing step, the performance further improves. When all three steps are deployed simultaneously, our AlignedCoT reaches 82.4%. Therefore, the Probing, Refining, and Formatting steps all contribute to AlignedCoT for multi-step reasoning, and they work best when deployed in combination. We include further ablation studies on a setting with CORRECT "native-style" prompts before the Refining step to find the pure impact of such "native-

Retriever	Example Pool	GSM8K
Random Selection	Original Data GSM8K-Align	76.5 78.0 (+1.5)
EPR (Rubin et al., 2022)	Original Data GSM8K-Conv GSM8K-Align	77.3 80.1 (+2.8) 80.9 ( <b>+3.6</b> )
Complex CoT (Fu et al., 2023)	Original 8-shot AlignedCoT 8-shot	79.6 <b>82.4 (+2.8)</b>

Table 6: Experimental results of retrieve-based methods on GSM8K. We compare the performance between the Original Data and two types of Aligned Data derived with AlignedCoT: *GSM8K-Align* and *GSM8K-Conv*.

style" prompts without intervention of refinement. Discussions are found in appendix A.

### 4.5 AlignedCoT with Smaller LMs

To investigate the generalizability and robustness of our approach, we further apply AlignedCoT to smaller language models. Specifically, we conduct experiments with the representative Llama-2-7bchat (Touvron et al., 2023). The results shown in Table 5 demonstrate the effectiveness of our AlignedCoT across different LLMs and Scales.

## 4.6 AlignedCoT for RAG

We further explore the effectiveness of AlignedCoT for retrieval-augmented generation (RAG) with incontext learning. We use AlignedCoT to overwrite training data from the original GSM8K training

Question John plans to sell all his toys and use the money to buy video games. He has 13 lego sets and he sells them for \$15 each. He ends up buying 8 video games for \$20 each and has \$5 left. How many lego sets does he still have?	AlignedCoT Output (Ours) Let's think step by step. STEP 1: Calculate the total amount of money John gets from selling the lego sets.
Ground Truth SolutionHe spent \$160 on video games because $8 \times 20 = 160$ He earned \$165 from his sale because $160 + 5 = 165$ He sold 11 lego sets because $11 \times 15 = 165$ He has 2 sets left because $13 - 11 = 2$ So the answer is 2.	John has 13 lego sets and sells them for \$15 each, so he gets 13 * $$15 = $195$ . STEP 2: Calculate the total cost of the video games.John buys 8 video games for \$20 each, so the total cost is 8 * \$20 = \$160. STEP 3: Calculate the remaining amount of money John has. John has \$5 left, so the remaining amount of money is \$5. STEP 4: Calculate the total amount of money John spent. The total amount of money John spent is \$195 (from selling the
<b>Complex CoT Output</b> Let's think step by step. John sells 13 lego sets for \$15 each, so he earns $13 * $15 = $195$ . He buys 8 video games for \$20 each, so he spends $8 * $20 = $160$ . After buying the video games, he has $$195 - $160 = $35$ left. Since he has \$5 left, he must have spent $$35 - $5 = $30$ on lego sets. Since each lego set costs \$15, he must have bought $$30 / $15 = 2$ lego sets. Therefore, John still has $13 - 2 = 11$ lego sets. The answer is $11. \ge$	lego sets) - \$160 (for the video games) + \$5 (remaining amount) = \$40. STEP 5: Calculate the number of lego sets John still has. The total amount of money John spent is \$40, which is the cost of the lego sets he still has. Since each lego set costs \$15, the number of lego sets John still has is $40 / 15 = 2.67$ . Since John cannot have a fraction of a lego set, we round down to the nearest whole number. Therefore, John still has 2 lego sets. Answer: 2

Figure 6: A case of the GSM8K dataset. We show one example in the few-show prompt and one test example from the test split. The "manual-style" CoT is colored in blue, while the "native-style" CoT is colored in green.

set: (1) We first use few-shot demonstrations as in Figure 2.A to query the LLM to output the nativestyle CoT for each sample in the training set. (2) For those samples that can not be answered correctly in the previous setting, we create a 4-shot prompt with a question, an answer in the original dataset (handcrafted), and a native-style answer from AlignedCoT. (*style conversion prompt.*) (3) For a very small proportion of examples (around 1%) that can not be answered correctly (1) and (2), we remove them from the example pool. Consequently, we obtain the overwritten data *GSM8K-Align*. Furthermore, we refer to the data generated based on *style conversion prompt* as *GSM8K-Conv*.

We choose Random Selection, Efficient Prompt Retriever (EPR) (Rubin et al., 2022), and Complex CoT (Fu et al., 2023) as baselines. Random Selection method randomly extracts 8 samples from the training set. Efficient Prompt Retriever (EPR) (Rubin et al., 2022) retrieves the most similar training instances as exemplars for a given test case. Complex CoT (Fu et al., 2023) builds prompt by selecting the examples with the most complex reasoning steps in the training set, and therefore also serves as a strong baseline of the retrieve methods.

Table 6 shows the results of AlignedCoT for RAG. Further details are in Appendix B. With our Aligned Data, we achieve +1.5%, +3.6%, and +2.8% improvement on Random Selection, EPR, and Complex CoT, respectively. Moreover, *GSM8K-Conv* achieves +2.8% improvement with

the EPR retriever, inferior to the *GSM8K-Align* counterpart. The results suggest that AlignedCoT is consistently effective for generalized in-context learning settings. The *GSM8K-Align* will be released later. We hope it provides a resource and support to the in-context RAG study.

## 4.7 Case Study

Figure 6 demonstrates a comparing case between LLM's "native style" by AlignedCoT and "manual style" CoT. Given the test question, we compare the ground truth answer, LLM ouptut prompted by Complex CoT, and output by AlignedCoT CoT, respectively. Compared to the "manual-style" Complex CoT deriving an incorrect answer, the "native-style" AlignedCoT CoT provides clear intermediate steps for deriving the correct answer. The AlignedCoT CoT is also a detailed expansion of the ground truth solution.

## 5 Conclusion

This paper proposes a new zero-shot prompting approach Aligned Chain-of-Thought (AlignedCoT), which elicits LLMs' "native style" thinking process for leveraging their profound embedded knowledge for effective multi-step reasoning. AlignedCoT operates in proving, refining, and formatting to obtain competing "native-style" CoTs with handcrafted demonstrations. Experiments suggest multiple advantages of AlignedCoT: 1) AlignedCoT is demonstrated effective for multi-step reasoning tasks. Moreover, it can be easily combined with CoT, Complex CoT, and self-consistency and achieve further improvements. 2) AlignedCoT enhances LLMs' capability of detecting logical errors in reasoning questions. 3) AlignedCoT benefits generalized CoT scenarios including retrievalaugmentated generation.

# 6 Limitations and Ethical Considerations

Due to resource limitations, we are unable to test the proposed approach on more benchmarks. Similarly, we can not test the performance based on selfconsistency on each benchmark, because the number of samples is proportional to the cost. Moreover, future research endeavors can focus on probing more accurate native styles of LLM and combining the retrieve-based prompting method with native style data. Future studies can also try to combine AlignedCoT with other in-context learning approaches to further improve LLMs.

The data and annotations are collected without personal or confidential information. Therefore, we believe that there is no ethical concern.

### Acknowledgements

Jing Tang's work is partially supported by National Key R&D Program of China under Grant No. 2023YFF0725100, by the National Natural Science Foundation of China (NSFC) under Grant No. 62402410 and U22B2060, by National Language Commission under Grant No. WT145-39, by The Department of Science and Technology of Guangdong Province under Grant No. 2023A1515110131, and by Guangzhou Municipal Science and Technology Bureau under Grant No. 2023A03J0667 and 2024A04J4454.

### References

- BIG bench authors. 2023. Beyond the imitation game: Quantifying and extrapolating the capabilities of language models. *Transactions on Machine Learning Research*.
- Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei.

2020. Language models are few-shot learners. In *Proceedings of the 34th International Conference on Neural Information Processing Systems*, NIPS'20, Red Hook, NY, USA. Curran Associates Inc.

- Karl Cobbe, Vineet Kosaraju, Mohammad Bavarian, Mark Chen, Heewoo Jun, Lukasz Kaiser, Matthias Plappert, Jerry Tworek, Jacob Hilton, Reiichiro Nakano, Christopher Hesse, and John Schulman. 2021. Training verifiers to solve math word problems.
- Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. 2019. BERT: Pre-training of deep bidirectional transformers for language understanding. In Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers), pages 4171–4186, Minneapolis, Minnesota. Association for Computational Linguistics.
- Yao Fu, Hao Peng, Ashish Sabharwal, Peter Clark, and Tushar Khot. 2023. Complexity-based prompting for multi-step reasoning. In *The Eleventh International Conference on Learning Representations*.
- Luyu Gao, Aman Madaan, Shuyan Zhou, Uri Alon, Pengfei Liu, Yiming Yang, Jamie Callan, and Graham Neubig. 2023. Pal: Program-aided language models. In *Proceedings of the 40th International Conference on Machine Learning*, ICML'23. JMLR.org.
- Mor Geva, Daniel Khashabi, Elad Segal, Tushar Khot, Dan Roth, and Jonathan Berant. 2021. Did aristotle use a laptop? a question answering benchmark with implicit reasoning strategies. *Transactions of the Association for Computational Linguistics*, 9:346– 361.
- Shibo Hao, Yi Gu, Haodi Ma, Joshua Jiahua Hong, Zhen Wang, Daisy Zhe Wang, and Zhiting Hu. 2023. Reasoning with language model is planning with world model.
- Mohammad Javad Hosseini, Hannaneh Hajishirzi, Oren Etzioni, and Nate Kushman. 2014. Learning to solve arithmetic word problems with verb categorization. In Proceedings of the 2014 Conference on Empirical Methods in Natural Language Processing (EMNLP), pages 523–533, Doha, Qatar. Association for Computational Linguistics.
- Jared Kaplan, Sam McCandlish, T. J. Henighan, Tom B. Brown, Benjamin Chess, Rewon Child, Scott Gray, Alec Radford, Jeff Wu, and Dario Amodei. 2020. Scaling laws for neural language models. *ArXiv*, abs/2001.08361.
- Takeshi Kojima, Shixiang (Shane) Gu, Machel Reid, Yutaka Matsuo, and Yusuke Iwasawa. 2022. Large language models are zero-shot reasoners. In *Advances in Neural Information Processing Systems*, volume 35, pages 22199–22213. Curran Associates, Inc.

- Rik Koncel-Kedziorski, Hannaneh Hajishirzi, Ashish Sabharwal, Oren Etzioni, and Siena Dumas Ang. 2015. Parsing algebraic word problems into equations. Transactions of the Association for Computational Linguistics, 3:585–597.
- Xiaonan Li, Kai Lv, Hang Yan, Tianyang Lin, Wei Zhu, Yuan Ni, Guotong Xie, Xiaoling Wang, and Xipeng Qiu. 2023a. Unified demonstration retriever for incontext learning. In *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pages 4644–4668, Toronto, Canada. Association for Computational Linguistics.
- Yifei Li, Zeqi Lin, Shizhuo Zhang, Qiang Fu, Bei Chen, Jian-Guang Lou, and Weizhu Chen. 2023b. Making language models better reasoners with step-aware verifier. In Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), pages 5315–5333, Toronto, Canada. Association for Computational Linguistics.
- Wang Ling, Dani Yogatama, Chris Dyer, and Phil Blunsom. 2017. Program induction by rationale generation: Learning to solve and explain algebraic word problems. In Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), pages 158–167, Vancouver, Canada. Association for Computational Linguistics.
- Jiachang Liu, Dinghan Shen, Yizhe Zhang, Bill Dolan, Lawrence Carin, and Weizhu Chen. 2022. What makes good in-context examples for GPT-3? In Proceedings of Deep Learning Inside Out (DeeLIO 2022): The 3rd Workshop on Knowledge Extraction and Integration for Deep Learning Architectures, pages 100–114, Dublin, Ireland and Online. Association for Computational Linguistics.
- Pengfei Liu, Weizhe Yuan, Jinlan Fu, Zhengbao Jiang, Hiroaki Hayashi, and Graham Neubig. 2023. Pretrain, prompt, and predict: A systematic survey of prompting methods in natural language processing. *ACM Comput. Surv.*, 55(9).
- Jieyi Long. 2023. Large language model guided tree-ofthought.
- Yao Lu, Max Bartolo, Alastair Moore, Sebastian Riedel, and Pontus Stenetorp. 2022. Fantastically ordered prompts and where to find them: Overcoming fewshot prompt order sensitivity. In *Proceedings of the* 60th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers), pages 8086–8098, Dublin, Ireland. Association for Computational Linguistics.
- Harsha Nori, Yin Tat Lee, Sheng Zhang, Dean Carignan, Richard Edgar, Nicolo Fusi, Nicholas King, Jonathan Larson, Yuanzhi Li, Weishung Liu, et al. 2023. Can generalist foundation models outcompete special-purpose tuning? case study in medicine. *Medicine*, 84(88.3):77–3.
- OpenAI. 2022. Introducing chatgpt.

- OpenAI. 2023. GPT-4 technical report. CoRR, abs/2303.08774.
- Arkil Patel, Satwik Bhattamishra, and Navin Goyal. 2021. Are NLP models really able to solve simple math word problems? In Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, pages 2080–2094, Online. Association for Computational Linguistics.
- Alec Radford and Karthik Narasimhan. 2018. Improving language understanding by generative pretraining. In *openai.com*.
- Colin Raffel, Noam Shazeer, Adam Roberts, Katherine Lee, Sharan Narang, Michael Matena, Yanqi Zhou, Wei Li, and Peter J. Liu. 2020. Exploring the limits of transfer learning with a unified text-to-text transformer. J. Mach. Learn. Res., 21(1).
- Ohad Rubin, Jonathan Herzig, and Jonathan Berant. 2022. Learning to retrieve prompts for in-context learning. In Proceedings of the 2022 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, pages 2655–2671, Seattle, United States. Association for Computational Linguistics.
- Taylor Shin, Yasaman Razeghi, Robert L. Logan IV, Eric Wallace, and Sameer Singh. 2020. AutoPrompt: Eliciting Knowledge from Language Models with Automatically Generated Prompts. In Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing (EMNLP), pages 4222–4235, Online. Association for Computational Linguistics.
- Hongjin Su, Jungo Kasai, Chen Henry Wu, Weijia Shi, Tianlu Wang, Jiayi Xin, Rui Zhang, Mari Ostendorf, Luke Zettlemoyer, Noah A. Smith, and Tao Yu. 2022. Selective annotation makes language models better few-shot learners.
- Hongjin Su, Jungo Kasai, Chen Henry Wu, Weijia Shi, Tianlu Wang, Jiayi Xin, Rui Zhang, Mari Ostendorf, Luke Zettlemoyer, Noah A. Smith, and Tao Yu. 2023. Selective annotation makes language models better few-shot learners. In *The Eleventh International Conference on Learning Representations*.
- Mirac Suzgun, Nathan Scales, Nathanael Schärli, Sebastian Gehrmann, Yi Tay, Hyung Won Chung, Aakanksha Chowdhery, Quoc Le, Ed Chi, Denny Zhou, and Jason Wei. 2023. Challenging BIG-bench tasks and whether chain-of-thought can solve them. In Findings of the Association for Computational Linguistics: ACL 2023, pages 13003–13051, Toronto, Canada. Association for Computational Linguistics.
- Alon Talmor, Jonathan Herzig, Nicholas Lourie, and Jonathan Berant. 2019. CommonsenseQA: A question answering challenge targeting commonsense knowledge. In Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers), pages

4149–4158, Minneapolis, Minnesota. Association for Computational Linguistics.

- Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, et al. 2023. Llama 2: Open foundation and fine-tuned chat models. *arXiv preprint arXiv:2307.09288*.
- Jinyuan Wang, Junlong Li, and Hai Zhao. 2023a. Selfprompted chain-of-thought on large language models for open-domain multi-hop reasoning. In *Findings of the Association for Computational Linguistics: EMNLP 2023*, pages 2717–2731.
- Xuezhi Wang, Jason Wei, Dale Schuurmans, Quoc V Le, Ed H. Chi, Sharan Narang, Aakanksha Chowdhery, and Denny Zhou. 2023b. Self-consistency improves chain of thought reasoning in language models. In *The Eleventh International Conference on Learning Representations*.
- Yan Wang, Xiaojiang Liu, and Shuming Shi. 2017. Deep neural solver for math word problems. In Proceedings of the 2017 Conference on Empirical Methods in Natural Language Processing, pages 845–854, Copenhagen, Denmark. Association for Computational Linguistics.
- Jason Wei, Yi Tay, Rishi Bommasani, Colin Raffel, Barret Zoph, Sebastian Borgeaud, Dani Yogatama, Maarten Bosma, Denny Zhou, Donald Metzler, Ed H. Chi, Tatsunori Hashimoto, Oriol Vinyals, Percy Liang, Jeff Dean, and William Fedus. 2022a. Emergent abilities of large language models.
- Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, brian ichter, Fei Xia, Ed Chi, Quoc V Le, and Denny Zhou. 2022b. Chain-of-thought prompting elicits reasoning in large language models. In Advances in Neural Information Processing Systems, volume 35, pages 24824–24837. Curran Associates, Inc.
- Jing Xiong, Zixuan Li, Chuanyang Zheng, Zhijiang Guo, Yichun Yin, Enze Xie, Zhicheng Yang, Qingxing Cao, Haiming Wang, Xiongwei Han, Jing Tang, Chengming Li, and Xiaodan Liang. 2023. Dq-lore: Dual queries with low rank approximation re-ranking for in-context learning.
- Zhicheng Yang, Jinghui Qin, Jiaqi Chen, and Xiaodan Liang. 2022a. Unbiased math word problems benchmark for mitigating solving bias. In *Findings of the Association for Computational Linguistics: NAACL* 2022, pages 1401–1408, Seattle, United States. Association for Computational Linguistics.
- Zhicheng Yang, Jinghui Qin, Jiaqi Chen, Liang Lin, and Xiaodan Liang. 2022b. LogicSolver: Towards interpretable math word problem solving with logical prompt-enhanced learning. In *Findings of the Association for Computational Linguistics: EMNLP* 2022, pages 1–13, Abu Dhabi, United Arab Emirates. Association for Computational Linguistics.

- Shunyu Yao, Dian Yu, Jeffrey Zhao, Izhak Shafran, Thomas L. Griffiths, Yuan Cao, and Karthik Narasimhan. 2023. Tree of thoughts: Deliberate problem solving with large language models.
- Jiacheng Ye, Zhiyong Wu, Jiangtao Feng, Tao Yu, and Lingpeng Kong. 2023. Compositional exemplars for in-context learning. In *Proceedings of the 40th International Conference on Machine Learning*, ICML'23. JMLR.org.
- Yifan Zhang, Jingqin Yang, Yang Yuan, and Andrew Chi-Chih Yao. 2023a. Cumulative reasoning with large language models.
- Zhuosheng Zhang, Aston Zhang, Mu Li, and Alex Smola. 2023b. Automatic chain of thought prompting in large language models. In *The Eleventh International Conference on Learning Representations*, *ICLR 2023, Kigali, Rwanda, May 1-5, 2023*. Open-Review.net.
- Jiachen Zhao, Zonghai Yao, Zhichao Yang, and Hong Yu. 2023. Self-explain: Teaching large language models to reason complex questions by themselves. *arXiv preprint arXiv:2311.06985*.
- Zihao Zhao, Eric Wallace, Shi Feng, Dan Klein, and Sameer Singh. 2021. Calibrate before use: Improving few-shot performance of language models. In Proceedings of the 38th International Conference on Machine Learning, volume 139 of Proceedings of Machine Learning Research, pages 12697–12706. PMLR.
- Denny Zhou, Nathanael Schärli, Le Hou, Jason Wei, Nathan Scales, Xuezhi Wang, Dale Schuurmans, Claire Cui, Olivier Bousquet, Quoc V Le, and Ed H. Chi. 2023. Least-to-most prompting enables complex reasoning in large language models. In *The Eleventh International Conference on Learning Representations*.

# Appendix

# A Performance Improvement of "Native-Style" Prompt

In order to further clarify whether the enhancements are mainly attributed to our "native-style" CoT or the refinement, we conducted the following experiments: For the original Complex CoT prompt of GSM8K, we delete the examples that can not be answered correctly by GPT-3.5-Turbo. We denote this prompt as "ComplexCoT\*" and its Aligned Prompt is "ComplexCoT\*-Align". Further, we also sampled two few-shot prompts, all of the examples can be answered correctly by GPT-3.5-Turbo. They are denoted as "Prompt-1" and "Prompt-2", respectively, and their Aligned Prompt is denoted as "Align-1" and "Align-2". Under such an experimental setup, we can ensure that our AlignedCoT does not involve the refinement step, thus being able to measure the impact of the "native-style" prompt on the performance of LLMs. The results are shown in Table 7. The experimental results show that without refinement, the "native-style" prompt significantly improves model performance. We also believe that the improvement of AlignedCoT on model performance mainly comes from the "native-style" prompt, and refinement reduces the misleading of wrong examples to LLMs on this basis.

Prompt	GSM8K
ComplexCoT*	79.8
ComplexCoT*-Align	81.9 (+2.3)
Prompt-1	76.8
Align-1	77.9 (+1.3)
Prompt-2	78.0
Align-2	79.5 (+1.5)

Example Pool	Original CoT Acc	AlignedCoT Acc
random selection 1	76.9	79.5 (+2.6)
random selection 2	77.1	78.4 (+1.3)
random selection 3	75.5	76.1 (+0.6)
avg	76.5	78.0(+1.5)

Table 7: Performance without influenceof Refinement.

Table 8: Consistent improvements on Random Selection exam-	
ples.	

# **B** Consistent Improvement of AlignedCoT across Random Selection Examples

Our approach has shown consistent performance improvements in the settings of different few-shot examples. In the Random Selection method, we randomly select 8 samples to construct a few-shot prompt. This procedure is repeated 3 times to ensure statistical robustness, following which we computed the average accuracy to accurately gauge the method's effectiveness. The test accuracy of the 3 prompts obtained from random selection is shown in Table 8.

# C Examples of Refinement and Formatting in AlignedCoT

In this section, we show some examples of Refinement (Step 2) and Formatting (Step 3) in our AlignedCoT.

# C.1 Example of Refinement

Figure 9 shows an example of our Refinement process. Human modification part is colored in brown.

Refined CoT	Formatted CoT
Question: Angelo and Melanie want	Question: Angelo and Melanie want
Solution: Let's think step by step.	Solution: Let's think step by step.
STEP 1: Calculate the total time needed to study the	STEP 1: Calculate the total time needed to study the
textbook chapters.	textbook chapters.
They have 2 chapters of their textbook to study, and they	They have 2 chapters of their textbook to study, and they
plan to dedicate 3 hours to each chapter.	plan to dedicate 3 hours to each chapter.
Therefore, they should plan to study for a total of 6 days	Answer: 6
over the next week.	Question: Bella has two times as many marbles
Question: Bella has two times as many marbles	Solution: Let's think step by step.
Solution: Let's think step by step.	<b>STEP 1</b> : Calculate the number of marbles she currently has.
1. Bella currently has 60 marbles	
	Together, Bella will have a total of $14+42+84 = 140$ items.
Together, Bella will have a total of $14+42+84 = 140$ items.	Answer: 140
< more examples>	< more examples>
	step format answer format

Figure 7: An illustration of formatting answer text and solution steps on GSM8K.

Refined CoT	Formatted CoT		
[Question]: If there are 3 cars in the parking lot and 2 more	[Question]: If there are 3 cars in the parking lot and 2 more		
cars arrive, how many cars are in the parking lot?	cars arrive, how many cars are in the parking lot?		
[Solution]:	[Solution]:		
Let's think step by step.	Let's think step by step.		
Step 1: There are 3 cars in the parking lot, then 2 more cars	Step 1: There are 3 cars in the parking lot, then 2 more cars		
arrive.	arrive.		
Step 2:	Step 2:		
[Question]: There were nine computers in the server room.	[Question]: There were nine computers in the server room.		
Five more computers were installed each day, from monday	Five more computers were installed each day, from monday		
to thursday. How many computers are now in the server	to thursday. How many computers are now in the server		
room?	room?		
[Solution]:	[Solution]:		
Let's think step by step.	Let's think step by step.		
We know that there were originally 9 computers in the	Step 1: We know that there were originally 9 computers in		
server room. Then, 5 more computers were installed each	the server room. Then, 5 more computers were installed		
day, from monday to thursday.	each day, from monday to thursday.		
There are 4 days from Monday to Thursday.	Step 2: There are 4 days from Monday to Thursday.		
So, a total of $5 * 4 = 20$ more computers were installed.	Step 3: So, a total of $5 * 4 = 20$ more computers were		
Therefore, there are now $9 + 20 = 29$ computers in the	installed.		
server room.	Step 4: Therefore, there are now $9 + 20 = 29$ computers in		
	the server room.		
< more examples>	Answer: 29		
step format answer format	< more examples>		

Figure 8: An example of formatting answer text and solution steps on GSM8K.

## C.2 Example of Formatting

For Formatting, we aim to unify the format of each examples in the few-shot prompt. This process focus on two aspects: the format of the answer text and the punctuation marks of solution steps. An illustration of this step on GSM8K is shown in Figure 7. 'Refined CoT' is the prompt we acquired after Refinement (Step 2). 'Formatted CoT' is the prompt we acquired after Formatting (Step 3), which we use as the final AlignedCoT. More specifically, for the answer text, we unify it as "Answer:", which also facilitates the extraction of the answer text. For punctuation marks of solution steps, we unify according to the most common and reasonable form in Refined CoT. In Figure 7, the form is "STEP N:". If there are no obvious punctuation marks, we don't make changes. We show some more cases of the Formatting step in Figure 8.

```
[Question]: The compound and the simple interests on a certain sum
         at the same rate of interest for two years are Rs.11730 and Rs.10200
         respectively. Find the sum
         [Options]: A)Rs.17037, B)Rs.17000, C)Rs.17276, D)Rs.170287,
         E)Rs.171881
         [Solution]:
         Let's think step by step.
1<sup>st</sup> Gen Let the principal sum be P and the rate of interest be R%.
         Let's first give the formulas for compound interest (CI) and simple
         interest (SI).
         CI = P(1 + r/100)^n - P
   1<sup>st</sup>
\begin{array}{l} \mathbf{I}^{st} \\ \mathbf{Modify} \\ \mathbf{SI} = \mathbf{P} * \mathbf{r} * \mathbf{n}/100 \\ \text{Where,} \end{array}
         P = Principal amount
         r = Rate of interest
         n = The number of interest periods, which should be an integer.
         Given that the compound interest (CI) and the simple interest (SI)
2<sup>st</sup> Gen for 2 years is Rs. 11730 and Rs. 10200 respectively.
  2<sup>st</sup> Let's assume the principal amount (P) as x.
Modify So, we have CI = Rs. 11730, SI = Rs. 10200, and n = 2.
         Substituting these values in the formulas, we have:
         11730 = P(1 + r/100)^2 - P
3^{st} Gen 10200 = P * r * 2/100
         Now, let's solve the equations to find P.
         From the second equation, we can rewrite it as:
         r = 10200 * 100 / (P * 2)
  2st
        Substituting this value of r in the first equation
Modify r = 510000 / P
4<sup>st</sup> Gen Substituting this value of r in the first equation, we have:

11730 = P(1 + (510000 / P)/100)^{2} - P
  4st
        Simplifying the equation, we get:
Modify 11730 = P(1 + 5100/P)^2 - P
         11730 = P(1 + 5100/P)(1 + 5100/P) - P
5^{\text{st}} Gen 11730 = P(1 + 2 * 5100/P + 5100^2/P^2) - P
         11730 = P(1 + 10200/P + (5100/P)^2) - P
   5st
         11730 = P + 10200 + 5100(P/P)^2 - P
Modify 11730 = P + 2*5100 + 5100^{2}/P - P
         11730 = 10200 + 5100^{2}/P
         1530 = 5100^{2}/P
         P = 5100^{2}/1530
6^{st} \text{ Gen } \stackrel{P = 5100}{P = 2601000/1530}
         P = 17000
         Therefore, the sum is Rs. 17000.
         Hence, the correct option is B) Rs. 17000.
```

Figure 9: A case of Refinement on Complex CoT for AQUA.

# **D** The Amount of Refinement in AlignedCoT

In our AlignedCoT, the proportion of refinement intervention is low, which demonstrates one of the superiorities of our approach. We present the percentage of samples involved in the Refinement stage for the different few-shot prompts in Table 9 and Table 10. "Refined/All" indicates the ratio of the number of refined examples to the total number of examples. Overall, in our AlignedCoT, GPT-3.5-turbo only requires refinement for 11% of the examples in the prompts of the benchmarks we evaluated, whereas GPT-4 only needs 4% (two examples).

Prompt	GSM8K	AQUA	SVAMP*	AddSub	SingleEQ	Penguins	Total	
СоТ	0/8	1/4	0/8	0/8	0/8	0/3	9/82=11%	
Complex CoT	2/8	3/8	1/8	1/8	1/8	0/3	9/82=11%	

Table 9: The proportion of refinement intervention for GPT-3.5-Turbo. The right side of the semicolon '/' represents the number of examples in the prompt, and the left side indicates the number of examples involved in refinement.

Prompt	GSM8K	AQUA	SVAMP*	Penguins	Total	
СоТ	0/8	0/4	0/8	0/3	2/50=4%	
Complex CoT	0/8	2/8	0/8	0/3	2/30=4%	

Table 10: The proportion of refinement intervention for GPT-3.5-Turbo. The right side of the semicolon '/' represents the number of examples in the prompt, and the left side indicates the number of examples involved in refinement.

# **E** Full Set of Prompts

We show all the prompts we used in this section. These prompts are also released in our github repo.

E.1 CoT w/ AlignedCoT exemplars for GSM8K, SVAMP, AddSub, and SingleEQ

AlignedCoT For GPT-3.5-Turbo	
[Question]: There are 15 trees in the grove. Grove workers will plant trees in the grove today. After the there will be 21 trees. How many trees did the grove workers plant today? [Solution]: Let's think step by step. Step 1: We know that there are originally 15 trees in the grove, and after the grove workers plant trees, there trees. Step 2: The workers planted 21 - 15 = 6 trees today. Step 3: Therefore, the grove workers planted 6 trees today. Answer: 6	
<ul> <li>[Question]: If there are 3 cars in the parking lot and 2 more cars arrive, how many cars are in the lot?</li> <li>[Solution]:</li> <li>Let's think step by step.</li> <li>Step 1: We know that there are originally 3 cars in the parking lot, and then 2 more cars arrive.</li> <li>Step 2: Therefore, there are 3 + 2 = 5 cars in the parking lot.</li> <li>Answer: 5</li> </ul>	he parking
<ul> <li>[Question]: Leah had 32 chocolates and her sister had 42. If they ate 35, how many pieces do left in total?</li> <li>[Solution]:</li> <li>Let's think step by step.</li> <li>Step 1: We know that Leah had 32 chocolates and her sister had 42. They ate 35 pieces.</li> <li>Step 2: Leah and her sister had 32 + 42 = 74 chocolates in total.</li> <li>Step 3: After eating 35 chocolates, they have 74 - 35 = 39 chocolates left.</li> <li>Step 4: Therefore, they have 39 chocolates left in total.</li> <li>Answer: 39</li> </ul>	they have
<ul> <li>[Question]: Jason had 20 lollipops. He gave Denny some lollipops. Now Jason has 12 lollipop many lollipops did Jason give to Denny?</li> <li>[Solution]:</li> <li>Let's think step by step.</li> <li>Step 1: We know that Jason originally had 20 lollipops, and after giving some to Denny, he now has 12 loll Step 2: Therefore, Jason gave 20 - 12 = 8 lollipops to Denny.</li> <li>Answer: 8</li> </ul>	-
[Question]: Shawn has five toys. For Christmas, he got two toys each from his mom and dad. It toys does he have now? [Solution]: Let's think step by step. Step 1: We know that Shawn originally has 5 toys, and then he gets 2 toys each from his mom and dad for the step of	

Step 2: The total number of toys he got for Christmas is 2 + 2 = 4. Step 3: After Christmas, Shawn has 5 + 4 = 9 toys. Step 4: Therefore, Shawn has 9 toys now. Answer: 9 [Question]: There were nine computers in the server room. Five more computers were installed each day, from monday to thursday. How many computers are now in the server room? [Solution]: Let's think step by step. Step 1: We know that there were originally 9 computers in the server room. Then, 5 more computers were installed each day, from monday to thursday. Step 2: There are 4 days from Monday to Thursday. Step 3: So, a total of 5 \* 4 = 20 more computers were installed. Step 4: Therefore, there are now 9 + 20 = 29 computers in the server room. Answer: 29 [Question]: Michael had 58 golf balls. On tuesday, he lost 23 golf balls. On wednesday, he lost 2 more. How many golf balls did he have at the end of wednesday? [Solution]: Let's think step by step. Step 1: We know that Michael had 58 golf balls. On tuesday, he lost 23 golf balls. On wednesday, he lost 2 more. Step 2: After he lost 23 golf balls, he had 58 - 23 = 35 golf balls left. Step 3: After he lost 2 more, he had 35 - 2 = 33 golf balls left. Step 4: Therefore, at the end of Wednesday, Michael had 33 golf balls. Answer: 33 [Question]: Olivia has \$23. She bought five bagels for \$3 each. How much money does she have left? [Solution]: Let's think step by step. Step 1: We know that Olivia has \$23 and she bought five bagels for \$3 each. Step 2: The total cost of the bagels is 5 \* \$3 = \$15. Step 3: After buying the bagels, Olivia has 23 - 15 = 8 left. Step 4: Therefore, Olivia has \$8 left.

Answer: 8

#### AlignedCoT For GPT-4

[Question]: There are 15 trees in the grove. Grove workers will plant trees in the grove today. After they are done, there will be 21 trees. How many trees did the grove workers plant today? [Solution]: Let's think step by step. First, we know that there were originally 15 trees in the grove. Then, the grove workers planted some trees. After they finished, there were 21 trees in total. So, to find out how many trees they planted, we subtract the original number of trees from the final number of trees. That is, 21 - 15 = 6. So, the grove workers planted 6 trees today. Answer: 6. [Question]: If there are 3 cars in the parking lot and 2 more cars arrive, how many cars are in the parking lot? [Solution]: Let's think step by step. First, there were 3 cars in the parking lot. Then, 2 more cars arrived. So, we add the number of cars that were already there (3) to the number of cars that arrived (2). 3 + 2 = 5So, there are 5 cars in the parking lot. Answer: 5. [Question]: Leah had 32 chocolates and her sister had 42. If they ate 35, how many pieces do they have left in total? [Solution]: Let's think step by step. First, we add the number of chocolates Leah and her sister had together. That is 32 + 42 = 74 chocolates. Then, we subtract the number of chocolates they ate from the total number of chocolates they had. That is 74 - 35 = 39chocolates.

So, they have 39 pieces of chocolates left in total. Answer: 39. [Question]: Jason had 20 lollipops. He gave Denny some lollipops. Now Jason has 12 lollipops. How many lollipops did Jason give to Denny? [Solution]: Let's think step by step. First, Jason had 20 lollipops. Then he gave some to Denny and now he has 12 lollipops. So, to find out how many lollipops Jason gave to Denny, we need to subtract the number of lollipops Jason has now from the number he had at the beginning. So, 20 - 12 = 8. Therefore, Jason gave 8 lollipops to Denny. Answer: 8. [Question]: Shawn has five toys. For Christmas, he got two toys each from his mom and dad. How many toys does he have now? [Solution]: Let's think step by step. First, Shawn had five toys. Then, he got two toys from his mom, so he had 5 + 2 = 7 toys. Finally, he got two more toys from his dad, so he now has 7 + 2 = 9 toys. So, Shawn now has 9 toys. Answer: 9. [Question]: There were nine computers in the server room. Five more computers were installed each day, from monday to thursday. How many computers are now in the server room? [Solution]: Let's think step by step. There were originally 9 computers. Five more computers were installed each day from Monday to Thursday. That's 4 days. So, 5 computers \*4 days = 20 computers were added. So, the total number of computers now in the server room is 9 (original) + 20 (added) = 29 computers. Answer: 29. [Question]: Michael had 58 golf balls. On tuesday, he lost 23 golf balls. On wednesday, he lost 2 more. How many golf balls did he have at the end of wednesday? [Solution]: Let's think step by step. First, Michael lost 23 golf balls on Tuesday. So, 58 - 23 = 35 golf balls remained. Then, he lost 2 more golf balls on Wednesday. So, 35 - 2 = 33 golf balls remained. Therefore, Michael had 33 golf balls at the end of Wednesday. Answer: 33. [Question]: Olivia has \$23. She bought five bagels for \$3 each. How much money does she have left? [Solution]: Let's think step by step. First, we need to find out how much Olivia spent on bagels. She bought 5 bagels for 3 each, so she spent 5 \* 3 = 15. Then, we subtract the amount she spent from the amount she had. She had 23 and spent 15, so she has 23 - 15 = 8left. Therefore, Olivia has left \$8. Answer: 8.

# E.2 Complex CoT w/ AlignedCoT exemplars for GSM8K

### AlignedCoT For GPT-3.5-Turbo

**[Question]**: Angelo and Melanie want to plan how many hours over the next week they should study together for their test next week. They have 2 chapters of their textbook to study and 4 worksheets to memorize. They figure out that they should dedicate 3 hours to each chapter of their textbook and 1.5 hours for each worksheet. If they plan to study no more than 4 hours each day, how many days should they plan to study total over the next week if they take a 10-minute break every hour, include 3 10-minute snack breaks each day, and 30 minutes for lunch each day? **[Solution]**:

Let's think step by step.

STEP 1: Calculate the total time needed to study the textbook chapters.

They have 2 chapters of their textbook to study, and they plan to dedicate 3 hours to each chapter.

So, the total time needed to study the textbook chapters is 2 \* 3 = 6 hours.

STEP 2: Calculate the total time needed to memorize the worksheets.

They have 4 worksheets to memorize, and they plan to dedicate 1.5 hours for each worksheet.

So, the total time needed to memorize the worksheets is 4 \* 1.5 = 6 hours.

STEP 3: Calculate the total time needed for breaks and meals each day.

They take a 10-minute break every hour, so in a 4-hour study session, they will have 4 \* 10 = 40 minutes of breaks. They also have 3 10-minute snack breaks each day, so they will have 3 \* 10 = 30 minutes of snack breaks.

They have 30 minutes for lunch each day.

So, the total time needed for breaks and meals each day is 40 + 30 + 30 = 100 minutes, which is equal to 100/60 = 1.67 hours.

STEP 4: Calculate the total time needed to study each day.

They plan to study no more than 4 hours each day, and they need to subtract the time needed for breaks and meals. So, the total time they can study each day is 4 - 1.67 = 2.33 hours.

So, the total time they can study each day is 4 - 1.07 = 2.33 no STEP 5: Calculate the total number of days needed to study.

They need a total of 6 hours to study the textbook chapters and 6 hours to memorize the worksheets.

So, the total time needed to study is 6 + 6 = 12 hours.

Since they can study 2.33 hours each day, they will need 12/2.33 = 5.15 days to complete their study.

Since they can't study for a fraction of a day, they should plan to study for 6 days.

Therefore, they should plan to study for a total of 6 days over the next week.

Answer: 6

**[Question]**: Mark's basketball team scores 25 2 pointers, 8 3 pointers and 10 free throws. Their opponents score double the 2 pointers but half the 3 pointers and free throws. What's the total number of points scored by both teams added together?

[Solution]:

Let's think step by step.

STEP 1: Calculate the number of points scored by Mark's team.

Mark's team scores 25 2 pointers, which means they score 25 \* 2 = 50 points from 2 pointers.

They also score 8 3 pointers, which means they score 8 \* 3 = 24 points from 3 pointers.

Finally, they score 10 free throws, which means they score 10 \* 1 = 10 points from free throws.

Therefore, the total number of points scored by Mark's team is 50 + 24 + 10 = 84 points.

STEP 2: Calculate the number of points scored by the opponents.

The opponents score double the 2 pointers, which means they score 2 \* 50 = 100 points from 2 pointers.

They also score half the 3 pointers, which means they score 0.5 \* 24 = 12 points from 3 pointers.

Finally, they score half the free throws, which means they score 0.5 \* 10 = 5 points from free throws.

Therefore, the total number of points scored by the opponents is 100 + 12 + 5 = 117 points.

STEP 3: Calculate the total number of points scored by both teams.

The total number of points scored by both teams is 84 + 117 = 201 points.

Answer: 201

**[Question]**: Bella has two times as many marbles as frisbees. She also has 20 more frisbees than deck cards. If she buys 2/5 times more of each item, what would be the total number of the items she will have if she currently has 60 marbles?

[Solution]:

Let's think step by step.

STEP 1: Calculate the number of marbles she currently has.

When Bella buys 2/5 times more marbles, she'll have increased the number of marbles by 2/5\*60 = 24

The total number of marbles she'll have is 60+24 = 84

STEP 2: Calculate the number of frisbees she currently has.

If Bella currently has 60 marbles, and she has two times as many marbles as frisbees, she has 60/2 = 30 frisbees.

If Bella buys 2/5 times more frisbees, she'll have 2/5\*30 = 12 more frisbees.

The total number of frisbees she'll have will increase to 30+12 = 42

STEP 3: Calculate the number of deck cards she currently has.

Bella also has 20 more frisbees than deck cards, meaning she has 30-20 = 10 deck cards

If she buys 2/5 times more deck cards, she'll have 2/5\*10 = 4 more deck cards.

The total number of deck cards she'll have is 10+4 = 14

STEP 4: Calculate the total number of items she'll have If she buys 2/5 times more of each item.

Together, Bella will have a total of 14+42+84 = 140 items

Answer: 140

**[Question]**: A group of 4 fruit baskets contains 9 apples, 15 oranges, and 14 bananas in the first three baskets and 2 less of each fruit in the fourth basket. How many fruits are there? **[Solution]**:

Let's think step by step.

STEP 1: Figure out the total number of fruits in the first three baskets.

In each of the first three basket, there are 9 apples + 15 oranges + 14 bananas = 38 fruits.

So, in the first three baskets, there are a total of 38 fruits \* 3 = 114 fruits.

STEP 2: Figure out the number of fruits in the fourth basket.

In the fourth basket, there are 2 less of each fruit compared to the first three baskets.

So, there are 9 apples - 2 = 7 apples.

There are 15 oranges - 2 = 13 oranges. There are 14 bananas - 2 = 12 bananas. Therefore, in the fourth basket, there are a total of 7 apples + 13 oranges + 12 bananas = 32 fruits. STEP 3: Figure out the total number of fruits in all four baskets. The four baskets together have 114 (total fruits in the first three baskets) + 32 (fruits in the fourth basket) = 146 fruits. Answer: 146 [Question]: You can buy 4 apples or 1 watermelon for the same price. You bought 36 fruits evenly split between oranges, apples and watermelons, and the price of 1 orange is \$0.50. How much does 1 apple cost if your total bill was \$66? [Solution]: Let's think step by step. STEP 1: Calculate the number of each kind of fruit you bought. We also know that you bought 36 fruits evenly split between oranges, apples, and watermelons. So, you bought 36/3 =12 for each kind of fruit. STEP 2: Calculate the total cost of the oranges. We know that the price of 1 orange is \$0.50. So, the total cost of all the oranges is 12 \* \$0.50 = \$6. STEP 3: Define the variable. Let's assume the cost of 1 apple is x dollars. STEP 4: Establish an equation according to: the sum of the cost of each kind of fruit (apple, watermelon, and watermelon) equals to the total cost \$66. So, the total cost of all the apples is 12 \* x = 12x dollars. We are given that you can buy 4 apples or 1 watermelon for the same price. So, the cost of 1 watermelon is also 4xdollars. The total cost of all the watermelons is 12 \* 4x = 48x dollars. We know that the total bill was \$66. Therefore, we can write the equation: \$6 + 12x + 48x = \$66. STEP 5: Solve the equation and get the answer. Simplifying the equation, we get 6 + 60x = 66. Subtracting \$6 from both sides, we get 60x = \$60. Dividing both sides by 60, we get x =\$1. So, the cost of 1 apple is \$1. Answer: 1 [Question]: Susy goes to a large school with 800 students, while Sarah goes to a smaller school with only 300 students. At the start of the school year, Susy had 100 social media followers. She gained 40 new followers in the first week of the school year, half that in the second week, and half of that in the third week. Sarah only had 50 social media followers at the start of the year, but she gained 90 new followers the first week, a third of that in the second week, and a third of that in the third week. After three weeks, how many social media followers did the girl with the most total followers have? [Solution]: Let's think step by step. STEP 1: Figure out how many followers Susy has after three weeks. After one week, Susy has 100+40 = 140 followers. In the second week, Susy gains 40/2 = 20 new followers. In the third week, Susy gains 20/2 = 10 new followers. In total, Susy finishes the three weeks with 140+20+10 = 170 total followers. STEP 2: Figure out how many followers Sarah has after three weeks. After one week, Sarah has 50+90 = 140 followers. After the second week, Sarah gains 90/3 = 30 followers. After the third week, Sarah gains 30/3 = 10 followers. So, Sarah finishes the three weeks with 140+30+10 = 180 total followers. STEP 3: Figure out who has the most total followers. Thus, Sarah is the girl with the most total followers with a total of 180. Answer: 180 [Question]: Sam bought a dozen boxes, each with 30 highlighter pens inside, for \$10 each box. He rearranged five of these boxes into packages of six highlighters each and sold them for \$3 per package. He sold the rest of the highlighters separately at the rate of three pens for \$2. How much profit did he make in total, in dollars? [Solution]: Let's think step by step. STEP 1: Calculate the total cost of buying the boxes. Sam bought a dozen boxes, which means he bought 12 boxes in total. Each box cost \$10, so the total cost of buying the boxes is 12 \* \$10 = \$120. STEP 2: Calculate the total number of highlighters Sam bought. Each box contains 30 highlighter pens, so the total number of highlighters Sam bought is 12 \* 30 = 360 highlighters. STEP 3: Calculate the total revenue from selling the packages.

Sam rearranged five boxes into packages of six highlighters each, so he made 5 \* 30 / 6 = 25 packages.

He sold each package for \$3, so the total revenue from selling the packages is 25 \* \$3 = \$75. STEP 4: Calculate the total revenue from selling the highlighters separately. Sam sold the rest of the highlighters, which is 360 - (5 \* 30) = 210 highlighters, separately. He sold three highlighters for \$2, so the total revenue from selling the highlighters separately is (210/3) \* \$2 = \$140. STEP 5: Calculate the total revenue. The total revenue is the sum of the revenue from selling the packages and the revenue from selling the highlighters separately, which is \$75 + \$140 = \$215. STEP 6: Calculate the profit. The profit is the total revenue minus the total cost, which is \$215 - \$120 = \$95. Answer: \$95 [Ouestion]: In a certain school, 2/3 of the male students like to play basketball, but only 1/5 of the female students like to play basketball. What percent of the population of the school do not like to play basketball if the ratio of the male to female students is 3:2 and there are 1000 students? [Solution]: Let's think step by step. STEP 1: Figure out the number of male and female students in the school. The students are divided into 3 + 2 = 5 parts where 3 parts are for males and 2 parts are for females. Each part represents 1000/5 = 200 students. So, there are  $3 \times 200 = 600$  males. And there are  $2 \ge 200 = 400$  females. STEP 2: Figure out the number of males and females who like to play basketball. 2/3 of the male students like to play basketball. Hence,  $600 \ge 2/3 = 400$  males play basketball. 1/5 of the female students like to play basketball. Hence,  $400 \times 1/5 = 80$  females play basketball. STEP 3: Figure out how many people do not like to play basketball. A total of 400 + 80 = 480 students play basketball. Therefore, 1000 - 480 = 520 do not like to play basketball. STEP 4: Calculate the percentage of the population that do not like to play basketball. The percentage of the school that do not like to play basketball is 520/1000 \* 100 = 52Answer: 52 AlignedCoT For GPT-4

**[Question]**: Angelo and Melanie want to plan how many hours over the next week they should study together for their test next week. They have 2 chapters of their textbook to study and 4 worksheets to memorize. They figure out that they should dedicate 3 hours to each chapter of their textbook and 1.5 hours for each worksheet. If they plan to study no more than 4 hours each day, how many days should they plan to study total over the next week if they take a 10-minute break every hour, include 3 10-minute snack breaks each day, and 30 minutes for lunch each day?

[**Solution**]: Let's think step by step.

First, calculate the total time they need to study the textbook and worksheets. They need 3 hours for each of the 2 chapters, which is 3\*2=6 hours. They also need 1.5 hours for each of the 4 worksheets, which is 1.5\*4=6 hours. So, they need a total of 6+6=12 hours to study.

Next, calculate the total break time each day. They take a 10-minute break every hour, which is 10\*4=40 minutes. They also take 3 10-minute snack breaks, which is 3\*10=30 minutes. Plus, they take 30 minutes for lunch. So, they take a total of 40+30+30=100 minutes of breaks each day. Convert this to hours by dividing by 60, which is 100/60=1.67 hours.

Subtract the break time from the total hours they can study each day to find out how many hours they can actually study each day. They can study 4 hours each day, but they take 1.67 hours of breaks, so they can actually study 4-1.67=2.33 hours each day.

Finally, divide the total hours they need to study by the hours they can actually study each day to find out how many days they need to study. They need to study 12 hours total and can study 2.33 hours each day, so they need to study 12/2.33=5.15 days. Since they can't study for a fraction of a day, they should plan to study for 6 days. Answer: 6

**[Question]**: Mark's basketball team scores 25 2 pointers, 8 3 pointers and 10 free throws. Their opponents score double the 2 pointers but half the 3 pointers and free throws. What's the total number of points scored by both teams added together?

[Solution]:

Let's think step by step.

First, calculate the total points scored by Mark's team. A 2 pointer is worth 2 points, a 3 pointer is worth 3 points and a free throw is worth 1 point. So Mark's team scores  $25 \times 2 + 8 \times 3 + 10 \times 1 = 50 + 24 + 10 = 84$  points.

Next, calculate the total points scored by their opponents. They score double the 2 pointers, so that's 25 \* 2 \* 2 = 100 points. They score half the 3 pointers, so that's 8 \* 3 / 2 = 12 points. They also score half the free throws, so that's 1 / 2 = 5 points. So their opponents score 100 + 12 + 5 = 117 points.

Finally, add the points scored by both teams to find the total: 84 + 117 = 201 points. Answer: 201 **[Question]**: Bella has two times as many marbles as frisbees. She also has 20 more frisbees than deck cards. If she buys 2/5 times more of each item, what would be the total number of the items she will have if she currently has 60 marbles?

[Solution]:

Let's think step by step.

First, we know that Bella has two times as many marbles as frisbees. So if she has 60 marbles, she has 60/2 = 30 frisbees.

Next, we know that Bella has 20 more frisbees than deck cards. So she has 30 - 20 = 10 deck cards.

So currently, Bella has 60 marbles + 30 frisbees + 10 deck cards = 100 items.

If Bella buys 2/5 times more of each item, she will have 2/5 \* 60 = 24 more marbles, 2/5 \* 30 = 12 more frisbees, and 2/5 \* 10 = 4 more deck cards.

So in total, Bella will have 100 + 24 + 12 + 4 = 140 items. Answer: 140

**[Question]**: A group of 4 fruit baskets contains 9 apples, 15 oranges, and 14 bananas in the first three baskets and 2 less of each fruit in the fourth basket. How many fruits are there?

[Solution]: Let's think step by step.

First, we need to find out how many fruits are in the first three baskets. In each basket, there are 9 apples, 15 oranges, and 14 bananas. So, in total, there are 9+15+14 = 38 fruits in each basket. Since there are three such baskets, there are 3\*38 = 114 fruits in the first three baskets.

Next, we need to find out how many fruits are in the fourth basket. We know that there are 2 less of each fruit in the fourth basket. So, there are 9-2 = 7 apples, 15-2 = 13 oranges, and 14-2 = 12 bananas in the fourth basket. In total, there are 7+13+12 = 32 fruits in the fourth basket.

Finally, to find out how many fruits are there in total, we need to add the number of fruits in the first three baskets and the number of fruits in the fourth basket. So, there are 114+32 = 146 fruits in total. Answer: 146

**[Question]**: You can buy 4 apples or 1 watermelon for the same price. You bought 36 fruits evenly split between oranges, apples and watermelons, and the price of 1 orange is \$0.50. How much does 1 apple cost if your total bill was \$66?

#### [Solution]:

Let's think step by step.

First, since the fruits are evenly split, it means you bought 12 of each fruit (12 oranges, 12 apples, and 12 watermelons). Next, we know that the price of 1 orange is 0.50. So, the total cost for the oranges is 12 \* 0.50 = 6.

We also know that the total bill was \$66. So, the cost for the apples and watermelons is 66 - 6 = 60.

Since 4 apples cost the same as 1 watermelon, it means that 12 apples cost the same as 3 watermelons. Therefore, the cost for 12 apples and 12 watermelons (which is 15 fruits in total) is \$60.

So, the cost for 1 fruit (either an apple or a watermelon) is 60 / 15 = 4.

Therefore, since 4 apples cost 4, 1 apple costs 4 / 4 = 1

Answer: 1

**[Question]**: Susy goes to a large school with 800 students, while Sarah goes to a smaller school with only 300 students. At the start of the school year, Susy had 100 social media followers. She gained 40 new followers in the first week of the school year, half that in the second week, and half of that in the third week. Sarah only had 50 social media followers at the start of the year, but she gained 90 new followers the first week, a third of that in the second week, and a third of that in the third week. After three weeks, how many social media followers did the girl with the most total followers have?

#### [Solution]:

Let's think step by step.

In the first week, Susy gained 40 new followers, so she had 100 + 40 = 140 followers.

In the second week, she gained half of 40, which is 40/2 = 20 new followers, so she had 140 + 20 = 160 followers. In the third week, she gained half of 20, which is 20/2 = 10 new followers, so she had 160 + 10 = 170 followers. On the other hand, Sarah gained 90 new followers in the first week, so she had 50 + 90 = 140 followers.

In the second week, she gained a third of 90, which is 90/3 = 30 new followers, so she had 140 + 30 = 170 followers. In the third week, she gained a third of 30, which is 30/3 = 10 new followers, so she had 170 + 10 = 180 followers. Therefore, the girl with the most total followers after three weeks is Sarah, with 180 followers. Answer: 180

**[Question]**: Sam bought a dozen boxes, each with 30 highlighter pens inside, for \$10 each box. He rearranged five of these boxes into packages of six highlighters each and sold them for \$3 per package. He sold the rest of the highlighters separately at the rate of three pens for \$2. How much profit did he make in total, in dollars? **[Solution]**:

Let's think step by step.

First, we calculate the total cost of the boxes. Sam bought a dozen boxes, which is 12 boxes, at \$10 each. So, the total cost is 12 \* \$10 = \$20.

Next, we calculate how many highlighters Sam has in total. Each box has 30 highlighters, so 12 boxes have 12 \* 30 = 360 highlighters.

Then, we calculate how many packages of six highlighters Sam made. He rearranged five boxes into packages of six highlighters each. So, he made 5 \* 30 / 6 = 25 packages.

We calculate how much money Sam made from selling these packages. He sold them for 3 each, so he made 25 \* 3 = 75.

Next, we calculate how many highlighters Sam sold separately. He sold the rest of the highlighters separately, which is 360 - 5 \* 30 = 210 highlighters.

We calculate how much money Sam made from selling these highlighters. He sold them at the rate of three pens for \$2, so he made 210 / 3 \* \$2 = \$140.

Finally, we calculate Sam's profit. His profit is the money he made minus the cost, which is 75 + 140 - 120 = 95. So, Sam made a profit of 95

Answer: 95

**[Question]**: In a certain school, 2/3 of the male students like to play basketball, but only 1/5 of the female students like to play basketball. What percent of the population of the school do not like to play basketball if the ratio of the male to female students is 3:2 and there are 1000 students?

[Solution]:

Let's think step by step.

First, let's find out how many male and female students there are in the school. The ratio of male to female students is 3:2, which means for every 3 male students, there are 2 female students.

So, out of 5 parts (3+2), 3 parts are male and 2 parts are female.

Therefore, the number of male students is (3/5)\*1000 = 600 and the number of female students is (2/5)\*1000 = 400. Next, let's find out how many students like to play basketball.

2/3 of the male students like to play basketball, so (2/3)\*600 = 400 male students like to play basketball.

1/5 of the female students like to play basketball, so (1/5)\*400 = 80 female students like to play basketball.

So, a total of 400+80 = 480 students like to play basketball.

Therefore, the number of students who do not like to play basketball is 1000 - 480 = 520.

So, the percentage of students who do not like to play basketball is (520/1000)\*100 = 52%.

Answer: 52

# E.3 Complex CoT w/ AlignedCoT exemplars for SVAMP, AddSub, and SingleEQ

## Complex CoT we retrieved from SVAMP training set.

[Question]: Adam bought 9.0 packages of cat food and 7.0 packages of dog food. Each package of cat food contained 10.0 cans, and each package of dog food contained 5.0 cans. How many more cans of cat food than dog food did Adam buy?

[Solution]:

Let's think step by step.

Adam bought 9.0 packages of cat food, and each package contained 10.0 cans, so he bought a total of  $9.0 \times 10.0 = 90.0$  cans of cat food.

Adam also bought 7.0 packages of dog food, and each package contained 5.0 cans, so he bought a total of 7.0 \* 5.0 = 35.0 cans of dog food.

Therefore, Adam bought 90.0 - 35.0 = 55.0 more cans of cat food than dog food. Answer: 55.0

[Question]: In a bag there are 13.0 red marbles, 5.0 blue marbles, and 7.0 green marbles. What percent of

#### the marbles are green?

[Solution]:

Let's think step by step.

To find the percentage of green marbles, we need to divide the number of green marbles by the total number of marbles and then multiply by 100.

The total number of marbles is 13.0 + 5.0 + 7.0 = 25.0

The number of green marbles is 7.0

So, the percentage of green marbles is (7.0/25.0) \* 100 = 28%

Answer: 28

**[Question]**: Mika had 20.0 stickers. She bought 26.0 stickers from a store in the mall and got 20.0 stickers for her birthday. Then Mika gave 6.0 of the stickers to her sister and used 58.0 to decorate a greeting card. How many stickers does Mika have left?

[Solution]:

Let's think step by step.

Mika starts with 20.0 stickers.

She buys 26.0 stickers, so she now has 20.0 + 26.0 = 46.0 stickers.

She also receives 20.0 stickers for her birthday, so she now has 46.0 + 20.0 = 66.0 stickers.

Mika gives 6.0 stickers to her sister, so she now has 66.0 - 6.0 = 60.0 stickers.

She uses 58.0 stickers to decorate a greeting card, so she now has 60.0 - 58.0 = 2.0 stickers left.

Answer: 2.0

[Question]: Luke had 20.0 stickers. He bought 12.0 stickers from a store in the mall and got 20.0 stickers for his birthday. Then Luke gave 5.0 of the stickers to his sister and used 8.0 to decorate a greeting card. How many stickers does Luke have left? [Solution]: Let's think step by step. Luke started with 20.0 stickers. He bought 12.0 stickers, so he now has 20.0 + 12.0 = 32.0 stickers. He also received 20.0 stickers for his birthday, so he now has 32.0 + 20.0 = 52.0 stickers. He gave 5.0 stickers to his sister, so he now has 52.0 - 5.0 = 47.0 stickers. He used 8.0 stickers to decorate a greeting card, so he now has 47.0 - 8.0 = 39.0 stickers left. Answer: 39.0 [Question]: How many yards of material from a 24.0 yard length of cloth remains after 3.0 pieces each 3.5 yards long and 5.0 pieces each 2.25 long are removed? [Solution]: Let's think step by step. The total length of cloth is 24.0 yards. 3 pieces of cloth, each 3.5 yards long, are removed. So,  $3 \ge 3.5 = 10.5$  yards of cloth are removed. 5 pieces of cloth, each 2.25 yards long, are removed. So,  $5 \times 2.25 = 11.25$  yards of cloth are removed. Therefore, a total of 10.5 + 11.25 = 21.75 yards of cloth are removed. The remaining length of cloth is 24.0 - 21.75 = 2.25 yards. Answer: 2.25 [Question]: If Bob can make 100.0 feet of rope in 2.0 hours and Tim can make 75.0 feet of rope in 2.0 hours, how many feet of rope can Bob and Tim working together make in 4.0 hours? [Solution]: Let's think step by step. Bob can make 100.0 feet of rope in 2.0 hours, so his rate of production is 100.0 feet / 2.0 hours = 50.0 feet per hour. Tim can make 75.0 feet of rope in 2.0 hours, so his rate of production is 75.0 feet / 2.0 hours = 37.5 feet per hour. Working together, their combined rate of production is 50.0 feet per hour + 37.5 feet per hour = 87.5 feet per hour. In 4.0 hours, they can make 87.5 feet per hour \* 4.0 hours = 350.0 feet of rope. Answer: 350.0 [Ouestion]: A neighborhood grocer sells a mix of chocolate and carob candy. The chocolate cost 2.7 dollars a pound and the carob costs 2.55 dollars a pound. If 20.0 pounds of the chocolate and 40.0 pounds of the carob candy are used, what is the cost per pound of the mixture in dollars? [Solution]: Let's think step by step. To find the cost per pound of the mixture, we need to calculate the total cost of the chocolate and carob candy and then divide it by the total weight of the mixture. The total cost of the chocolate candy is 20.0 pounds \* \$2.7/pound = \$54. The total cost of the carob candy is 40.0 pounds \* \$2.55/pound = \$102. The total weight of the mixture is 20.0 pounds + 40.0 pounds = 60.0 pounds. Therefore, the cost per pound of the mixture is (\$54 + \$102) / 60.0 pounds = \$156 / 60.0 pounds = \$2.60/pound. Answer: 2.60 [Question]: Tim got 3.0 nickels and 13.0 dimes for shining shoes, and in his tip jar found 7.0 dimes and 9.0 half - dollars. How much money did Tim get? [Solution]: Let's think step by step. Tim got 3.0 nickels, which is equal to 3 \* \$0.05 = \$0.15. Tim also got 13.0 dimes, which is equal to 13 \* \$0.10 = \$1.30. In his tip jar, Tim found 7.0 dimes, which is equal to 7 \* \$0.10 = \$0.70. Tim also found 9.0 half-dollars, which is equal to 9 \* \$0.50 = \$4.50. Therefore, Tim got a total of 0.15 + 1.30 + 0.70 + 4.50 = 6.65. Answer: 6.65

## AlignedCoT For GPT-3.5-Turbo

[Question]: Adam bought 9.0 packages of cat food and 7.0 packages of dog food. Each package of cat food contained 10.0 cans, and each package of dog food contained 5.0 cans. How many more cans of cat food than dog food did Adam buy?

#### [Solution]:

Let's think step by step.

1. Calculate the total number of cans of cat food. To find the total number of cans of cat food, we need to multiply the number of packages of cat food by the number of cans in each package. 9.0 packages of cat food \* 10.0 cans per package = 90.0 cans of cat food.

2. Calculate the total number of cans of dog food. To find the total number of cans of dog food, we need to multiply the number of packages of dog food by the number of cans in each package. 7.0 packages of dog food \* 5.0 cans per package = 35.0 cans of dog food.

3. Calculate the difference in the number of cans of cat food and dog food. To find the difference, we subtract the total number of cans of dog food from the total number of cans of cat food. 90.0 cans of cat food - 35.0 cans of dog food = 55.0 cans.

Therefore, Adam bought 55.0 more cans of cat food than dog food.

Answer: 55.0

**[Question]**: In a bag there are 13.0 red marbles, 5.0 blue marbles, and 7.0 green marbles. What percent of the marbles are green?

#### [Solution]:

Let's think step by step.

1. Find the total number of marbles in the bag. Total number of marbles = 13.0 red marbles + 5.0 blue marbles + 7.0 green marbles = 25.0 marbles

2. Find the number of green marbles as a fraction of the total number of marbles. Fraction of green marbles = Number of green marbles / Total number of marbles = 7.0 / 25.0

3. Convert the fraction to a percentage. Percentage of green marbles = Fraction of green marbles \* 100 = (7.0 / 25.0) \* 100 = 28.0%

Therefore, 28.0% of the marbles are green.

Answer: 28

**[Question]**: Mika had 20.0 stickers. She bought 26.0 stickers from a store in the mall and got 20.0 stickers for her birthday. Then Mika gave 6.0 of the stickers to her sister and used 58.0 to decorate a greeting card. How many stickers does Mika have left?

### [Solution]:

Let's think step by step.

1. Mika had 20.0 stickers.

2. She bought 26.0 stickers from a store in the mall, so now she has 20.0 + 26.0 = 46.0 stickers.

3. She also got 20.0 stickers for her birthday, so now she has 46.0 + 20.0 = 66.0 stickers.

4. Mika gave 6.0 stickers to her sister, so now she has 66.0 - 6.0 = 60.0 stickers.

5. Mika used 58.0 stickers to decorate a greeting card, so now she has 60.0 - 58.0 = 2.0 stickers left.

Therefore, Mika has 2.0 stickers left.

Answer: 2.0

**[Question]**: Luke had 20.0 stickers. He bought 12.0 stickers from a store in the mall and got 20.0 stickers for his birthday. Then Luke gave 5.0 of the stickers to his sister and used 8.0 to decorate a greeting card. How many stickers does Luke have left?

#### [Solution]:

Let's think step by step.

1. Luke had 20.0 stickers.

2. He bought 12.0 stickers from a store in the mall, so he now has 20.0 + 12.0 = 32.0 stickers.

3. He also received 20.0 stickers for his birthday, so he now has 32.0 + 20.0 = 52.0 stickers.

4. Luke gave 5.0 stickers to his sister, so he now has 52.0 - 5.0 = 47.0 stickers.

5. He used 8.0 stickers to decorate a greeting card, so he now has 47.0 - 8.0 = 39.0 stickers left.

Therefore, Luke has 39.0 stickers left.

Answer: 39.0

**[Question]**: How many yards of material from a 24.0 yard length of cloth remains after 3.0 pieces each 3.5 yards long and 5.0 pieces each 2.25 long are removed?

[Solution]:

Let's think step by step.

1. Start with a 24.0 yard length of cloth.

2. Remove 3.0 pieces, each 3.5 yards long. This is a total of  $3.0 \times 3.5 = 10.5$  yards.

3. Subtract the length of the removed pieces from the original length: 24.0 - 10.5 = 13.5 yards remaining.

4. Remove 5.0 pieces, each 2.25 yards long. This is a total of  $5.0 \times 2.25 = 11.25$  yards.

5. Subtract the length of the second set of removed pieces from the remaining length: 13.5 - 11.25 = 2.25 yards remaining.

Therefore, after removing the specified pieces, there are 2.25 yards of material remaining from the original 24.0 yard length of cloth.

Answer: 2.25

**[Question]**: If Bob can make 100.0 feet of rope in 2.0 hours and Tim can make 75.0 feet of rope in 2.0 hours, how many feet of rope can Bob and Tim working together make in 4.0 hours? **[Solution]**:

Let's think step by step.

1. Let's find out how much rope Bob can make in 1 hour. We can do this by dividing the total amount of rope Bob can make in 2 hours (100.0 feet) by the number of hours (2.0 hours). Bob's rate of making rope = 100.0 feet / 2.0 hours =

50.0 feet/hour

2. Let's find out how much rope Tim can make in 1 hour. We can do this by dividing the total amount of rope Tim can make in 2 hours (75.0 feet) by the number of hours (2.0 hours). Tim's rate of making rope = 75.0 feet / 2.0 hours = 37.5 feet/hour

3. Let's find out how much rope Bob and Tim can make together in 1 hour. We can do this by adding their individual rates of making rope. Bob and Tim's combined rate of making rope = Bob's rate + Tim's rate = 50.0 feet/hour + 37.5 feet/hour = 87.5 feet/hour

4. Let's find out how much rope Bob and Tim can make together in 4 hours. We can do this by multiplying their combined rate of making rope by the number of hours (4.0 hours). Total rope made by Bob and Tim in 4 hours = Combined rate \* Number of hours = 87.5 feet/hour \* 4.0 hours = 350.0 feet

Therefore, Bob and Tim working together can make 350.0 feet of rope in 4.0 hours.

Answer: 350.0

**[Question]**: A neighborhood grocer sells a mix of chocolate and carob candy. The chocolate cost 2.7 dollars a pound and the carob costs 2.55 dollars a pound. If 20.0 pounds of the chocolate and 40.0 pounds of the carob candy are used, what is the cost per pound of the mixture in dollars?

[Solution]:

Let's think step by step.

1. We need to find the total cost of the chocolate candy. We can do this by multiplying the cost per pound (\$2.7) by the number of pounds (20.0): Total cost of chocolate candy = \$2.7/pound \* 20.0 pounds = \$54.0

2. We need to find the total cost of the carob candy. We can do this by multiplying the cost per pound (\$2.55) by the number of pounds (40.0): Total cost of carob candy = \$2.55/pound \* 40.0 pounds = \$102.0

3. We can find the total cost of the mixture by adding the total cost of the chocolate candy and the total cost of the carob candy: Total cost of mixture = \$54.0 + \$102.0 = \$156.0

4. We can find the cost per pound of the mixture by dividing the total cost of the mixture by the total weight of the mixture (20.0 pounds + 40.0 pounds = 60.0 pounds): Cost per pound of mixture = 156.0 / 60.0 pounds = 2.6 Therefore, the cost per pound of the mixture is 2.6.

Answer: 2.60

**[Question]**: Tim got 3.0 nickels and 13.0 dimes for shining shoes, and in his tip jar found 7.0 dimes and 9.0 half - dollars. How much money did Tim get?

[Solution]:

Let's think step by step.

1. Tim got 3.0 nickels, which means he received 3.0 \* \$0.05 = \$0.15 from the nickels.

2. Tim also got 13.0 dimes, which means he received 13.0 \* \$0.10 = \$1.30 from the dimes.

3. In his tip jar, Tim found 7.0 dimes, which means he received an additional 7.0 \* \$0.10 = \$0.70 from the dimes in the tip jar.

4. Tim also found 9.0 half-dollars, which means he received an additional 9.0 \* \$0.50 = \$4.50 from the half-dollars in the tip jar.

5. Adding up all the amounts, Tim received 0.15 + 1.30 + 0.70 + 4.50 = 6.65 in total.

Therefore, Tim get \$6.65.

Answer: 6.65

## AlignedCoT For GPT-4

[Question]: Adam bought 9.0 packages of cat food and 7.0 packages of dog food. Each package of cat food contained 10.0 cans, and each package of dog food contained 5.0 cans. How many more cans of cat food than dog food did Adam buy?

#### [Solution]:

Let's think step by step.

First, let's calculate how many cans of cat food Adam bought.

He bought 9.0 packages of cat food, and each package contained 10.0 cans.

So, he bought 9.0 \* 10.0 = 90.0 cans of cat food.

Next, let's calculate how many cans of dog food Adam bought.

He bought 7.0 packages of dog food, and each package contained 5.0 cans.

So, he bought 7.0 \* 5.0 = 35.0 cans of dog food.

Finally, let's calculate how many more cans of cat food than dog food Adam bought.

He bought 90.0 cans of cat food and 35.0 cans of dog food.

So, he bought 90.0 - 35.0 = 55.0 more cans of cat food than dog food.

Answer: 55.0

[Question]: In a bag there are 13.0 red marbles, 5.0 blue marbles, and 7.0 green marbles. What percent of the marbles are green?

[Solution]:

Let's think step by step.

First, let's calculate the total number of marbles in the bag.

The total number of marbles is 13.0 red marbles + 5.0 blue marbles + 7.0 green marbles = 25.0 marbles.

Next, let's calculate the percentage of the marbles that are green. The percentage is the number of green marbles divided by the total number of marbles, multiplied by 100. So, the percentage of green marbles is (7.0 green marbles / 25.0 total marbles) \* 100 = 28%. Answer: 28 [Question]: Mika had 20.0 stickers. She bought 26.0 stickers from a store in the mall and got 20.0 stickers for her birthday. Then Mika gave 6.0 of the stickers to her sister and used 58.0 to decorate a greeting card. How many stickers does Mika have left? [Solution]: Let's think step by step. First, let's calculate how many stickers Mika had after she bought some and got some for her birthday. She had 20.0 stickers, bought 26.0 stickers, and got 20.0 stickers for her birthday. So, she had 20.0 + 26.0 + 20.0 = 66.0 stickers. Next, let's calculate how many stickers Mika had left after she gave some to her sister and used some to decorate a greeting card. She gave 6.0 stickers to her sister and used 58.0 stickers. So, she had 66.0 - 6.0 - 58.0 = 2.0 stickers left. Answer: 2.0 [Question]: Luke had 20.0 stickers. He bought 12.0 stickers from a store in the mall and got 20.0 stickers for his birthday. Then Luke gave 5.0 of the stickers to his sister and used 8.0 to decorate a greeting card. How many stickers does Luke have left? [Solution]: Let's think step by step. First, let's calculate how many stickers Luke had after he bought some and got some for his birthday. He had 20.0 stickers, bought 12.0 stickers, and got 20.0 stickers for his birthday. So, he had 20.0 + 12.0 + 20.0 = 52.0 stickers. Next, let's calculate how many stickers Luke had left after he gave some to his sister and used some to decorate a greeting card. He gave 5.0 stickers to his sister and used 8.0 stickers. So, he had 52.0 - 5.0 - 8.0 = 39.0 stickers left. Answer: 39.0 [Ouestion]: How many yards of material from a 24.0 yard length of cloth remains after 3.0 pieces each 3.5 yards long and 5.0 pieces each 2.25 long are removed? [Solution]: Let's think step by step. First, let's calculate how much material is used for the 3.0 pieces each 3.5 yards long. The total length of these pieces is 3.0 pieces \* 3.5 yards/piece = 10.5 yards.Next, let's calculate how much material is used for the 5.0 pieces each 2.25 yards long. The total length of these pieces is 5.0 pieces \* 2.25 yards/piece = 11.25 yards. So, the total length of material used is 10.5 yards + 11.25 yards = 21.75 yards. Finally, let's calculate how much material remains from the 24.0 yard length of cloth. The remaining length is 24.0 yards - 21.75 yards = 2.25 yards. Answer: 2.25 [Question]: If Bob can make 100.0 feet of rope in 2.0 hours and Tim can make 75.0 feet of rope in 2.0 hours, how many feet of rope can Bob and Tim working together make in 4.0 hours? [Solution]: Let's think step by step. First, let's calculate how much rope Bob and Tim can each make in one hour. Bob can make 100.0 feet / 2.0 hours = 50.0 feet/hour. Tim can make 75.0 feet / 2.0 hours = 37.5 feet/hour. Next, let's calculate how much rope Bob and Tim can make together in one hour. Working together, they can make 50.0 feet/hour + 37.5 feet/hour = 87.5 feet/hour. Finally, let's calculate how much rope Bob and Tim can make together in 4.0 hours. In 4.0 hours, they can make 87.5 feet/hour \* 4.0 hours = 350.0 feet. Answer: 350.0 [Question]: A neighborhood grocer sells a mix of chocolate and carob candy. The chocolate cost 2.7 dollars a pound and the carob costs 2.55 dollars a pound. If 20.0 pounds of the chocolate and 40.0 pounds of the carob candy are used, what is the cost per pound of the mixture in dollars? [Solution]: Let's think step by step. First, let's calculate the total cost of the chocolate and carob candy. The cost of the chocolate is 20.0 pounds \* 2.7 dollars/pound = 54 dollars. The cost of the carob candy is 40.0 pounds \* 2.55 dollars/pound = 102 dollars. So, the total cost of the mixture is 54 dollars + 102 dollars = 156 dollars.

Next, let's calculate the total weight of the mixture. The total weight is 20.0 pounds + 40.0 pounds = 60.0 pounds. Finally, let's calculate the cost per pound of the mixture. The cost per pound is the total cost divided by the total weight. So, the cost per pound is 156 dollars / 60.0 pounds = 2.6 dollars/pound. Answer: 2.6 [Question]: Tim got 3.0 nickels and 13.0 dimes for shining shoes, and in his tip jar found 7.0 dimes and 9.0 half - dollars. How much money did Tim get? [Solution]: Let's think step by step. First, let's calculate how much money Tim got from nickels. A nickel is worth 5 cents. So, 3.0 nickels are worth 3.0 \* 5 = 15 cents. Next, let's calculate how much money Tim got from dimes. A dime is worth 10 cents. So, 13.0 dimes from shining shoes are worth  $13.0 \times 10 = 130$  cents. And 7.0 dimes from the tip jar are worth 7.0 \* 10 = 70 cents. Then, let's calculate how much money Tim got from half-dollars. A half-dollar is worth 50 cents. So, 9.0 half-dollars are worth 9.0 \* 50 = 450 cents. Finally, let's add up all the money Tim got. He got 15 cents from nickels, 130 cents from dimes for shining shoes, 70 cents from dimes in the tip jar, and 450 cents from half-dollars. So, the total amount of money Tim got is 15 + 130 + 70 + 450 = 665 cents. Since 100 cents make a dollar, Tim got 665 / 100 = \$6.65. Answer: 6.65

# E.4 CoT w/ AlignedCoT exemplars for AQUA

### AlignedCoT For GPT-3.5-Turbo

[Question]: John found that the average of 15 numbers is 40. If 10 is added to each number then the mean of the numbers is? [Options]: A)50, B)45, C)65, D)78, E)64 [Solution]: First, Let's find the sum of the 15 numbers. Since the average of the 15 numbers is 40, the sum of the 15 numbers is 15 \* 40 = 600. Next, let's add 10 to each number. If we add 10 to each number, the sum of the numbers will increase by 10 \* 15 = 150. Then, let's find the new average. The new sum of the numbers is 600 + 150 = 750. Since there are still 15 numbers, the new average is 750 / 15 = 50. Therefore, the mean of the numbers after adding 10 to each number is 50. Answer: A **[Question]**: If a / b = 3/4 and 8a + 5b = 22, then find the value of a. [**Options**]: A)1/2, B)3/2, C)5/2, D)4/2, E)7/2 [Solution]: Let's think step by step. First, let's solve the equation a/b = 3/4 for a. We can do this by cross-multiplying: 4a = 3bNext, let's substitute this value of a into the second equation 8a + 5b = 22: 8(3b/4) + 5b = 22Multiplying through by 4 to get rid of the fraction: 24b + 20b = 88Combining like terms: 44b = 88Dividing both sides by 44: b = 2Now, let's substitute this value of b back into the equation 4a = 3b: 4a = 3(2)4a = 6Dividing both sides by 4: a = 6/4Simplifying: a = 3/2Therefore, the value of a is 3/2. Answer: B

[Question]: A person is traveling at 20 km/hr and reached his destiny in 2.5 hr then find the distance? [Options]: A)53 km, B)55 km, C)52 km, D)60 km, E)50 km [Solution]: Let's think step by step. Given: Speed = 20 km/hrTime = 2.5 hrTo find the distance, we can use the formula: Distance = Speed x TimeSubstituting the given values: Distance =  $20 \text{ km/hr} \times 2.5 \text{ hr}$ Calculating: Distance = 50 kmTherefore, the distance is 50 km. Answer: E [Question]: How many keystrokes are needed to type the numbers from 1 to 500? [Options]: A)1156, B)1392, C)1480, D)1562, E)1788 [Solution]: Let's think step by step. For the numbers from 1 to 9, 1 keystroke is needed for each number. There are 9 numbers from 1 to 9, so 9 keystrokes are needed. For the numbers from 10 to 99, 2 keystrokes are needed for each number. There are 90 numbers from 10 to 99, so 90 \* 2 = 180 keystrokes are needed. For the numbers from 100 to 500, 3 keystrokes are needed for each number. There are 401 numbers from 100 to 500, so 401 \* 3 = 1203 keystrokes are needed. Adding up all the keystrokes, we get 9 + 180 + 1203 = 1392 keystrokes. Therefore, the 1392 keystrokes are needed to type. Answer: B

### AlignedCoT For GPT-4

[Question]: John found that the average of 15 numbers is 40. If 10 is added to each number then the mean of the numbers is? [Options]: A)50, B)45, C)65, D)78, E)64 [Solution]: Let's think step by step. Step 1: We know the average of 15 numbers is 40, which means the total sum of these numbers is 15 \* 40 = 600. Step 2: If 10 is added to each number, the total sum increases by 10 \* 15 = 150. Step 3: So, the new total sum is 600 + 150 = 750. Step 4: The new average or mean is the total sum divided by the number of numbers, which is 750/15 = 50. So, the new mean of the numbers is 50. Answer: A **[Question]**: If a / b = 3/4 and 8a + 5b = 22, then find the value of a. [Options]: A)1/2, B)3/2, C)5/2, D)4/2, E)7/2 [Solution]: Let's think step by step. Step 1: From the first equation, we can express a in terms of b. That is a = 3b/4. Step 2: Substitute a = 3b/4 into the second equation. We get 8(3b/4) + 5b = 22, which simplifies to 6b + 5b = 22. Step 3: Combine like terms to get 11b = 22. Step 4: Solve for b by dividing both sides by 11. We get b = 2. Step 5: Substitute b = 2 into the equation a = 3b/4 to get a = 3(2)/4 = 3/2. So, the value of a is 3/2. Answer: B [Question]: A person is traveling at 20 km/hr and reached his destiny in 2.5 hr then find the distance? [Options]: A)53 km, B)55 km, C)52 km, D)60 km, E)50 km [Solution]: Let's think step by step. Step 1: We know the speed of the person which is 20 km/hr. Step 2: We also know the time taken by the person to reach his destination which is 2.5 hr. Step 3: We need to find the distance. We know that distance = speed \* time. Step 4: Substituting the given values in the formula, we get distance = 20 km/hr \* 2.5 hr = 50 km. So, the person traveled a distance of 50 km. Answer: E

[Question]: How many keystrokes are needed to type the numbers from 1 to 500? [Options]: A)1156, B)1392, C)1480, D)1562, E)1788 [Solution]: Let's think step by step. Step 1: For 1 to 9, we have 9 numbers, each of which is a single digit, so we need 9 keystrokes. Step 2: For 10 to 99, we have 90 numbers, each of which is a double digit, so we need 90 \* 2 = 180 keystrokes. Step 3: For 100 to 499, we have 400 numbers, each of which is a triple digit, so we need 400 \* 3 = 1200 keystrokes. Step 4: For 500, this is a triple digit number, so we need 3 keystrokes. Step 5: Adding all these up, we get 9 + 180 + 1200 + 3 = 1392 keystrokes. So, to type the numbers from 1 to 500, we need 1392 keystrokes.

## E.5 Complex CoT w/ AlignedCoT exemplars for AQUA

## AlignedCoT For GPT-3.5-Turbo

**[Question]**: There were 35 students in a hostel. Due to the admission of 7 new students the expenses of the mess were increased by Rs.84 per day while the average expenditure per head diminished by Re 1. What was the original expenditure of the mess? [Options]: A)Rs 450, B)Rs 920, C)Rs 550, D)Rs.630, E)None of these [Solution]: Let's think step by step. Let's assume the original average expenditure per head be Rs.x So, the total expenditure of the mess before the admission of new students = 35x. After the admission of 7 new students, the total number of students becomes 35 + 7 = 42. The new average expenditure per head = x - 1. So, the total expenditure of the mess after the admission of new students = 42(x - 1). According to the given information, the new total expenditure is increased by Rs.84 per day. So, we can write the equation as: 42(x - 1) - 35x = 84.Now, let's solve the equation. 42x - 42 - 35x = 84. 7x = 126. x = 18. The original expenditure of the mess was Rs. 18 per head. Therefore, the original expenditure of the mess = 35 \* 18 = Rs. 630. Answer: D [Question]: A train 200 m long passes a man, running at 5 km/hr in the same direction in which the train is going, in 10 seconds. The speed of the train is? [Options]: A)28, B)50, C)77, D)22, E)12 [Solution]: Let's think step by step. Length of the train = 200 m = 0.2 kmSpeed of the man = 5 km/hrTime taken to pass the man = 10 s = (10 / 3600) hr = (1 / 360) hrLet's assume the speed of the train is 'x' km/hr. Relative speed of the train with respect to the man = (x - 5) km/hr Distance covered by the train in 10 seconds = Length of the train = 200 mUsing the formula: Distance = Speed  $\times$  Time, we can write the equation as:  $0.2 = (x - 5) \times (1 / 360)$ Now, let's solve the equation.  $0.2 \times 360 = x - 5$ 72 + 5 = xx = 77 Therefore, the speed of the train is 77 km/hr. Answer: C [Question]: Solution X contains 20% of material A and 80% of material B. Solution Y contains 30% of material A and 70% of material B. A mixture of both these solutions contains 22% of material A in the final product. how much solution X is present in the mixture? [**Options**]: A)40%, B)60%, C)80%, D)100%, E)110% [Solution]: Let's think step by step. Let's assume that the mixture contains x% of solution X and (100-x)% of solution Y. In solution X, 20% of material A is present, so the amount of material A in solution X is 0.2x. In solution Y, 30% of material A is present, so the amount of material A in solution Y is 0.3(100-x).

In the final mixture, 22% of material A is present, so the amount of material A in the mixture is 0.22(100). Since the amount of material A in the mixture is the sum of the amounts of material A in solution X and solution Y, we can write the equation: 0.2x + 0.3(100 - x) = 0.22(100)Now, let's solve the equation. 0.2x + 30 - 0.3x = 22-0.1x = -8x = 80 Therefore, 80% of solution X is present in the mixture. Answer: C [Question]: A trader sells 40 metres of cloth for Rs.8200 at a profit of Rs.35 per metre of cloth. How much profit will the trder earn on 40 metres of cloth? [Options]: A)Rs.950, B)Rs.1500, C)Rs.1000, D)Rs.1400, E)None of these [Solution]: Let's think step by step. The trader earns a profit of Rs.35 per metre of cloth. The trader sells 40 metres of cloth. So, the trader will earn a profit of  $Rs.35 \times 40 = Rs.1400$  on 40 metres of cloth. Answer<sup>.</sup> D **[Question]**: If x < y < z and y - x > 5, where x is an even integer and y and z are odd integers, what is the least possible value S of z - x? [Options]: A)6, B)7, C)8, D)9, E)10 [Solution]: Let's think step by step. Since x is an even integer and y is an odd integer, the difference y - x will always be an odd integer. Given that y - x > 5, since it has to be an odd integer greater than 5, the smallest possible value for y - x is 7. Since y and z are both odd integers, the difference z - y will always be an even integer. Given that y < z, which means z - y > 0. Since z - y is an even integer greater than 0, the smallest possible value for z - yis 2. Therefore, the least possible value of z - x = (z - y) + (y - x) is 2 + 7 = 9. Answer: D [Question]: What is the difference between the C.I. on Rs. 6000 for 1 1/2 years at 4% per annum compounded yearly and half-yearly? [Options]: A)s.2.04, B)s.2.08, C)s.2.02, D)s.2.83, E)s.2.45 [Solution]: Let's think step by step. Let's first give the formula for compound interest:  $CI = P(1 + r/100)^n - P$ Where, P = Principal amount r = Rate of interestn = The number of interest periods, which should be an integer Let's calculate the compound interest (CI) for 1 1/2 years at 4% per annum compounded yearly. We are given that: The principal amount is Rs. 6000. So, P = 6000; The rate of interest is 4% per annum. So, r = 4%; The number of interest periods is 1 1/2 years. So n = 1 1/2. The n is not an integer, and people can only get half interest for the rest half year. So, the CI compounded yearly for 1 1/2 years is: CI = P(1 + r/100)(1 + 1/2 \* r/100) - P= 6000(1 + 4/100)(1 + 1/2 \* 4/100) - 6000= 6000(104/100)(102/100) - 6000= 6000 \* 26/25 \* 51/50 - 6000 = 6000 \* 1326/1250 - 6000 = 6000 \* 1.0608 - 6000 = 6364.8 - 6000 = 364.8 Now, let's calculate the compound interest (CI) for 1 1/2 years at 4% per annum compounded half-yearly. We are given that: The principal amount is Rs. 6000. So, P = 6000. The rate of interest is 4% per annum compounded half-yearly. So, r = 4% / 2 = 2%. The number of interest periods is (1 1/2) years / (1/2) year = 3. So, the CI compounded half-yearly for 1 1/2 years is:  $CI = P(1 + r/100)^n - P$  $= 6000(1 + 2/100)^3 - 6000$  $= 6000(102/100)^{3} - 6000$ = 6000 \* 51/50 \* 51/50 \* 51/50 - 6000 = 6000 \* 132651 / 125000 - 6000 = 6000 \* 1.061208 - 6000

= 6367.248 - 6000= 367.248So, the difference between the two compound interests is: 367.248 - 364.8 = 2.448 = Rs.2.45 Answer: E [Question]: The average weight of A, B and C is 45 kg. If the average weight of A and B be 40 kg and that of B and C be 45 kg, then the weight of B is: [Options]: A)31 kg, B)32 kg, C)33 kg, D)35 kg, E)None of these [Solution]: Let's think step by step. Let's think step by step. Let the weight of A be x kg, the weight of B be y kg, and the weight of C be z kg. According to the given information, the average weight of A and B is 40 kg. So, we can write the equation: (x + y)/2 = 40Simplifying this equation, we get: x + y = 80Similarly, the average weight of B and C is 45 kg. So, we can write the equation: (y + z)/2 = 45Simplifying this equation, we get: y + z = 90Now, we need to find the weight of B. We can do this by subtracting the weight of A and C from the total weight of A, B, and C. The average weight of A, B, and C is 45 kg. So, we can write the equation: (x + y + z)/3 = 45Simplifying this equation, we get: x + y + z = 135Now, subtracting the equation (x + y = 80) from the equation (x + y + z = 135), we get: z = 55tuting the value of z in the equation (y + z = 90), we get: y + 55 = 90Subtracting 55 from both sides of the equation, we get: y = 35Therefore, the weight of B is 35 kg. Answer: D [Question]: The compound and the simple interests on a certain sum at the same rate of interest for two years are Rs.11730 and Rs.10200 respectively. Find the sum [Options]: A)Rs.17037, B)Rs.17000, C)Rs.17276, D)Rs.170287, E)Rs.171881 [Solution]: Let's think step by step. Let's first give the formulas for compound interest (CI) and simple interest (SI).  $CI = P(1 + r/100)^n - P$ SI = P \* r \* n/100Where, P = Principal amount r = Rate of interestn = The number of interest periods, which should be an integer. Given that the compound interest (CI) and the simple interest (SI) for 2 years is Rs. 11730 and Rs. 10200 respectively. So, we have CI = Rs. 11730, SI = Rs. 10200, and n = 2. Substituting these values in the formulas, we have:  $11730 = P(1 + r/100)^2 - P$ 10200 = P \* r \* 2/100Now, let's solve the equations to find P. From the second equation, we can rewrite it as: r = 10200 \* 100 / (P \* 2)r = 510000 / PNow, substitute this value of r in the first equation:  $11730 = P(1 + 510000/P/100)^2 - P$ Simplifying the equation, we get:  $11730 = P(1 + 5100/P)^2 - P$  $11730 = P(1 + 2 * 5100/P + 5100^{2}/P^{2}) - P$  $11730 = P + 2* 5100 + 5100^2/P - P$  $11730 = 10200 + 5100^{2}/P$ 1530 = 5100<sup>2</sup>/P  $P = 5100^2/1530$ P = 2601000/1530P = 17000Therefore, the sum is Rs. 17000.

Answer: B

#### AlignedCoT For GPT-4

**[Question]**: there were 35 students in a hostel. due to the admission of 7 new students the expenses of the mess were increased by rs. 84 per day while the average expenditure per head diminished by re 1. what was the original expenditure of the mess ? [Options]: (a) rs 450 (b) rs 920 (c) rs 550 (d) rs . 630 (e) none of these [Solution]: Let's think step by step. The original number of students was 35 and the original expenditure was X. So, the original average expenditure per head was X/35. After the admission of 7 new students, the total number of students became 42 and the total expenditure became X+84. So, the new average expenditure per head was (X+84)/42. According to the problem, the new average expenditure per head is 1 less than the original average expenditure per head. So, we can write the equation as follows: X/35 - (X+84)/42 = 1. Now, let's solving the above equation, Multiplying both sides by 35 \* 42, we get 42X - 35(X+84) = 35\*42. Simplifying, we get 7X - 35\*84 = 35\*42. 7X = 35\*84 + 35\*42 = 35(84 + 42) = 35\*126 = 35\*7\*18.X = 35\*18 = 630.So, the original expenditure of the mess was Rs. 630. Answer: D [Question]: a train 200 m long passes a man, running at 5 km / hr in the same direction in which the train is going, in 10 seconds. the speed of the train is? **[Options]**: (a) 28 (b) 50 (c) 77 (d) 22 (e) 12 [Solution]: Let's think step by step. Convert the speed of the man from km/hr to m/s. We know that 1 km/hr = 5/18 m/s. So, the speed of the man is 5\*(5/18) = 25/18 m/s. The train passes the man in 10 seconds. This means the relative speed of the train to the man is the distance divided by the time, which is 200m/10s = 20 m/s. The actual speed of the train is the relative speed plus the speed of the man, because they are moving in the same direction. So, the speed of the train is 20 m/s + 25/18 m/s = 385/18 m/s. Convert the speed of the train from m/s to km/hr. We know that 1 m/s = 18/5 km/hr. So, the speed of the train is (385/18)\*(18/5) = 77 km/hr. So, the correct answer is 77. Answer: C [Question]: solution x contains 20 % of material a and 80 % of material b . solution y contains 30 % of material a and 70 % of material b. a mixture of both these solutions contains 22 % of material a in the final product. how much solution x is present in the mixture ? **[Options]**: (a) 40 % (b) 60 % (c) 80 % (d) 100 % (e) 110 % [Solution]: Let's think step by step. Let's assume that the amount of solution X used is x% and the amount of solution Y used is (100-x)%. The amount of material A in the final mixture is given by the sum of the amounts of material A in solutions X and Y. So, we can write the equation as follows: 0.20x + 0.30(100-x) = 22. Now, let's solving the above equation, 0.20x + 0.30(100-x) = 220.20x + 30 - 0.30x = 220.10x = 8x = 80 So, 80% of solution X is present in the mixture. Answer: C [Question]: a trader sells 40 metres of cloth for rs. 8200 at a profit of rs. 35 per metre of cloth. how much profit will the trder earn on 40 metres of cloth ? [Options]: (a) rs . 950 (b) rs . 1500 (c) rs . 1000 (d) rs . 1400 (e) none of these [Solution]: Let's think step by step. The trader earns a profit of Rs. 35 per metre of cloth. So, for 40 metres of cloth, the trader will earn a profit of 40\*35 = Rs. 1400. So, the trader will earn a profit of Rs. 1400 on 40 metres of cloth. Answer: D

**[Question]**: if x < y < z and y - x > 5, where x is an even integer and y and z are odd integers, what is the least possible value s of z - x? [**Options**]: (a) 6 (b) 7 (c) 8 (d) 9 (e) 10 [Solution]: Let's think step by step. Since x is an even integer and y is an odd integer, the difference between y and x must be an odd number. Given that y x > 5, the smallest possible value for y - x is 7. Since y < z and y and z are both odd integers, the smallest possible difference between y and z is 2 (because odd numbers are 2 units apart). Therefore, the smallest possible value for z - x is the sum of the smallest possible values for y - x and y - z, which is 7 + 2 = 9So, the least possible value of z - x is 9. Answer: D [Question]: what is the difference between the c. i. on rs. 6000 for 1 1 / 2 years at 4 % per annum compounded yearly and half - yearly ? [Options]: (a) s . 2.04 (b) s . 2.08 (c) s . 2.02 (d) s . 2.83 (e) s . 2.45 [Solution]: Let's think step by step. Calculate the compound interest (C.I.) when compounded yearly. The formula for C.I. is  $A = P(1 + r/n)^{(nt)}$ , where A is the amount. P is the principal, r is the rate of interest, n is the number of times interest is compounded per time period, and t is the time. Here,  $P = Rs.\ 6000$ , r = 4/100 = 0.04, n = 1 (since it's compounded yearly), and t = 1.5 years. However, the rest half year in the 1.5 years time period can not cover the whole compound period. People can only get half interest for the rest half year. So, A = 6000(1 + 0.04/1)(1 + 0.5\*0.04/1)= 6000(1.04)(1.02)= 6000 \* 1.0608= 6364.8The C.I. is A - P = Rs. 6364.8 - Rs. 6000 = Rs. 364.8. Calculate the C.I. when compounded half-yearly. Now, n = 2 (since it's compounded half-yearly). So, A =  $6000(1 + 0.04/2)^{(2*1.5)}$  $= 6000(1.02)^{3}$ = 6000 \* 1.061208 = 6367.248The C.I. is A - P = Rs. 6367.248 - Rs. 6000 = Rs. 367.248. The difference between the C.I. when compounded yearly and half-yearly is Rs. 367.248 - Rs. 364.8 = Rs. 2.448. = Rs. 2.45 So, the correct answer is Rs. 2.45. Answer: E [Question]: the average weight of a , b and c is 45 kg . if the average weight of a and b be 40 kg and that of b and c be 45 kg, then the weight of b is : [Options]: (a) 31 kg (b) 32 kg (c) 33 kg (d) 35 kg (e) none of these [Solution]: Let's think step by step. The average weight of a, b, and c is 45 kg. So, (a + b + c)/3 = 45 kg. Then, a + b + c = 45\*3 = 135 kg. The average weight of a and b is 40 kg. So, (a + b)/2 = 40 kg. Then,  $a + b = 40^{\circ}2 = 80$  kg. The average weight of b and c is 45 kg. So, (b + c)/2 = 45 kg. Then, b + c = 45\*2 = 90 kg. Now, we have a + b = 80 kg and b + c = 90 kg. So, a + b + b + c = 80 + 90 = 170 kg. We already know that a + b + c = 135 kg. So, 135 = 170 - b. Then, b = 170 - 135 = 35 kg. So, the weight of b is 35 kg. Answer: D [Question]: the compound and the simple interests on a certain sum at the same rate of interest for two years are rs. 11730 and rs. 10200 respectively. find the sum [Options]: (a) rs. 17037 (b) rs. 17000 (c) rs. 17276 (d) rs. 170287 (e) rs. 171881 [Solution]: Let's think step by step. The difference between the compound interest and the simple interest for two years gives the interest for one year on the

simple interest for one year. So, the interest for one year is Rs. 11730 - Rs. 10200 = Rs. 1530. The simple interest for two years is Rs. 10200, so the simple interest for one year is Rs. 10200 / 2 = Rs. 5100. The rate of interest is the interest for one year divided by the principal amount. So, the rate of interest is Rs. 1530 / Rs. 5100 = 0.3 or 30%. The principal amount is the simple interest for one year divided by the rate of interest. So, the principal amount is Rs. 5100 / 0.3 = Rs. 17000. So, the sum is Rs. 17000. Answer: B

### E.6 CoT w/ AlignedCoT exemplars for Penguins

### AlignedCoT For GPT-3.5-Turbo

**Q**: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 How many penguins are less than 8 years old? **Options:** (A) 1 (B) 2 (C) 3 (D) 4 (E) 5 A: Let's think step by step. We are given a table with the information of several penguins. We need to find out how many penguins are less than 8 years old. Looking at the table, we can see that Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, and Gwen is 8 years old. The additional penguin, James, is 12 years old. Out of these five penguins, only Louis and Bernard are less than 8 years old. So the answer is (B). Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. Which is the youngest penguin? **Options**: (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. We are given a table with the information of several penguins. We need to find out the the youngest penguin. First, let's identify the column that represents the age of each penguin. In this case, it is the second column. Next, let's compare the ages of each penguin: Louis: 7 Bernard: 5 Vincent: 9 Gwen: 8 From the comparison, we can see that Bernard is the youngest penguin with an age of 5. So the answer is (B). **O**: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. What is the name of the second penguin sorted by alphabetic order? **Options**: (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. We are given a table with the information of several penguins. We need to find the name of the second penguin sorted by alphabetic order. First, let's identify the name of each penguin in the table. In this case, the names are in the first column. So, the names are Louis, Bernard, Vincent, and Gwen.

Next, let's sort the penguins by alphabetical order. The penguins listed in alphabetical order are Bernard, Gwen, Louis, and Vincent. Therefore, the name of the second penguin sorted by alphabetical order is Gwen.

So the answer is (D).

## AlignedCoT For GPT-4

**Q**: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 How many penguins are less than 8 years old? **Options:** (A) 1 (B) 2 (C) 3 (D) 4 (E) 5 A: Let's think step by step. First, we need to find the age of each penguin. According to the table, Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, Gwen is 8 years old, and James is 12 years old. We are looking for penguins that are less than 8 years old. Louis is 7 years old, which is less than 8. Bernard is 5 years old, which is also less than 8. Therefore, there are 2 penguins that are less than 8 years old. So the answer is (B). Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. Which is the youngest penguin? **Options**: (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. First, we need to find the age of each penguin. According to the table, Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, and Gwen is 8 years old. The youngest penguin is the one with the smallest age. In this case, the 5 years old Bernard is the youngest penguin. So the answer is (B). Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. What is the name of the second penguin sorted by alphabetic order? **Options**: (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. First, we need to find the age of each penguin. According to the table, the names of the penguins are Louis, Bernard, Vincent, and Gwen. Then, we need to sort the names of the penguins in alphabetical order. we get Bernard, Gwen, Louis, and Vincent. The second penguin in this sorted list is Gwen. So the answer is (D).

### E.7 Complex CoT w/ AlignedCoT exemplars for Penguins

### AlignedCoT For GPT-3.5-Turbo

Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 And here is a similar table, but listing giraffes: name, age, height (cm), weight (kg) Jody, 5, 430, 620 Gladys, 10, 420, 590 Marian, 2, 310, 410 Donna, 9, 440, 650 What is the name of the last animal sorted by alphabetic order? **Options**: (A) Vincent (B) Louis (C) Louise (D) Marian (E) Jody A: Let's think step by step. First, let's identify the name of each animal in the tables. In this case, the names are in the first column. For the penguins table, the names are Louis, Bernard, Vincent, Gwen, and James. For the giraffes table, the names are Jody, Gladys, Marian, and Donna. Next, let's sort the names in alphabetical order. For the penguins table, the names in alphabetical order are Bernard, Gwen, James, Louis, and Vincent. For the giraffes table, the names in alphabetical order are Donna, Gladys, Jody, and Marian. Now, let's find the last animal in alphabetical order. For the penguins table, the last animal in alphabetical order is Vincent. For the giraffes table, the last animal in alphabetical order is Marian. Vincent is alphabetically after Marian. So the answer is (A). Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 And here is a similar table, but listing giraffes: name, age, height (cm), weight (kg) Jody, 5, 430, 620 Gladys, 10, 420, 590 Marian, 2, 310, 410 Donna, 9, 440, 650 How many animals are less than 8 years old? **Options:** (A) 2 (B) 3 (C) 4 (D) 5 (E) 6 A: Let's think step by step. First, let's count the number of penguins that are less than 8 years old. From the given table, we can see that Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, and Gwen is 8 years old. Out of these four penguins, only Louis and Bernard are less than 8 years old. So, there are 2 penguins that are less than 8 years old. Next, let's count the number of giraffes that are less than 8 years old. From the given table, we can see that Jody is 5 years old, Gladys is 10 years old, Marian is 2 years old, and Donna is 9 years old. Out of these four giraffes, only Jody and Marian are less than 8 years old. So, there are 2 giraffes that are less than 8 years old. Adding the number of penguins and giraffes that are less than 8 years old, we get: 2 (penguins) + 2 (giraffes) = 4Therefore, there are 4 animals in total that are less than 8 years old. So the answer is (C). Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height

(cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis

is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add two penguins to the table: James, 4, 90, 12, Dick, 5, 75, 15. Which is the youngest penguin? **Options:** (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. First, let's identify the age of each penguin. Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, Gwen is 8 years old, James is 4 years old, and Dick is 5 years old. Out of these options, James is the youngest penguin as he is 4 years old. Therefore, the answer is (E) James.

### AlignedCoT For GPT-4

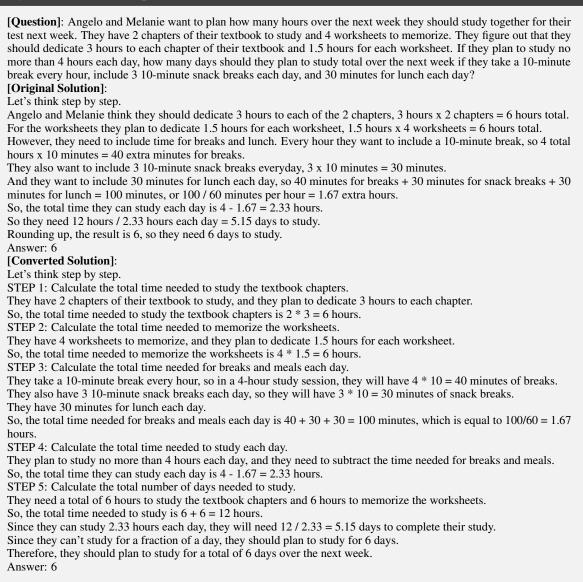
Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 And here is a similar table, but listing giraffes: name, age, height (cm), weight (kg) Jody, 5, 430, 620 Gladys, 10, 420, 590 Marian, 2, 310, 410 Donna, 9, 440, 650 What is the name of the last animal sorted by alphabetic order? **Options:** (A) Vincent (B) Louis (C) Louise (D) Marian (E) Jody A: Let's think step by step. First, let's list all the names of the animals: Louis, Bernard, Vincent, Gwen, James, Jody, Gladys, Marian, Donna. When we sort these names in alphabetical order, we get: Bernard, Donna, Gladys, Gwen, James, Jody, Louis, Marian, Vincent. So, the last animal sorted by alphabetic order is Vincent. Therefore, the correct answer is (A) Vincent. Q: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add a penguin to the table: James, 12, 90, 12 And here is a similar table, but listing giraffes: name, age, height (cm), weight (kg) Jody, 5, 430, 620 Gladys, 10, 420, 590 Marian, 2, 310, 410 Donna, 9, 440, 650 How many animals are less than 8 years old? **Options:** (A) 2 (B) 3 (C) 4 (D) 5 (E) 6 A: Let's think step by step. First, let's look at the penguins. Louis is 7 years old, Bernard is 5 years old, Vincent is 9 years old, Gwen is 8 years old, and James is 12 years old. So, there are 2 penguins that are less than 8 years old: Louis and Bernard. Now, let's look at the giraffes. Jody is 5 years old, Gladys is 10 years old, Marian is 2 years old, and Donna is 9 years old. So, there are 2 giraffes that are less than 8 years old: Jody and Marian. Adding these together, there are 2 penguins + 2 giraffes = 4 animals that are less than 8 years old. So, the answer is (C) 4.

**O**: Here is a table where the first line is a header and each subsequent line is a penguin: name, age, height (cm), weight (kg) Louis, 7, 50, 11 Bernard, 5, 80, 13 Vincent, 9, 60, 11 Gwen, 8, 70, 15 For example: the age of Louis is 7, the weight of Gwen is 15 kg, the height of Bernard is 80 cm. We now add two penguins to the table: James, 4, 90, 12, Dick, 5, 75, 15. Which is the youngest penguin? **Options**: (A) Louis (B) Bernard (C) Vincent (D) Gwen (E) James A: Let's think step by step. First, we need to look at the age of each penguin. Louis is 7, Bernard is 5, Vincent is 9, Gwen is 8, James is 4, and Dick is 5. The youngest penguin is James, who is 4 years old. So, the answer is (E) James.

### E.8 Style Conversion Prompt for GSM8K

In our experiment, we use GPT-3.5-Turbo to convert the training set in GSM8K. During data preprocessing, we deleted the computational part (bracketed by '«' and '»') of the training set.

#### Style Conversion Prompt



[Question]: Mark's basketball team scores 25 2 pointers, 8 3 pointers and 10 free throws. Their opponents score double the 2 pointers but half the 3 pointers and free throws. What's the total number of points scored by both teams added together? [Original Solution]: Let's think step by step. Mark's team scores 25 2 pointers, meaning they scored 25\*2= 50 points in 2 pointers. His team also scores 6 3 pointers, meaning they scored 8\*3= 24 points in 3 pointers They scored 10 free throws, and free throws count as one point so they scored 10\*1=10 points in free throws. All together his team scored 50+24+10=84 points Mark's opponents scored double his team's number of 2 pointers, meaning they scored 50\*2=100 points in 2 pointers. His opponents scored half his team's number of 3 pointers, meaning they scored 24/2= 12 points in 3 pointers. They also scored half Mark's team's points in free throws, meaning they scored 10/2=5 points in free throws. All together Mark's opponents scored 100+12+5=117 points The total score for the game is both team's scores added together, so it is 84+117=201 points Answer: 201 [Converted Solution]: Let's think step by step. STEP 1: Calculate the number of points scored by Mark's team. Mark's team scores 25 2 pointers, which means they score 25 \* 2 = 50 points from 2 pointers. They also score 8 3 pointers, which means they score 8 \* 3 = 24 points from 3 pointers. Finally, they score 10 free throws, which means they score 10 \* 1 = 10 points from free throws. Therefore, the total number of points scored by Mark's team is 50 + 24 + 10 = 84 points. STEP 2: Calculate the number of points scored by the opponents. The opponents score double the 2 pointers, which means they score 2 \* 50 = 100 points from 2 pointers. They also score half the 3 pointers, which means they score 0.5 \* 24 = 12 points from 3 pointers. Finally, they score half the free throws, which means they score 0.5 \* 10 = 5 points from free throws. Therefore, the total number of points scored by the opponents is 100 + 12 + 5 = 117 points. STEP 3: Calculate the total number of points scored by both teams. The total number of points scored by both teams is 84 + 117 = 201 points. Answer: 201 [Question]: A group of 4 fruit baskets contains 9 apples, 15 oranges, and 14 bananas in the first three baskets and 2 less of each fruit in the fourth basket. How many fruits are there? [Original Solution]: Let's think step by step. For the first three baskets, the number of apples and oranges in one basket is 9+15=24 In total, together with bananas, the number of fruits in one basket is 24+14=38 for the first three baskets. Since there are three baskets each having 38 fruits, there are 3\*38=114 fruits in the first three baskets. The number of apples in the fourth basket is 9-2=7 There are also 15-2=13 oranges in the fourth basket The combined number of oranges and apples in the fourth basket is 13+7=20 The fourth basket also contains 14-2=12 bananas. In total, the fourth basket has 20+12=32 fruits. The four baskets together have 32+114=146 fruits. Answer: 146 [Converted Solution]: Let's think step by step. STEP 1: Figure out the total number of fruits in the first three baskets. In each of the first three basket, there are 9 apples + 15 oranges + 14 bananas = 38 fruits. So, in the first three baskets, there are a total of 38 fruits \* 3 = 114 fruits. STEP 2: Figure out the number of fruits in the fourth basket. In the fourth basket, there are 2 less of each fruit compared to the first three baskets. So, there are 9 apples -2 = 7 apples. There are 15 oranges - 2 = 13 oranges. There are 14 bananas - 2 = 12 bananas. Therefore, in the fourth basket, there are a total of 7 apples + 13 oranges + 12 bananas = 32 fruits. STEP 3: Figure out the total number of fruits in all four baskets. The four baskets together have 114 (total fruits in the first three baskets) + 32 (fruits in the fourth basket) = 146 fruits. Answer: 146 [Question]: In a certain school, 2/3 of the male students like to play basketball, but only 1/5 of the female students like to play basketball. What percent of the population of the school do not like to play basketball if the ratio of the male to female students is 3:2 and there are 1000 students? [Original Solution]: Let's think step by step. The students are divided into 3 + 2 = 5 parts where 3 parts are for males and 2 parts are for females. Each part represents 1000/5 = 200 students. So, there are  $3 \times 200 = 600$  males.

And there are  $2 \ge 200 = 400$  females. Hence,  $600 \ge 2/3 = 400$  males play basketball. And  $400 \ge 1/5 = 80$  females play basketball. A total of 400 + 80 = 480 students play basketball. Therefore, 1000 - 480 = 520 do not like to play basketball. The percentage of the school that do not like to play basketball is 520/1000 \* 100 = 52Answer: 52 [Converted Solution]: Let's think step by step. STEP 1: Figure out the number of male and female students in the school. The students are divided into 3 + 2 = 5 parts where 3 parts are for males and 2 parts are for females. Each part represents 1000/5 = 200 students. So, there are  $3 \times 200 = 600$  males. And there are  $2 \times 200 = 400$  females. STEP 2: Figure out the number of males and females who like to play basketball. 2/3 of the male students like to play basketball. Hence,  $600 \ge 2/3 = 400$  males play basketball. 1/5 of the female students like to play basketball. Hence,  $400 \times 1/5 = 80$  females play basketball. STEP 3: Figure out how many people do not like to play basketball. A total of 400 + 80 = 480 students play basketball. Therefore, 1000 - 480 = 520 do not like to play basketball. STEP 4: Calculate the percentage of the population that do not like to play basketball. The percentage of the school that do not like to play basketball is 520/1000 \* 100 = 52Answer: 52