# Executing Natural Language-Described Algorithms with Large Language Models: An Investigation 

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#### Abstract

Executing computer programs described in natural language has long been a pursuit of computer science. With the advent of enhanced natural language understanding capabilities exhibited by large language models (LLMs), the path toward this goal has been illuminated. In this paper, we seek to examine the capacity of present-day LLMs to comprehend and execute algorithms outlined in natural language. We established an algorithm test set sourced from Introduction to Algorithm, a well-known textbook that contains many representative widely-used algorithms. To systematically assess LLMs' code execution abilities, we selected 30 algorithms, generated 300 random-sampled instances in total, and evaluated whether popular LLMs can understand and execute these algorithms. Our findings reveal that LLMs, notably GPT-4, can effectively execute programs described in natural language, as long as no heavy numeric computation is involved. We believe our findings contribute to evaluating LLMs' code execution abilities and would encourage further investigation and application for the computation power of LLMs. Our code and data are available at https://github.com/MrZhengXin/natural_language_program.


Keywords: algorithm execution, instruction-following, large language models

## 1. Introduction

Algorithms are the main knowledge carriers for computing machines, which are conventionally outlined using high-level languages or even pseudocodes due to their communication effectiveness. The endeavor to create a mechanical system that could comprehend and execute natural languagedescribed programs has long been a goal in computer science (Sammet, 1966).

Recently, advancements in large language models (LLMs) have revolutionized the field of natural language processing and artificial Intelligence, creating new SOTAs and reaching human-level language understanding performance on a series of tasks and benchmarks (Brown et al., 2020; OpenAI, 2023; Anil et al., 2023). LLMs, trained on extensive text corpora and code data, acquired world knowledge, commonsense and logical reasoning (Han et al., 2021). After the stage of instruction-tuning (Ouyang et al., 2022), LLMs could act consistently with complicated prompts. During this process, they perform the specific task according to what the instruction presents and return the desired output. As illustrated in Table 1, just as the prompt demands, the model repeatedly uses the keyword to generate a sentence, picks one word as the new keyword, and stops when satisfying the iteration count. These abilities are very analogous to the capabilities that are required to execute a program,

[^0]which raises our interest in whether current LLMs could serve as an environment to execute natural language-described programs.

To run arbitrary algorithms, the ability to follow sequential, selection and iteration statements is needed (Böhm and Jacopini, 1966). A model that does not rigorously support any of the sequential, selection and iteration structures, would fail at execution. Such a model is limited in computation power, and would not perform well on some realworld tasks. In contrast, a model that successfully generates the correct output, is likely to well understand the three critical control flows. With the potential to conduct any computation within the context length theoretically, it is at least promising toward AGI. Therefore, the investigation of program execution could be beneficial for the understanding of LLMs.

However, except for limited preliminary studies (Bubeck et al., 2023; Jojic et al., 2023), there is still a lack of quantitative and qualitative analysis experiments on whether LLMs can serve as effective program executor, as well as a standard benchmark to evaluate how much could a LLM accomplish the goal. Such absence limits our understanding of the latest cutting-edge research progress in this field. To this end, this paper investigates whether current large language models could execute natural language-described algorithms. To address this gap, we first establish an algorithm test set from the classical textbook Introduction to Algo-

## Prompt

The initial keyword is "art". For each iteration, generate a sentence that MUST include the keyword, then select just a single word (rather than two or more words) from the generated sentence as the new keyword and print the new keyword. Iterate 5 times, with each iteration mark with its index, i.e. 1. 2. 3. etc.

1. Art is a form of expression that can be seen in many different mediums.
Keyword:
2. Mediums such as painting, sculpture, and photography are popular forms of art.
Keyword: sculpture
3. Sculpture is a three-dimensional art form that can be made from a variety of materials.
Keyword: materials
4. Materials such as clay, metal, and wood are often used in sculpture.
Keyword: wood
5. Wood carving is a popular form of sculpture that has been used for centuries.
Keyword: centuries
Table 1: The prompt for iterative sentence generation with keyword constraint and the response of Text-Davinci-003. According to the given instruction, the model faithfully executes the loop, repeatedly generating a text with the designated keyword and picking a new keyword. Different keywords are annotated with different colors.
rithm (Cormen et al., 2022) for systematic evaluation of the program execution ability of LLMs. We randomly sampled 10 distinct instances for each algorithm, which reduces the likelihood of data leakage. Based on the benchmark, we convert the algorithms together with the problem input into natural language description prompts, and input them into the LLMs, trying to see whether LLMs could execute the algorithm step by step accurately, and yield the correct result. Finally, we conduct experiments on 30 algorithms using three popular LLMs, namely Text-Davinci-003, GPT-3.5-Turbo (Ouyang et al., 2022), and GPT-4 (OpenAI, 2023), and systematically evaluate the ability of these LLMs as executors of natural language-described algorithms.

Our experiments reveal that the existing LLMs, especially GPT-4, can effectively run programs described in natural language. They can accurately follow the control flow of the algorithm as per the prompt description, precisely execute each step, and perform the calculation. Simultaneously, LLMs can maintain and update the values of variables consistently through the text output. This indicates that existing LLMs could execute statements of sequence, selection, and iteration, and mimic the core functions of the Von-Neumann Machine, including calculation, flow control, variable storage,
and input-output understanding. As a result, it's unlikely that they are not the interpreters of natural language-described programs.

Our main contributions are as follows:

1. We build up a test set of algorithms from a widely used algorithm textbook, establishing a foundation for evaluating the program execution abilities of LLMs;
2. We construct natural language prompts for the algorithms;
3. We test a series of algorithms on current state-of-the-art LLMs and systematically evaluate their abilities as natural language program interpreters.

We anticipate that the results presented in this research will stimulate further interest and research into the computation power of large language models. we are hopeful for further breakthroughs that will contribute positively to various domains of artificial intelligence.

## 2. Algorithm Prompting

### 2.1. Algorithm Selection

Guided by previous work (Veličković et al., 2022), we choose algorithms from the widely-used textbook for algorithm courses, Introduction to Algorithms (Cormen et al., 2022), listed in Section 3.2. We first pick 26 representative algorithms, forming the evaluation set CLRS-mini. These algorithm implementations involve sequence, selection, and iteration control flows, nested loops, and recursive calls, which could effectively evaluate the ability of LLMs to execute programs. They all have the polynomial time complexity and only involve integer/float addition and integer multiplication, so we expect the current SOTA LLM would conduct these tasks well. To further challenge the current LLMs, we additionally formulate another evaluation set CLRS-Numeric, which consists of 4 numeric-operation-intensive algorithms and requires floating-point multiplication/division and calculation of exponential and trigonometric functions. While today's LLM alone may not be able to solve them, we believe the aid of external tools such as Python Interpreter may be beneficial, and the performance of future LLMs on float operations remains to be seen.

### 2.2. Algorithm Prompt Design

In our design of program prompting, the aim is to create a prompt structure that is both rigorous and easy to interpret. Emphasizing precision, each task-specific instruction was written in clear, unambiguous natural language. As illustrated in Table 2 and Table 3, we employed "goto" statements to trigger iterative behaviors and use natural language to express if/else branch selection, with distinct

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the list of parentheses P: P[1] = '(' P[2] = ']' $\mathrm{P}[3]=$ ' ${ }^{\prime} \mathrm{P}[4]=$ ' (' .
Set Stack_1 = [].
Set $\mathrm{i}=1$.
Step 1: What are the value of P[i] and Stack_i ? Print them.
Step 2: What is the type of P[i] ? Classify it. Hint: '('' is the left parenthesis, '[' is the left parenthesis, ' $\{$ ' is the left parenthesis. ')' is the right parenthesis, ']' is the right parenthesis, ' $\}$ ' is the right parenthesis.
i. If $\mathrm{P}[\mathrm{i}]$ is the left parenthesis: Step by step push Stack_\{i+1\} as [(P[i], i)] + Stack_i.
ii. If $\mathrm{P}[\mathrm{i}]$ is the right parenthesis: Print Stack_i[0]. Is Stack_i[0] None? If Stack_i[0] is not None, step by step pop Stack_\{i+1\} as Stack_i[1:]. Otherwise, print "Invalid" and halt. Question: Are Stack_i[0][0] and P[i] matched? Print Stack_i[0][0] and P[i], apply the following rule, then answer: '(' and ')' matched, '[' and ']' matched, '\{' and '\}' matched. '(' and ']' not matched, '[' and ')' not matched, '\{' and ']' not matched; '(' and '\}' not matched, '[' and '\}' not matched, ' $\{$ ' and ')' not matched.
a. If yes, continue.
b. If no, print "Invalid" and halt.

Step 3: Increment i by 1. If $i<=4$, go to Step 1. Otherwise, proceed to Step 4.
Step 4: What is the value of Stack_5 ? Print it. What is the length of Stack_5 ? Count it.
i. If the length is 0 , print "Valid";
ii. If the length is greater than 0 , print "Invalid".

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $\mathrm{i}=1$, copy from Initial, $\mathrm{P}[1]=$ ' ('; Stack_1 = [].
2. The type of $\mathrm{P}[1]=$ '(' is the left parenthesis. Push Stack_2 as [('(', 1)] + Stack_1 = [('(', 1)] + [] = ['('', 1)].
3. Increment i by $1 . \mathrm{i}=2$.
4. $\mathrm{P}[2]=$ ' $]$ '; Stack_2 $=\left[\left({ }^{\prime}(', 1)\right]\right.$.
5. The type of $\mathrm{P}[2]=$ ']' is the right parenthesis. Print Stack_2[0] = ('(', 1). Stack_2[0] is not None, so pop Stack_3 as Stack_2[1:] = [].
6. Are Stack_2[0][0] and P[2] matched? Print Stack_2[0][0] = '(' and P[2] = ']'. '(' and ']' are not matched, so print "Invalid" and halt

Table 2: The prompt of valid parentheses and the response of Text-Davinci-003. This task examines if a sequence of parentheses is matched or not. Once a parenthesis is unmatched, returns invalid. If in the end, the stack is empty, return valid, otherwise still returns invalid. In this example, the second element is not matched with the first element, so the model correctly returns invalid and halts the execution. The final result Invalid is italicized, and the stopword halt is marked red.
branches denoted by index markers such as "i." and "ii." and Python-style spaces indent.

To facilitate stepwise parsing and execution, we asked the model to mark each line of the procedure with a sequential index, serving as a delimiter. This setup helped distinguish the current computation step that the model generated from the previously completed steps. We also included the first computation step within the prompt to ensure that the model was forced to execute the instructions rather than merely rephrasing them.

Inspired by the work of Jojic et al. (2023), encouraging the model to think step by step as much as possible is also crucial. Rather than using typical human expressions that place the final result before the reasoning (e.g., "Yes, ' (' and ' )' match"), we opted for a reasoning-first approach (e.g., "Are Stack_2[0][0] and P[2] matched? Print Stack_2[0][0] = ' (' and P[2] = ']'. '(' and ']' are not mat ched"). To force the model actually make the comparison between two values and overcome
the attempts of guessing and hallucination, we can tell the model to subtract the two values first, then check the sign of the result, which is exactly what the CPU actually performs. For example, instead of high-level statement "v - pi[u]", we ask the model to "Calculate bne_v_pi_u = v pi[u] and present the result.". It's also worth noting that fetching the value of an array at a specific index can be non-trivial since it includes addressing operation, so if the list is constant, we explicitly express the value at each position, for example, " P [1] = ' (' ", rather than simply states " $P=['(', '] ', ~ '\} ', ~ '('] ~ ", ~ w h i c h ~$ requires more computation in finding the needed value. Similarly, in the instruction we replace the constant variables with their actual value. For example, instead of " $i<n$ ", where the value of $n$ is 4 , we explicitly state " $i<4$ ".

Similar to the prior work (Jojic et al., 2023), to ensure the alignment between the words used in the prompts and the actions they represented, in the task of valid parentheses, we set "halt" as the

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array $A: A[0]=4, A[1]=5, A[2]=7, A[3]=8, A[4]=13, A[5]=14, A[6]=15, A[7]=17, A[8]=$ 18.

Set the length of the array n : 9 .
Set the target element x: 18.
Set the low index I to the first element of the array $(I=0)$ and the high index $r$ to the last element $(r=8)$.
Step 1: Calculate the middle index mid. mid $=I+(r-I) / / 2$. Print the values of $I, r$, and mid.
Step 2: Compare the element at the middle index $A[m i d]$ with the target element $x$.
i. If $A[m i d]==x$, return mid and halt.
ii. If $A[m i d]<x$, set $I=$ mid +1 and proceed to Step 3.
iii. If $A[$ mid $]>x$, set $r=$ mid -1 and proceed to Step 3.

Step 3: Check if the search space is exhausted ( $1<=r$ ).
i. If $\mathrm{I}<=\mathrm{r}$, go back to Step 1 .
ii. If $I>r$, return -1 and halt.

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $I=0, r=8, \operatorname{mid}=0+(8-0) / / 2=4$.
2. $A[$ mid $]=A[4]=13$, which is less than $x(18)$, so set $I=\operatorname{mid}+1=4+1=5$.
3. I (5) is less than or equal to $r(8)$, so go back to Step 1.
4. $I=5, r=8$, mid $=5+(8-5) / / 2=6$.
5. $A[$ mid $]=A[6]=15$, which is less than $x(18)$, so set $I=\operatorname{mid}+1=6+1=7$.
6. I (7) is less than or equal to $r(8)$, so go back to Step 1 .
7. $1=7, r=8$, $\operatorname{mid}=7+(8-7) / / 2=7$.
8. $A[$ mid $]=A[7]=17$, which is less than $x(18)$, so set $I=\operatorname{mid}+1=7+1=8$.
9. I (8) is less than or equal to $r(8)$, so go back to Step 1.
10. $I=8, r=8$, mid $=8+(8-8) / / 2=8$.
11. $A[$ mid $]=A[8]=18$, which is equal to $x(18)$, so return mid ( 8 ) and halt.

Table 3: The prompt of binary search and the response of GPT-4. Binary search is a search algorithm used to find the position of a key in a sorted array. It works by repeatedly dividing the search interval in half until the target value is found or determined to be not present. The search interval is defined by two indices, the lower bound and the upper bound which are adjusted on each iteration. In this example, GPT-4 correctly found the position of element " 18 ", which is at the 8 th position.
stopword to prevent the model (especially GPT 3.5) from continuing generation after detecting the error. Furthermore, we took measures to prevent the model from skipping steps as the output became longer and repetitive. We prohibited the use of words such as "...", "Repeat", or "Continue", which could lead to overlooked or incomplete steps, and result in the wrong answer. The example prompts are presented at Table 2 and 3.

Our method of prompting is different from that of Liu et al. (2023). Ours requires few operations defining and mainly relies on the actions that natural language commonly represents. Moreover, since the semantics of natural language goes far beyond formal language, we may easily express complex tasks like "generate a sentence" in a zero-shot manner, in which traditional programming languages are struggling Leveraging the power of instructionfollowing (Ouyang et al., 2022), we argue that without concrete examples and repetitive deletion of previous history context (Jojic et al., 2023), it’s still possible to trigger GPT into a computation device given the program alone. On the other hand, pure programming language prompt leads to low accu-
racy (Jojic et al., 2023). This is because GPT may not always parse the program correctly as the real interpreter or compiler does, or be triggered to think step by step without "jumping to conclusions". However, by crafting with more detail and clarity, our natural language prompt offers better performance.

### 2.3. Test Case Generation

Unlike previous work (Veličković et al., 2022), which used a problem size of 16 for training and validation and 64 for testing, we adjusted ours to be smaller. This adjustment was due to concerns about the context-length limit, generation time, and inference cost. Generally, we set the problem size to 9 and 10 for tasks that only need a single iteration, and 4 and 5 , or even smaller, for more complex tasks that require a long generation length. For algorithms that require sorting, we pre-sorted the input data to save the length of instruction and generation. And since we would select various sorting algorithms for testing, this simplification would not reduce the diversity of our evaluation. For each task, we randomly sample 10 instances. Just as in the case of
algorithm competitions, we set the final output of the algorithm as the gold answer, and consider the prediction correct if the value presented in the last line is exactly the same. For the tasks in CLRSNumeric, we allow an absolute tolerance of 0.1.

## 3. Experiments

### 3.1. Setup

For language model, we use GPT-3.5 (Ouyang et al., 2022) text-davinci-003 and gpt-3.5-turbo-0301 versions with 4 k context window, and GPT-4 (OpenAI, 2023) gpt-4-0314 version with 8 k context window. They are accessed via OpenAI API. The temperature is consistently set to 0 . All results are from a single run.
We also set a baseline of Python Code, which only replaces the step-by-step natural instructions of the algorithm with the corresponding program, while the input data is unchanged. This can help to investigate the effectiveness of our proposed design.

### 3.2. Testing algorithms

For CLRS-mini, we select 26 classical algorithms, namely insertion sort, bubble sort, heapsort (Williams, 1964), quicksort (Hoare, 1961a), minimum search, binary search, quickselect (Hoare, 1961b), maximum subarray (Bentley, 1984), activity selection (Gavril, 1972), task scheduling (Lawler, 1985), matrix chain multiplication, longest common subsequence, optimal binary search tree (Aho and Hopcroft, 1974), depth-first search (Moore, 1959), breadth-first search (Moore, 1959), topological sorting (Knuth, 1973), articulation points, bridges, Kosaraju's strongly connected components (Aho and Hopcroft, 1974), Kruskal's minimum spanning tree (Kruskal, 1956), Prim's minimum spanning tree (Prim, 1957), Bellman-Ford algorithm for singlesource shortest paths (Bellman, 1958), Dijkstra's algorithm for single-source shortest paths (Dijkstra, 2022), Floyd-Warshall algorithm for all-pairs shortest-paths (Floyd, 1962), naive string matching, and Knuth-Morris-Pratt string matcher (Colussi, 1994). For CLRS-Numeric, we select 4 algorithms emphasizing the arithmetic operations, including Least Square Regression, Discrete Fourier Transform, and two convex hull algorithms of Graham Scan (Graham, 1972) and Jarvis March (Jarvis, 1973). The time complexity and problem size of each task would be in the appendix once published.

Apart from the above ones, we also included two tasks, valid parentheses and longest common subsequence (short), for comparison with previous work (Jojic et al., 2023). Both of which come from BIG-bench cs-algorithms category (Srivastava
et al., 2022). The task of valid parentheses is to verify if a sequence of parentheses consisting of three different types is balanced or not, which requires stack manipulation, and it has $\mathbf{1 , 0 0 0}$ test instances with the maximum length of 20 . As for longest common subsequence, the goal is to compute the length of longest common subsequence given two sequences, and two nested loops are needed to complete the task. Due to the context-length issue, Jojic et al. (2023) limited the maximum length to 6 and constructed a new test set of 100 instances.

| Model | Acc (\%) |
| :--- | :--- |
| Random | 50.0 |
| GPT-3, few shot (Srivastava et al., 2022) | 57.8 |
| PALM 2, few shot (Anil et al., 2023) | 83.4 |
| IRSA (Jojic et al., 2023) | 96.0 |
| GPT-3.5-Turbo | 66.0 |
| Text-Davinci-003 | $\mathbf{1 0 0}$ |
| GPT-4 | $\mathbf{1 0 0}$ |

Table 4: Results of valid parentheses.

| Model | Acc (\%) |
| :--- | :--- |
| Random | 44 |
| GPT-3, few shot (Jojic et al., 2023) | 7 |
| IRSA (Jojic et al., 2023) | 93 |
| GPT-4, code exec (Jojic et al., 2023) | 69 |
| GPT-3.5-Turbo | 38 |
| Text-Davinci-003 | 71 |
| GPT-4 | $\mathbf{1 0 0}$ |

Table 5: Results of longest common subsequence.

## 4. Results

### 4.1. Previous Tasks

Table 4 presents the result of the valid parentheses task. Previously, Jojic et al. (2023) proposed the method of IRSA. They leveraged prompts made of similar operation procedure examples, rather than instruction, to trigger the execution, and for post-processing, they delete the computation process and save only the final state once the model completes an iteration. For LLM, they chose GPT-3 Code-Davinci-0 02 version, claiming it provides similar results but has lower cost compared with Text-Davinci-002 or Text-Davinci-003. IRSA achieved $96 \%$ accuracy, which is already impressive. But with our natural language program prompting, both Text-Davinci003 and GPT-4 models reached 100\% accuracy, demonstrating the effectiveness of our method in perfectly solving this task.

| Task | Natural Language Prompt (Ours) |  |  | Python Code |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | GPT-3.5-T | Davinci-003 | GPT-4 | GPT-3.5-T | Davinci-003 | GPT-4 |
| Sorting |  |  |  |  |  |  |
| Insertion Sort | 50 | 80 | 100 | 80 | 70 | 100 |
| Bubble Sort | 60 | 70 | 100 | 100 | 0 | 100 |
| Heapsort | 90 | 20 | 100 | 60 | 70 | 50 |
| Quicksort | 70 | 100 | 100 | 90 | 80 | 100 |
| Searching |  |  |  |  |  |  |
| Minimum | 90 | 60 | 100 | 30 | 20 | 70 |
| Binary Search | 90 | 100 | 100 | 90 | 70 | 100 |
| Quick Select | 50 | 70 | 100 | 30 | 40 | 60 |
| Strings |  |  |  |  |  |  |
| Naive String Matching | 90 | 80 | 100 | 20 | 50 | 100 |
| Knuth-Morris-Pratt | 30 | 10 | 100 | 20 | 0 | 80 |
| Divide and Conquer |  |  |  |  |  |  |
| Maximum Subarray | 40 | 0 | 100 | 30 | 40 | 20 |
| Greedy |  |  |  |  |  |  |
| Activity selection | 0 | 0 | 100 | 10 | 0 | 100 |
| Task scheduling | 40 | 50 | 100 | 60 | 10 | 80 |
| Dynamic programming |  |  |  |  |  |  |
| Matrix Chain Multiplication | 30 | 10 | 100 | 20 | 0 | 50 |
| Longest Common Subsequence | 30 | 60 | 100 | 20 | 50 | 70 |
| Optimal Binary Search Tree | 0 | 10 | 100 | 0 | 0 | 20 |
| Graphs |  |  |  |  |  |  |
| Depth-First Search | 0 | 0 | 100 | 0 | 0 | 60 |
| Breadth-First Search | 10 | 0 | 100 | 10 | 0 | 80 |
| Topological Sorting | 10 | 10 | 100 | 0 | 10 | 20 |
| Articulation Points | 0 | 0 | 100 | 0 | 0 | 30 |
| Bridges | 20 | 20 | 100 | 20 | 20 | 50 |
| Strongly Connected Components | 0 | 0 | 100 | 0 | 0 | 0 |
| Kruskal's MST | 50 | 60 | 100 | 20 | 40 | 70 |
| Prim's MST | 10 | 0 | 100 | 0 | 0 | 80 |
| Bellman-Ford | 20 | 0 | 100 | 0 | 0 | 100 |
| Dijkstra | 0 | 0 | 100 | 0 | 10 | 90 |
| Floyd-Warshall | 0 | 100 | 100 | 0 | 0 | 0 |
| Average | 35.0 | 36.2 | 100.0 | 27.3 | 25.4 | 65.4 |

Table 6: Results of CLRS-mini.

As shown in Table 5, the GPT-4 model was the only model to achieve perfect accuracy in the longest common subsequence task. Although with regimenting attention, which is to delete useless history context, IRSA method scored a high accuracy of $93 \%$, it is clear that the GPT-4 model demonstrated a stronger ability to handle this complex task.

### 4.2. CLRS-mini

We observe that GPT-4 demonstrates exceptional performance in comparison to the GPT-3.5 models, achieving an impressive $100 \%$ accuracy across all tasks. This illustrates its outstanding capacity for precise program execution and implies a significant enhancement in algorithm execution when compared to its predecessors. On average, Text-

Davinci-003 (36.9\%) performs marginally better than GPT-3.5-Turbo (35.0\%), but both still fall significantly behind GPT-4.

Partly due to the $4 k$ context length limit, the GPT3.5 models yielded a score of 0 in numerous graph algorithms, as these tasks require more tokens to complete. As the complexity of the tasks increases, the instruction encompasses more information, the control flow grows more intricate, and the required number of generation tokens also rises. Consequently, the performance of both GPT-3.5 models tends to decline. However, GPT-4 successfully manages to tackle these intricate tasks, highlighting its capabilities in simulating natural language programs.

Compared with detailed instruction, under Python Code only, the average performance of all three models declines. Especially for GPT-4, only
in relatively simple algorithms the model can get good accuracy, but as the complexity increases, the results drop. This echoes the previous findings that GPT-4 may not faithfully execute the program, and the intuition is that traditionally in computer science, the high-level Python code itself would require an interpreter to be analyzed first, for example, the transition between code lines needs to be determined.

### 4.3. CLRS-Numeric

Intriguingly, across all three evaluated models, a uniform performance result of $0 \%$ was observed, illuminating a pronounced and universal challenge encountered by current LLMs in handling such complex numerical operations. Inspecting the generation results, we found that GPT-4 still follow the instruction step by step and manages to generate a well-format wrong answer, indicating the errors mainly come from miscalculation. For example, in the least square regression task, despite its inability to conduct the actual computation within the generation of a few tokens, GPT-4 still manages to guess a float number, which is likely to be inaccurate, and continue the rest of the algorithm execution, as if the computed number is correct.

| Algorithm | Model | Acc |
| :--- | :--- | :--- |
| Least Square Regression | GPT-3.5-T | 0 |
|  | Davinci-003 | 0 |
|  | GPT-4 | 0 |
| Discrete Fourier Transform | GPT-3.5-T | 0 |
|  | Davinci-003 | 0 |
|  | GPT-4 | 0 |
| Graham Scan | GPT-3.5-T | 0 |
|  | Davinci-003 | 0 |
|  | GPT-4 | 0 |
| Jarvis March | GPT-3.5-T | 0 |
|  | Davinci-003 | 0 |
|  | GPT-4 | 0 |

Table 7: Results of CLRS-Numeric

### 4.4. Intermediate Results Evaluation

To further investigate the reason behind success/failure, we select 5 algorithms, Bubble Sort, Knuth-Morris-Pratt (Strings), Task Scheduling (Greedy), Optimal Binary Search Tree (Dynamic Programming) and Breadth-First Search (Graphs), which are relatively easy to extract and evaluate the intermediate results. The transition sequence of intermediate results for each algorithm is as follows:

[^1]- Knuth-Morris-Pratt: the longest proper prefix list lps.
- Task Scheduling: the list job.
- Optimal Binary Search Tree: the matrix $d p$.
- Breadth-First Search: the queue $Q$.

We can obtain the gold intermediate results by running the algorithm programs. For metrics, we compute the metric of Intermediate Accuracy, which requires all the intermediate results to be correct. We also compute the metric of Process Accuracy, which computes the ratio of correct intermediate sequence prefix, averaged over $N$ instances. The intuition is that, once an intermediate result goes wrong, the following computation based on the previous one would also be problematic:

$$
\text { Process }=\frac{1}{N} \sum_{i} \frac{\text { len }(\text { correct_prefix } \text { ) }}{\max \left(\text { len }\left(\text { pred }_{i}\right), \text { len }\left(\text { gold }_{i}\right)\right)}
$$

The results are shown in Table 8. We find that by replacing detailed instruction with "uninterpreted" Python code, the Intermediate Accuracy and Process Accuracy drop noticeably together with the Final Accuracy, as the scores of GPT-4 are no longer all $100 \%$. This further demonstrates the necessity of our proposed method. Under detailed instruction, GPT-4 did not make any mistakes in computing intermediate results, which further confirms its effectiveness and ability. For GPT-3.5-Turbo and Text-Davinci-003, lower final accuracy is associated with lower intermediate correctness.

Also, Process Accuracy and Intermediate Accuracy may not be smaller than Final accuracy, indicating that correct intermediate computation would be much more likely to lead to the correct final answer, while one single error would result in the wrong answer. Moreover, as expected, the inability to produce error-free intermediate results, which is largely due to miscalculation, contributes to the low performance of two GPT-3.5 models.

## 5. Discussion

### 5.1. Challenges of Step-wise Evaluation

Rigorous step-by-step evaluation of the model's computation process is non-trivial, since it would require an equivalent Turing Machine to compute that step and check if the result is consistent. And due to the flexible natural language style, it's challenging to extract the intermediate results by pure hand-written regular expression. Moreover, for a single model GPT-4, as each test instance could contain 100 lines, and we have 260 cases in total, with lengthy model-generated outputs, human annotation would be costly and time-consuming, yet

| Algorithm | Model | Final | Interm. | Proc. |
| :--- | :--- | :--- | :--- | :--- |
| Bubble Sort | GPT-3.5-T | 60 | 60 | 71.7 |
|  | Davinci-003 | 70 | 70 | 81.4 |
|  | GPT-4 | 100 | 100 | 100.0 |
| KMP | GPT-3.5-T | 30 | 80 | 86.7 |
|  | Davinci-003 | 10 | 50 | 66.7 |
|  | GPT-4 | 100 | 100 | 100.0 |
| Task | GPT-3.5-T | 40 | 40 | 71.0 |
| Scheduling | Davinci-003 | 50 | 50 | 50.0 |
|  | GPT-4 | 100 | 100 | 100.0 |
| Optimal BST | GPT-3.5-T | 0 | 0 | 43.2 |
|  | Davinci-003 | 10 | 0 | 4.4 |
|  | GPT-4 | 100 | 100 | 100.0 |
| BFS | GPT-3.5-T | 10 | 0 | 18.7 |
|  | Davinci-003 | 0 | 0 | 0.0 |
|  | GPT-4 | 100 | 100 | 100.0 |

(a) Natural Language Prompt (Ours)

| Algorithm | Model | Final | Interm. | Proc. |
| :--- | :--- | :--- | :--- | :--- |
| Bubble Sort | GPT-3.5-T | 100 | 100 | 100.0 |
|  | Davinci-003 | 0 | 60 | 72.2 |
|  | GPT-4 | 100 | 100 | 100.0 |
| KMP | GPT-3.5-T | 20 | 50 | 73.3 |
|  | Davinci-003 | 0 | 40 | 66.7 |
|  | GPT-4 | 80 | 100 | 100.0 |
| Task | GPT-3.5-T | 60 | 60 | 82.0 |
| Scheduling | Davinci-003 | 10 | 10 | 15.0 |
|  | GPT-4 | 80 | 80 | 86.5 |
| Optimal BST | GPT-3.5-T | 0 | 0 | 46.4 |
|  | Davinci-003 | 0 | 0 | 5.4 |
|  | GPT-4 | 20 | 20 | 72.2 |
| BFS | GPT-3.5-T | 10 | 10 | 21.5 |
|  | Davinci-003 | 0 | 0 | 1.4 |
|  | GPT-4 | 80 | 80 | 87.1 |

(b) Python Code

Table 8: Intermediate Results Evaluation
$100 \%$ accuracy is not guaranteed, making it also not feasible.
But from another perspective, as the algorithm becomes more complex, it's more challenging to guess a correct solution without actually computing step-by-step, and since the current state depends on the previous state, the chances of passing all the test cases for the wrong reason are more and more unlikely. Therefore, correct outcomes in all cases highly indicate the correctness of the intermediate computation steps.

### 5.2. On the Possibility of Data Leakage and Memorization

As mentioned previously, the test data was randomly generated. Given the vast input space,
although the algorithms themselves are widely known, it's highly unlikely that our concrete randomly generated instances overlap with examples available online. Moreover, due to the complexity of the algorithms, memorization is unlikely to result in successful execution. Since the input space is exponentially large, simple memorization of finite, linear training instances would not guarantee the performance on arbitrary new test cases; on the other hand, feeding exponential training instances would bring the issue of catastrophic forgetting.

Lastly, our experiment results do not support the data leakage hypothesis. If GPT-4 is trained on similar data, replacing our detailed yet Internetunavailable natural instruction with easily found Python code would not greatly reduce the performance, which is not the case.

## 6. Related Works

### 6.1. Large Language Models

GPT-3 (Brown et al., 2020), the first large language model (LLM) with 175 billion parameters, pioneered the trend. It showcased that without fine-tuning, LLMs can accomplish various tasks effectively via trigger strategies like few-shot (Brown et al., 2020) or chain-of-thought prompting (Wei et al., 2022d), which is observed as an emergent ability (Wei et al., 2022c). Since then, various new LLMs have been proposed (Scao et al., 2022; Touvron et al., 2023; OpenAI, 2023; Anil et al., 2023). In parallel, researchers have proposed theories to explain how performance improves as the model size increases (Kaplan et al., 2020; Hoffmann et al., 2022). Beyond unsupervised learning, a range of approaches for "instruction tuning" have been introduced (Wei et al., 2022b; Sanh et al., 2022; Wang et al., 2022; Ouyang et al., 2022). Instruction tuning aims to refine LLMs, making them more efficient and accessible for downstream applications.

### 6.2. Turing-Completeness of Neural Networks

The Turing-completeness (Turing, 1937) of neural networks has been extensively studied. Siegelmann and Sontag (1995) first provided an early demonstration that neural networks can simulate all Turing machines. Subsequently, Graves et al. (2014) developed the Neural Turing Machine. Similarly,Weiss et al. (2018) explored the computational power of RNNs, and later the computational properties of Transformers are studied (Pérez et al., 2019; Bhattamishra et al., 2020; Wei et al., 2022a). Recently, Schuurmans (2023) and Jojic et al. (2023) demonstrated the computational universality of large language models without further fine-tuning.

### 6.3. LLMs for Coding Tasks

LLMs have advanced a series of code-related tasks, including code generation (Bareiß et al., 2022), and particularly competitive programming (Li et al., 2023, 2022). In addition, tools like GitHub Copilot and others (Chen et al., 2021; Joshi et al., 2023) have harnessed the power of LLMs to assist developers. Furthermore, LLMs have also been applied to test generation (Schäfer et al., 2024) and code explanation (Nam et al., 2024).

## 7. Conclusion

In summary, our research shows compelling evidence that large language models, especially GPT4, can effectively interpret and execute algorithms described in natural language. These models demonstrated astonishing performance in following control flow and performing precise calculations and operations. They also exhibited strong capabilities in maintaining and updating variable values via text output. Such attributes mimic the core functions of the Von-Neumann Machine. Consequently, we can potentially instruct these models to perform complex operations merely through natural language prompts. We hope our research could shed light on further investigation of evaluating and leveraging the capabilities of large language models.

## 8. Acknowledgements

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## 9. Limitations

In this work, we use GPT-3.5 and GPT-4, which are not open-sourced and may only be accessed via API. Future works are needed to evaluate on publicly-available large language models once such models reach the performance of GPT-3.5 or even GPT-4.

## 10. Ethics Statement

This work is conducted in compliance with ethical principles. This work involves no sensitive data and uses several public-available datasets, or generates new datasets by random sampling.

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## A. Appendix

## A.1. Evaluation of Iterative Sentence Generation with Keyword Constraint

Task We argue that our method, program prompting, does not limit to pure program execution. To this end, we proposed a novel task, iterative sentence generation with keyword constraint, which contains 100 test instances. With the input of the initial keyword and iteration count, the task of iterative sentence generation with keyword constraint is to generate a sentence given the keyword, then select a word from the generation as the new keyword, and stop when reaching the iteration limit. The 20 initial words include "art", "business", "computer", "data", "entertainment", "environment", "fashion", "investigation", "lifestyle", "market", "medicine", "music", "politic", "science", "sports", "technology", "trade", "traffic", "weather", and "world". The iteration counts are 5, 10, 15, 20, and 25. The prompt is presented in Table 1.

Result GPT-4 model outperformed the others, achieving 100\% accuracy as shown in Table 9. Text-Davinci-003 model achieved a high accuracy of $98 \%$, nearly matching the performance of GPT4, while GPT-3.5-Turbo lagged behind with 58\% accuracy.

| Model | Accuracy (\%) |
| :--- | :--- |
| GPT-3.5-Turbo | 58 |
| Text-Davinci-003 | 98 |
| GPT-4 | $\mathbf{1 0 0}$ |

Table 9: Results of iterative sentence generation with keyword constraint

## A.2. On the Construction of Natural Language Prompt

We believe that program execution is a mechanical, deterministic procedure, unlike open-domain text generation, where the needed information is not fully present in the prefix. In the process of execution, as long as the LLMs predict the next correct token with more than $50 \%$ probability, we can ensure the final correctness of the whole output.
Therefore, the main intuition is that we need to tell LLMs how to jump between the instructions, which usually is the task of the compiler of high-level program language. For simplicity of methodology, we leverage the goto statement. Moreover, for future works, we believe it would also be feasible to leverage LLM+compiler to complete the conversion.
Another trick for writing unambiguous instructions is to avoid repeated words but without dif-
ferent meanings. We can scan the instructions, and replace any unintended repetition. Also, for some functions like sort or argmax, we shall clearly "implement" the details, just like when we use old Pascal to write code.

Finally, after manually constructing the prompt, we may leverage few-shot in-context learning to build the draft of other algorithms, in which GPT4 can mimic the rigid, unambiguous style. Then, we manually inspect the draft carefully, and fix the mistakes.

| Time Complexity | Input Size | Algorithm |
| :--- | :--- | :--- |
| $O($ logn $)$ | 9,10 | Binary Search |
| $O(n)$ | 9,10 | Minimum Search |
|  | 9,10 | Activity Selection* |
|  | 9,10 | Task Scheduling* |
|  | 9,10 | Least Square Regression |
| $O(n)$ | 4,5 | Maximum Subarray |
|  | 4,5 | Quickselect |
|  | 4,5 | Kruskal's Minimum Spanning Tree* |
| $O(n+m)$ | 4,5 | Depth-First Search |
|  | 4,5 | Breadth-First Search |
|  | 4,5 | Topological Sorting |
|  | 3,4 | Articulation Points |
|  | 3,4 | Bridges |
|  | 4,5 | Kosaraju's Strongly Connected Components |
|  | 4,5 | Knuth-Morris-Pratt String Matcher |
| $O(n l o g n)$ | 4,5 | Heapsort |
|  | 4,5 | Quicksort |
|  | 8 | Discrete Fourier Transform |
|  | 9,10 | Graham Scan |
| $O\left(n^{2}\right)$ | 4,5 | Insertion Sort |
|  | 4,5 | Bubble Sort |
|  | 4,5 | Optimal Binary Search Tree |
|  | 4,5 | Dijkstra's Algorithm |
|  | 4,5 | Prim's Minimum Spanning Tree |
| $O(n m)$ | 4,5 | Naive String Matching |
|  | 4,5 | Bellman-Ford Algorithm |
|  | 4,5 | Longest Common Subsequence |
|  | 9,10 | Jarvis March |
| $O\left(n^{3}\right)$ | 4,5 | Matrix Chain Multiplication |
|  | 4 | Floyd-Warshall Algorithm |

Table 10: The time complexity and input size (the length of input vector) of selected algorithms, sorted by time complexity. For algorithms with greater complexity, they require longer instruction and output length. so we choose a smaller problem size to avoid exceeding the context length limit and save the inference time and cost. The Asterisk * denotes that the input is sorted.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the deadlines array $D: D[0]=0, D[1]=3, D[2]=1, D[3]=0$.
Set the deadlines array $\mathrm{W}: \mathrm{W}[0]=10, \mathrm{~W}[1]=68, \mathrm{~W}[2]=68, \mathrm{~W}[3]=84$.
Set the length of the arrays $\mathrm{n}: 4$.
Set the maximum time slots t : 3 .
Initialize an array called 'result': [False, False, False, False].
Initialize an array called 'job': $[-1,-1,-1,-1]$.
Step 1: Set $\mathrm{i}=0$.
Step 2: Set $\mathrm{j}=\min (\mathrm{t}, \mathrm{d}[\mathrm{i}])$.
Step 3: Is result[j] False?
i. If result[j] is False, set result[j] to True, assign job[j] = i, print the array of result and job, and proceed to Step 5.
ii. If result[j] is True, proceed to Step 4.

Step 4: Decrement j by 1 . If $\mathrm{j}>-1$, go back to Step 3; otherwise, $\mathrm{j}<=-1$, proceed to Step 5.
Step 5: Increment i by 1. If $\mathrm{i}<4$, go back to Step 2; otherwise, $\mathrm{i}>=4$, proceed to Step 6.
Step 6: Print the 'job' array.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. etc.):

1. $i=0$.
2. $j=\min (3, D[0])=\min (3,0)=0$.
3. result[ $[0]$ is False, so set result[0] to True, job[0] = 0, print result: [True, False, False, False], print job: [0, -1 ,
$-1,-1]$.
4. $i=1$.
5. $j=\min (3, D[1])=\min (3,3)=3$.
6. result[3] is False, so set result[3] to True, job[3] = 1, print result: [True, False, False, True], print job: [0, -1 , $-1,1]$.
7. $i=2$.
8. $j=\min (3, D[2])=\min (3,1)=1$.
9. result[1] is False, so set result[1] to True, job[1] = 2, print result: [True, True, False, True], print job: [0, 2, -1 , 1].
10. $i=3$.
11. $j=\min (3, D[3])=\min (3,0)=0$.
12. result[0] is True, so proceed to Step 4.
13. $\mathrm{j}=0-1=-1$.
14. Since $\mathrm{j}<=-1$, proceed to Step 5 .
15. $i=4$.
16. Since $i>=4$, proceed to Step 6.
17. Print the 'job' array: [0, 2, -1, 1].

Table 11: The prompt of task scheduling and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Lazy shortcuts like "Continue this process" or "Repeat Steps" is prohibited, since insufficient computation would result in wrong answer. Do not stop before completion. Define two input sequences $A: A[1]=$ 'b' $A[2]=$ 'c' $A[3]=$ ' $c^{\prime} A[4]=$ 'b' $A[5]=$ ' $a$ ',
and B: B[1] = 'c' B[2] = 'c' B[3] = 'a' B[4] = 'a'.
Create a 2D table, called $f$, of size $(5+1) \times(4+1)$.
Step 1: Initialize the first row and the first column of the f table to 0 .
Step 2: Set $\mathrm{i}=1$.
Step 3: Set $\mathrm{j}=1$.
Step 4: Compare the elements $A[i]$ and $B[j]$, and answer the question: Are they equal or not?
a. If yes: Increase. Step by step set $f[i][j]$ to $f[i-1][j-1]+1$. For example, "f[1][1] $=f[1-1][1-1]+1=f[0][0]+1=0+1$ = 1."
b. If no: Select. Step by step set $f[i][j]$ to the maximum value of $f[i-1][j]$ and $f[i][j-1]$. For example, "f[1][1]= $\max (f[1-1][1], f[1][1-1])=\max (f[0][1], f[1][0])=\max (0,0)=0 . "$
Step 5: Increment j by 1. If j < $=4$, go to Step 4. If $\mathrm{j}>5$, increment i by 1 , and go to Step 6.
Step 6: If $\mathfrak{i}<=5$, go to Step 3. If $\mathfrak{i}>6$, proceed to Step 7 .
Step 7: Print the length of the LCS, which is the value of $f[5][4]$.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $\mathrm{f}[0][0]=0, f[0][1]=0, f[0][2]=0, f[0][3]=0, f[0][4]=0$.
$\mathrm{f}[1][0]=0, \mathrm{f}[2][0]=0, \mathrm{f}[3][0]=0, \mathrm{f}[4][0]=0, f[5][0]=0$.
2. $i=1$.
3. $\mathrm{j}=1$.
4. Copied $\mathrm{A}[1]=$ 'b' and $\mathrm{B}[1]=$ 'c' , is 'b' equal to 'c'? No. Select. $f[1][1]=\max (f[1-1][1], f[1][1-1])=\max (f[0][1]$, $\mathrm{f}[1][0])=\max (0,0)=0$.
5. $\mathrm{j}=2$.
6. $A[1]=$ 'b' and $B[2]=$ ' $c$ ', is ' $b$ ' equal to ' $c$ '? No. Select. $f[1][2]=\max (f[1-1][2], f[1][2-1])=\max (f[0][2], f[1][1])=$ $\max (0,0)=0$.
7. $\mathrm{j}=3$.
8. $A[1]=$ 'b' and $B[3]=$ ' $a$ ', is 'b' equal to 'a'? No. Select. $f[1][3]=\max (f[1-1][3], f[1][3-1])=\max (f[0][3], f[1][2])=$ $\max (0,0)=0$.
9. $\mathrm{j}=4$.
10. $A[1]=$ ' $b$ ' and $B[4]=$ ' $a$ ', is 'b' equal to ' $a$ '? No. Select. $f[1][4]=\max (f[1-1][4], f[1][4-1])=\max (f[0][4], f[1][3])=$ $\max (0,0)=0$.
11. $i=2$.
12. $\mathrm{j}=1$.
13. $A[2]=$ ' $c$ ' and $B[1]=$ ' $c$ ', is ' $c$ ' equal to ' ' ${ }^{\prime}$ '? Yes. Increase. $f[2][1]=f[2-1][1-1]+1=f[1][0]+1=0+1=1$.
14. $\mathrm{j}=2$.
15. $A[2]=$ ' $c$ ' and $B[2]=$ ' $c$ ', is ' $c$ ' equal to ' $c$ '? Yes. Increase. $f[2][2]=f[2-1][2-1]+1=f[1][1]+1=0+1=1$.
16. $\mathrm{j}=3$.
17. $A[2]=$ ' $c$ ' and $B[3]=$ ' $a$ ', is 'c' equal to 'a'? No. Select. $f[2][3]=\max (f[2-1][3], f[2][3-1])=\max (f[1][3], f[2][2])=$ $\max (0,1)=1$.
18. $j=4$.
19. $A[2]=$ ' $c$ ' and $B[4]=$ ' $a$ ', is ' $c$ ' equal to ' $a$ '? No. Select. $f[2][4]=\max (f[2-1][4], f[2][4-1])=\max (f[1][4], f[2][3])=$ $\max (0,1)=1$.
20. $i=3$.
21. $\mathrm{j}=1$.
22. $A[3]=$ ' $c$ ' and $B[1]=$ ' $c$ ', is ' $c$ ' equal to ' $c$ '? Yes. Increase. $f[3][1]=f[3-1][1-1]+1=f[2][0]+1=0+1=1$.
23. $\mathrm{j}=2$.
24. $A[3]=$ ' $c$ ' and $B[2]=$ ' $c$ ', is ' $c$ ' equal to ' $c$ '? Yes. Increase. $f[3][2]=f[3-1][2-1]+1=f[2][1]+1=1+1=2$.
25. $\mathrm{j}=3$.
26. $A[3]=$ ' $c$ ' and $B[3]=$ ' $a$ ', is 'c' equal to 'a'? No. Select. $f[3][3]=\max (f[3-1][3], f[3][3-1])=\max (f[2][3], f[3][2])=$ $\max (1,2)=2$.
27. $\mathrm{j}=4$.
28. $A[3]=$ ' $c$ ' and $B[4]=$ ' $a$ ', is ' 'c' equal to 'a'? No. Select. $f[3][4]=\max (f[3-1][4], f[3][4-1])=\max (f[2][4], f[3][3])=$ $\max (1,2)=2$.
29. $i=4$.
30. $j=1$.
31. $A[4]=$ 'b' and $B[1]=$ ' $c$ ', is 'b' equal to 'c'? No. Select. $f[4][1]=\max (f[4-1][1], f[4][1-1])=\max (f[3][1], f[4][0])=$ $\max (1,0)=1$.
32. $\mathrm{j}=2$.
```
33. A[4] = 'b' and B[2] = 'c', is 'b' equal to 'c'? No. Select. f[4][2] = max(f[4-1][2],f[4][2-1])= max(f[3][2], f[4][1])=
max}(2,1)=2
34. j= 3.
35. A[4] = 'b' and B[3] = 'a', is 'b' equal to 'a'? No. Select. f[4][3] = max(f[4-1][3],f[4][3-1]) = max(f[3][3],f[4][2])=
max(2, 2) = 2.
36. j=4.
37. A[4] = 'b' and B[4] = 'a', is 'b' equal to 'a'? No. Select. f[4][4] = max(f[4-1][4],f[4][4-1])= max(f[3][4],f[4][3])=
max(2, 2) = 2.
38. i= 5.
39. j= 1.
40. A[5] = 'a' and B[1] = 'c', is 'a' equal to 'c'? No. Select. f[5][1] = max(f[5-1][1],f[5][1-1]) = max(f[4][1],f[5][0])=
max}(1,0)=1
41. j = 2.
42. A[5] = 'a' and B[2] = 'c', is 'a' equal to 'c'? No. Select. f[5][2] = max(f[5-1][2], f[5][2-1]) = max(f[4][2],f[5][1])=
max}(2,1)=2
43. j = 3.
44. A[5] = 'a' and B[3] = 'a', is 'a' equal to 'a'? Yes. Increase. f[5][3] =f[5-1][3-1] + 1=f[4][2] + 1=2 +1 = 3.
45. j=4.
46. A[5] = 'a' and B[4] = 'a', is 'a' equal to 'a'? Yes. Increase. f[5][4] = f[5-1][4-1] +1 = f[4][3] + 1 = 2 + 1 = 3.
47. The length of the LCS is f[5][4]=3
```

Table 12: The prompt of longest common subsequence and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array A: $[2,3,2,9]$.
Set the length of the array $\mathrm{n}: 4$.
Set $\mathrm{i}=0$.
Step 1: What is the value of $i$ and $A[i]$ ? Print them.
Step 2: Set $\mathrm{j}=0$. Compute max $\mathrm{j}=\mathrm{n}-\mathrm{i}-1$.
Step 3: Compare $A[j]$ and $A[j+1]$. Are they in the correct order? Apply the following rule: $A[j]<=A[j+1]$ is the correct order, $A[j]>A[j+1]$ is the wrong order.
i. If $A[j]$ and $A[j+1]$ are in the correct order, continue.
ii. If $A[j]$ and $A[j+1]$ are in the wrong order, swap $A[j]$ and $A[j+1]$ to get the updated array $A$.

Step 4: Increment j by 1. If $\mathbf{j}$ < max_j, go back to Step 3. Otherwise, proceed to Step 5.
Step 5: Increment i by 1. If i<3, go back to Step 1. Otherwise, proceed to Step 6.
Step 6: Print the sorted array A.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $\mathrm{i}=0, \mathrm{~A}[0]=2$.
2. $j=0, \max j=4-0-1=3$.
3. $\mathrm{A}[0]=2, \mathrm{~A}[1]=3$, correct order.
4. $j=1, \max j=3$.
5. $A[1]=3, A[2]=2$, wrong order, swap $A[1]$ and $A[2], A=[2,2,3,9]$.
6. $j=2, \max j=3$.
7. $A[2]=3, A[3]=9$, correct order.
8. $i=1, A[1]=2$.
9. $\mathrm{j}=0, \max \mathrm{j}=4-1-1=2$.
10. $A[0]=2, A[1]=2$, correct order.
11. $\mathrm{j}=1, \max \mathrm{j}=2$.
12. $A[1]=2, A[2]=3$, correct order.
13. $i=2, A[2]=3$.
14. $j=0, \max _{\mathrm{j}} \mathrm{j}=4-2-1=1$.
15. $A[0]=2, A[1]=2$, correct order.
16. $i=3, A[3]=9$.
17. Sorted array $A=[2,2,3,9]$.

Table 13: The prompt of bubble sort and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the list of sortable items A: [7, 2, 9, 1] .
Set $\mathrm{N}=4$.
Define the function heapify $(\mathrm{A}, \mathrm{N}, \mathrm{i})$ to maintain the heap property.
Function heapify(A, N, i):

1. Set largest as i (root). Print N.
2. Calculate the left child index I: 2 * $i+1$.
3. Calculate the right child index r: 2 * $i+2$.
4. Check if the left child exists $(\mathrm{I}<\mathrm{N})$ and if its value $A[1]$ is greater than the root $A[l a r g e s t]$. If true, set largest as I .
5. Check if the right child exists ( $r<N$ ) and if its value $A[r]$ is greater than the root A[largest]. If true, set largest as
r.
6. If largest is not equal to $i$, perform the following steps:
a. Swap the values of $A[i]$ and $A[l a r g e s t]$.
b. Call the heapify function recursively with arguments ( $\mathrm{A}, \mathrm{N}$, largest).

End of function.

Step 1: Build a max heap from the input array A.
i. Iterate through the array from index 1 to 0 (inclusive) in reverse order.
ii. For each index $i$, call the heapify function with arguments ( $\mathrm{A}, \mathrm{N}, \mathrm{i}$ ).

Step 2: Sort the array using the max heap.
i. Iterate through the array from index 3 to 1 (inclusive) in reverse order.
ii. For each index i , perform the following steps:
a. Swap the first element of the array ( $\mathrm{A}[0]$ ) with the current element $(\mathrm{A}[\mathrm{i}])$.
b. Call the heapify function with arguments ( $\mathrm{A}, \mathrm{i}, 0$ ).

Step 3: Print the array A.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $i=1$, calling heapify $(A, 4,1)$.
2. In heapify $(A, 4,1): N=4$, largest $=1, l=3, r=4$.
3. $I<N, A[l]=1, A[$ largest $]=2$, largest remains 1 .
4. $r\rangle=N$, skip the check for the right child.
5. largest = 1, no need to swap or call heapify recursively.
6. $i=0$, calling heapify $(A, 4,0)$.
7. In heapify $(A, 4,0)$ : $N=4$, largest $=0, I=1, r=2$.
8. $I<N, A[l]=2, A[$ largest $]=7$, largest remains 0 .
9. $r<N, A[r]=9, A[$ largest $]=7$, largest is updated to 2 .
10. largest != 0 , swap $A[0]$ and $A[2], A$ becomes $[9,2,7,1]$.
11. Call heapify $(A, 4,2)$ recursively.
12. In heapify $(A, 4,2): N=4$, largest $=2, I=5, r=6$.
13. $I>=N$, skip the check for the left child.
14. $r>=N$, skip the check for the right child.
15. largest $=2$, no need to swap or call heapify recursively.
16. Max heap is built, $A=[9,2,7,1]$.
17. $i=3$, swap $A[0]$ and $A[3]$, A becomes [1, 2, 7, 9].
18. Call heapify $(A, 3,0)$.
19. In heapify $(A, 3,0)$ : $N=3$, largest $=0, I=1, r=2$.
20. $\mathrm{I}<\mathrm{N}, \mathrm{A}[\mathrm{I}]=2$, $\mathrm{A}[$ largest $]=1$, largest is updated to 1 .
21. $\mathrm{r}<\mathrm{N}, \mathrm{A}[r]=7, \mathrm{~A}[$ largest $]=2$, largest is updated to 2 .
22. largest $!=0, \operatorname{swap} A[0]$ and $A[2], A$ becomes $[7,2,1,9]$.
23. Call heapify $(A, 3,2)$ recursively.
24. In heapify $(A, 3,2)$ : $N=3$, largest $=2, I=5, r=6$.
25. $I>=N$, skip the check for the left child.
26. $r>=N$, skip the check for the right child.
27. largest $=2$, no need to swap or call heapify recursively.
28. $i=2$, swap $A[0]$ and $A[2], A$ becomes [1, 2, 7, 9].
29. Call heapify (A, 2, 0).
30. In heapify $(A, 2,0)$ : $N=2$, largest $=0, I=1, r=2$.
31. $\mathrm{I}<\mathrm{N}, \mathrm{A}[I]=2$, $\mathrm{A}[$ largest $]=1$, largest is updated to 1 .
32. $r>=N$, skip the check for the right child.
33. largest != 0 , swap $A[0]$ and $A[1], A$ becomes $[2,1,7,9]$.
34. Call heapify $(A, 2,1)$ recursively.
35. In heapify $(A, 2,1)$ : $N=2$, largest $=1, I=3, r=4$.
36. $I>=N$, skip the check for the left child.
37. $r>=N$, skip the check for the right child.
38. largest $=1$, no need to swap or call heapify recursively.
39. $i=1$, swap $A[0]$ and $A[1], A$ becomes $[1,2,7,9]$.
40. Call heapify $(A, 1,0)$.
41. In heapify $(A, 1,0)$ : $N=1$, largest $=0, I=1, r=2$.
42. $I>=N$, skip the check for the left child.
43. $r>=N$, skip the check for the right child.
44. largest $=0$, no need to swap or call heapify recursively.
45. The array $A$ is now sorted: $[1,2,7,9]$.

Table 14: The prompt of heapsort and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the list of sortable items A: $[2,8,8,7]$.
Set $\mathrm{N}=4$.
Create a function called "partition" that takes three arguments: array, low, and high.
Create a function called "quicksort" that takes three arguments: array, low, and high.
Step 1: Call the "quicksort" function with $\mathrm{A}, 0$, and $\mathrm{N}-1$ as arguments.
Inside the "quicksort" function, follow these steps:
Step 1.1: Check if low is less than high. If not, return.
Step 1.2: Call the "partition" function with array, low, and high as arguments, and store the result in a variable called "pi".
Step 1.3: Recursively call the "quicksort" function with array, low, and pi-1 as arguments.
Step 1.4: Recursively call the "quicksort" function with array, pi + 1, and high as arguments.
Inside the "partition" function, follow these steps:
Step 2.1: Set the pivot as the element at the "high" index of the array, which is A[high].
Step 2.2: Set a pointer "i" to low - 1 .
Step 2.3: Iterate through the array from the "low" index to the "high" index (exclusive) using a variable "j".
Step 2.4: Compare the element at index "j" $\mathrm{A}[\mathrm{j}]$ with the pivot. If it is less than or equal to the pivot, follow these steps:
a. Increment the pointer "i" by 1 .
b. Swap the elements at index "i" $\mathrm{A}[\mathrm{i}]$ and " $j$ " $\mathrm{A}[\mathrm{j}]$ in the array.

Step 2.5: After the iteration, swap the pivot element $A[h i g h]$ with the element at index $" i+1$ " $A[i+1]$ in the array.
Step 2.6: Return the value of " $i+1$ " as the partition position.
Step 3: Print the array A.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Call quicksort(A, 0,3 ).
2. Inside quicksort, low (0) is less than high (3), so continue.
3. Call partition (A, 0,3 ) and store the result in pi.
4. Inside partition, set pivot $=A[3]=7$, set $i=-1$.
5. Iterate through $A$ from low (0) to high (3) exclusive with $j$ :
a. $j=0, A[j]=2<=\operatorname{pivot}(7)$, increment $i(i=0)$, swap $A[i]$ and $A[j]$ (no change).
b. $j=1, A[j]=8>$ pivot (7), do nothing.
c. $j=2, A[j]=8>$ pivot (7), do nothing.
6. After iteration, swap $A[i+1]$ and $A[h i g h]$, i.e., $A[1]$ and $A[3]$, resulting in $A=[2,7,8,8]$.
7. Return $i+1=1$ as the partition position (pi).
8. Recursively call quicksort(A, $0, \mathrm{pi}-1$ ) which is quicksort(A, 0,0 ).
9. Inside the recursive quicksort, low (0) is not less than high ( 0 ), so return.
10. Recursively call quicksort(A, pi $+1,3$ ) which is quicksort(A, 2,3 ).
11. Inside the recursive quicksort, low (2) is less than high (3), so continue.
12. Call partition $(\mathrm{A}, 2,3)$ and store the result in pi.
13. Inside partition, set pivot $=A[3]=8$, set $i=1$.
14. Iterate through $A$ from low (2) to high (3) exclusive with $j$ :
a. $j=2, A[j]=8<=\operatorname{pivot}(8)$, increment $i(i=2)$, swap $A[i]$ and $A[j]$ (no change).
15. After iteration, swap $A[i+1]$ and $A[h i g h]$, i.e., $A[3]$ and $A[3]$ (no change).
16. Return $\mathrm{i}+1=3$ as the partition position (pi).
17. Recursively call quicksort(A, 2 , pi-1) which is quicksort(A, 2,2 ).
18. Inside the recursive quicksort, low (2) is not less than high (2), so return.
19. Recursively call quicksort(A, pi $+1,3$ ) which is quicksort(A, 4, 3).
20. Inside the recursive quicksort, low (4) is not less than high (3), so return.
21. Print the array A: $[2,7,8,8]$.

Table 15: The prompt of quicksort and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array A: $[7,2,6,0,3,7,9,5,6]$.
Set the length of the array n : 9 .
Set $\min =0$.
Set $\mathrm{i}=1$.
Step 1: What are the values of A[min_] and A[i]? Print them.
Step 2: Compare $A\left[m i n \_\right]$and $A[i]$. Is $A[\min ]$ greater than $A[i]$ ?
i. If yes, update min_ as the current value of $i$.
ii. If no, continue without updating min_.

Step 3: Increment i by 1. If i < 9, go back to Step 1. Otherwise, proceed to Step 4.
Step 4: What is the value of min_? Print it.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. min_ $=0, A[0]=7 ; i=1, A[1]=2$.
2. Since $A[\min ]>A[i]$, update $\min _{-}=1$.
3. Increment $i$ to $2, \mathrm{~A}[2]=6$.
4. $A[\min ]=2, A[i]=6$. $A[m i n]$ is not greater than $A[i]$, so do not update min_.
5. Increment ito $3, A[3]=0$.
6. $A\left[\min \_\right]=2, A[i]=0$. Since $A[\min ]>A[i]$, update $\min -=3$.
7. Increment ito 4, A[4] = 3 .
8. $A[\min ]=0, A[i]=3$. $A\left[m i n \_\right]$is not greater than $A[i]$, so do not update min_.
9. Increment ito $5, A[5]=7$.
10. $A[\min ]=0, A[i]=7$. $A[\min ]$ is not greater than $A[i]$, so do not update min_.
11. Increment $i$ to $6, A[6]=9$.
12. $A[\min ]=0, A[i]=9$. $A[\min ]$ is not greater than $A[i]$, so do not update min_.
13. Increment i to 7, A[7] = 5 .
14. $A[\min ]=0, A[i]=5$. $A[\min ]$ is not greater than $A[i]$, so do not update min_.
15. Increment $i$ to $8, A[8]=6$.
16. $A[\min ]=0, A[i]=6$. $A\left[\mathrm{~min}_{]}\right]$is not greater than $A[i]$, so do not update min_.
17. $i=9$, which is equal to $n$, so proceed to Step 4.
18. The value of $\mathrm{min}_{\mathrm{n}}$ is 3 .

Table 16: The prompt of minimum and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the list of sortable items A: $[2,8,5,7]$.
Set $\mathrm{n}=4$.
Set $\mathrm{i}=0$.
Step 1: What is the value of $i$ and $A[i]$ ? Print them.
Step 2: Set key $=A[i]$ and $j=i-1$.
Step 3: Is $\mathrm{j}>=0$ and $\mathrm{A}[\mathrm{j}]>$ key? If yes, proceed to Step 4. If no, go to Step 6.
Step 4: Swap A[j+1] with A[j]. Print the updated A.
Step 5: Decrement j by 1. Go back to Step 3.
Step 6: Increment i by 1. If $\mathbf{i}$ 4, go back to Step 1. Otherwise, proceed to Step 7.
Step 7: What is the final sorted array A? Print it.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $i=0, A[0]=2$.
2. key $=2, j=-1$. ( j is not $>=0$, so go to Step 6)
3. $i=1, A[1]=8$.
4. key $=8, j=0 .(A[j]=2$, which is not > key, so go to Step 6)
5. $i=2, A[2]=5$.
6. key $=5, j=1$. $(A[j]=8$, which is $>$ key, so proceed to Step 4)
7. Swap $A[1]$ and $A[2]$. Updated A: [2, $5,8,7]$.
8. $j=0$. $(A[j]=2$, which is not $>$ key, so go to Step 6)
9. $i=3, A[3]=7$.
10. key $=7, j=2 .(A[j]=8$, which is $>$ key, so proceed to Step 4)
11. Swap $A[2]$ and $A[3]$. Updated $A:[2,5,7,8]$.
12. $j=1$. $(A[j]=5$, which is not $>$ key, so go to Step 6)
13. $i=4$. ( $i$ is not $<4$, so proceed to Step 7 )
14. The final sorted array $A$ is $[2,5,7,8]$.

Table 17: The prompt of insertion sort and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array A: $[9,5,0,3]$.
Set left index L: 0 , right index R: 3 , and the position $k$ : 3 .
Set $\mathrm{i}=\mathrm{L}$.
Define the partition function, with the parameter $A, L$, and $R$.
i. Set the pivot element $X$ as $A[R]$.
ii. Set the index $i$ as $L$.
iii. Iterate through the array from index $L$ to $R-1$ with index $j$.
a. Recall the value of $A[j]$ and $X$. Is $A[j]$ less than or equal to $X$ ? If yes, swap $A[i]$ and $A[j]$, print $A$, and increment i by 1 .
iv. Swap $A[i]$ and $A[R]$, print $A$.
v. Return the index $i$.

End of the partition function.
Define the kthSmallest function, with the parameter $A, K, L$, and $R$.
i. Call the partition function with arguments $A, L$, and $R$, and store the returned index in a variable called "index".
ii. Compute len_left $=$ index $-L+1$. Are len_left and $K$ the same?
a. If yes, return A[index].
b. If no, proceed to iii.
iii. Recall the value of len_left and $K$. Is len_left greater than $K$ ?
a. If yes, recursively call the $k$ thSmallest $(A, L=L, R=$ index $-1, K=K)$.
b. If no, recursively call the $k$ thSmallest $(A, L=$ index $+1, R=R, K=K$ - len_left).

End of the kthSmallest function.
Step 1: Call kthSmallest $(A, L=L, R=R, K=K)$, and print the returned value.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Call kthSmallest $(A, L=0, R=3, K=3)$.
2. Call partition $(A, L=0, R=3)$.
3. Set pivot element $X=A[3]=3$.
4. Set index $i=0$.
5. Iterate through the array from index 0 to 2 with index $j$.
a. $j=0, A[0]=9, X=3, A[0]$ is not less than or equal to $X$, no swap.
b. $j=1, A[1]=5, X=3, A[1]$ is not less than or equal to $X$, no swap.
c. $j=2, A[2]=0, X=3, A[2]$ is less than or equal to $X$, $\operatorname{swap} A[0]$ and $A[2], A=[0,5,9,3]$, increment $i$ to 1 .
6. Swap $A[1]$ and $A[3], A=[0,3,9,5]$, return index $i=1$.
7. len_left = $1-0+1=2$, len_left is not equal to $K$, proceed to step 8 .
8. len_left $=2$ is less than $K=3$, call kthSmallest $(A, L=1+1, R=3, K=3-2)$.
9. Call partition $(A, L=2, R=3)$.
10. Set pivot element $X=A[3]=5$.
11. Set index $i=2$.
12. Iterate through the array from index 2 to 2 with index $j$.
a. $j=2, A[2]=9, X=5, A[2]$ is not less than or equal to $X$, no swap.
13. Swap $A[2]$ and $A[3], A=[0,3,5,9]$, return index $i=2$.
14. len_left $=2-2+1=1$, len_left is equal to $K$, return $A[2]=5$.

The returned value is 5 .
Table 18: The prompt of quick select and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array A: A[0] = 8, $\mathrm{A}[1]=-3, \mathrm{~A}[2]=6, \mathrm{~A}[3]=3$.
Define the function maxSubArraySum with input parameters $A, l$ and $r$, where arr is an integer array, l is its left index and $r$ is its right index.
a: Check if the length of $A, r-I+1$, is equal to 1 (base case).
a.i. If yes, return the only element in arr.
a.ii. If no, proceed to (b).
b: Calculate the midpoint $\mathrm{m}=\mathrm{I}+(\mathrm{r}-\mathrm{I}) / / 2$.
c: Recursively call maxSubArraySum $(A, I, m)$ and store the result in left_max.
d: Recursively call maxSubArraySum (A, $m+1, r$ ) and store the result in right_max.
e: Initialize left_sum and right_sum to -100. Initialize sum to 0 . Initialize ito $\mathrm{m}+1$.
f: Is $i<=r$ ?
f.i. If $i<=r$, add $A[i]$ to sum. Update right_sum with max(right_sum, sum). Increment i by 1 . Go back to ( $f$ ).
f.ii. If $i>r$, proceed to (g).
g : Reset sum to 0 . Compute $\mathrm{m}-1$ and initialize i to m .
h: Is $\mathrm{i}>=1$ ?
f.i. If i$\rangle=\mathrm{I}$, add $\mathrm{A}[\mathrm{i}]$ to sum. Update left_sum with $\max (l$ left_sum, sum). Decrement i by 1 . Go back to (h).
f.ii. If $i$ < I, proceed to (i).
i: Calculate cross_max as the sum of left_sum and right_sum.
j : What is max(cross_max, left_max, right_max)? Return the value.
End of function maxSubArraySum.
Step 1: Call the maxSubArraySum function with arguments $A, 0$, and 3 , and print the result.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.): 1. maxSubArraySum (A, $l=0, r=3$ ).
1.1. $r-I+1=3-0+1=4,4!=1$.
1.2. $m=0+(3-0) / / 2=1$.
1.3. left_max $=$ maxSubArraySum( $A, l=0, r=1$ ).
1.3.1. $r-I+1=1-0+1=2,2!=1$.
1.3.2. $m=0+(1-0) / / 2=0$.
1.3.3. left_max $=$ maxSubArraySum $(A, l=0, r=0)$.
1.3.3.1. $r-I+1=0-0+1=1,1==1$, return $A[0]=8$.
1.3.4. right_max $=\operatorname{maxSubArraySum}(A, l=1, r=1)$.
1.3.4.1. $r-I+1=1-1+1=1,1==1$, return $A[1]=-3$.
1.3.5. left_sum $=-100$, right_sum $=-100$, sum $=0, i=1$.
1.3.6. $i<=r$, sum $+=A[1]=-3$, right_sum $=\max (-100,-3)=-3, i=2$.
1.3.7. $i>r$, sum $=0, i=0$.
1.3.8. $i>=I$, sum $+=A[0]=8$, left_sum $=\max (-100,8)=8, i=-1$.
1.3.9. $i<I$, cross_max $=$ left_sum + right_sum $=8+(-3)=5$.
1.3.10. $\max (5,8,-3)=8$, left_max $=8$.
1.4. right_max $=\operatorname{maxSubArraySum}(A, l=2, r=3)$.
1.4.1. $r-I+1=3-2+1=2,2!=1$.
1.4.2. $m=2+(3-2) / / 2=2$.
1.4.3. left_max $=\operatorname{maxSubArraySum}(A, l=2, r=2)$.
1.4.3.1. $r-I+1=2-2+1=1,1==1$, return $A[2]=6$.
1.4.4. right_max $=\operatorname{maxSubArraySum}(A, l=3, r=3$ ).
1.4.4.1. $r-I+1=3-3+1=1,1==1$, return $A[3]=3$.
1.4.5. left_sum $=-100$, right_sum $=-100$, sum $=0, i=3$.
1.4.6. $i<=r$, sum $+=A[3]=3$, right_sum $=\max (-100,3)=3, i=4$.
1.4.7. $i>r$, sum $=0, i=2$.
1.4.8. $i>=I$, sum $+=A[2]=6$, left_sum $=\max (-100,6)=6, i=1$.
1.4.9. $\mathrm{i}<\mathrm{I}$, cross_max $=$ left_sum + right_sum $=6+3=9$.
1.4.10. $\max (9,6,3)=9$, right_max $=9$.
1.5. left_sum $=-100$, right_sum $=-100$, sum $=0, i=2$.
1.6. $i<=r$, sum $+=A[2]=6$, right_sum $=\max (-100,6)=6, i=3$.
1.7. $i<=r$, sum $+=A[3]=9$, right_sum $=\max (6,9)=9, i=4$.
1.8. $i>r$, sum $=0, i=1$.
1.9. $i>=1$, sum $+=A[1]=-3$, left_sum $=\max (-100,-3)=-3, i=0$.
1.10. $i>=I$, sum $+=A[0]=5$, left_sum $=\max (-3,5)=5, i=-1$.
1.11. i < I , cross_max $=$ left_sum + right_sum $=5+9=14$.
1.12. $\max (14,8,9)=14$.

The result of maxSubArraySum $(\mathrm{A}, 0,3)$ is 14 .
Table 19: The prompt of maximum subarray and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the square matrix $A$ of size $6 \times 6$ :
$A[0,0]=0, A[0,1]=1, A[0,2]=0, A[0,3]=1, A[0,4]=0, A[0,5]=0$
$A[1,0]=0, A[1,1]=0, A[1,2]=0, A[1,3]=0, A[1,4]=1, A[1,5]=0$
$A[2,0]=0, A[2,1]=0, A[2,2]=0, A[2,3]=0, A[2,4]=1, A[2,5]=1$
$A[3,0]=0, A[3,1]=1, A[3,2]=0, A[3,3]=0, A[3,4]=0, A[3,5]=0$
$A[4,0]=0, A[4,1]=0, A[4,2]=0, A[4,3]=1, A[4,4]=0, A[4,5]=0$
$A[5,0]=0, A[5,1]=0, A[5,2]=0, A[5,3]=0, A[5,4]=0, A[5,5]=1$.
Set color: color[0] = 0, color[1] $=0$, color[2] $=0, \operatorname{color}[3]=0, \operatorname{color}[4]=0, \operatorname{color}[5]=0$.
Set d: $\mathrm{d}[0]=0, \mathrm{~d}[1]=0, d[2]=0, d[3]=0, d[4]=0, d[5]=0$.
Set pi: pi[0] $=0$, pi[1] $=1$, pi[2] $=2$, pi[3] $=3$, pi[4] $=4$, pi[5] $=5$.
Set s_prev: s_prev[0] = 0, s_prev[1] = 1, s_prev[2] = 2, s_prev[3] = 3, s_prev[4] = 4, s_prev[5] = 5 .
Set time: 0 .
Set s: 0 .
Step 1: Is $s<6$ ? If $s$ is equal to 6 , go to Step 6. Otherwise:
i. If color $[s]==0$, set $s$ _last $=s, u=s$, and $v=s$, go to Step 2.
ii. If color $[\mathrm{s}]!=0$, increment $s$ by 1 , and go to Step 1 .

Step 2: Check if color $[u]==0$ or $\mathrm{d}[\mathrm{u}]==0$.
i. If true, increment time by 1 , set $d[u]=$ time, and set color $[u]=1$.

Step 3: Iterate through each element v in range( N ).
i. If $\mathrm{A}[\mathrm{u}, \mathrm{v}]!=0$, check if color $[\mathrm{v}]==0$.
a. If true, set pi $[v]=u$, color $[v]=1, s \_p r e v[v]=s \_$last, and s_last $=v$. Then, break the iteration and go to Step 4 .
b. If false, continue.
ii. If $A[u, v]==0$, continue

Step 4: What are the values of s_last and $u$ ? Is s_last equal to $u$ ?
i. If true, set color[u] = 2 and increment time by 1 . Then, What is the value of s_prev[u]? Is s_prev[u] equal to $u$ ?
a. If true, assert s_prev[s_last] == s_last, increment s by 1 and go to step 1 .
b. If false, set pr = s_prev[s_last], s_prev[s_last] = s_last, and s_last = pr.
ii. If false, proceed to Step 5 .

Step 5: Set $\mathrm{u}=$ s_last and go to Step 2.
Step 6: Print the array pi.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $S=0,0<6$.
2. color $[0]==0$, set s_last $=0, u=0$, and $v=0$.
3. Increment time by 1 , time $=1$, set $d[0]=1$, and set color $[0]=1$.
4. Iterate through each element $v$ in range(6):
$-\mathrm{v}=0, \mathrm{~A}[0,0]=0$, continue.
$-v=1, A[0,1]=1$, color $[1]=0$, set pi[1] $=0$, color $[1]=1$, s_prev[1] $=0$, s_last $=1$, break the iteration.
5. s_last $=1, u=0$, s_last $!=u$, proceed to Step 5 .
6. Set $u=1$ and go to Step 2 .
7. color[1] == $1, d[1]==0$, increment time by 1 , time $=2$, set $d[1]=2$, and set color[ 1$]=1$.
8. Iterate through each element $v$ in range(6):
$-v=0, A[1,0]=0$, continue.
$-v=1, A[1,1]=0$, continue.
$-v=2, A[1,2]=0$, continue.
$-v=3, A[1,3]=0$, continue.
$-v=4, A[1,4]=1, \operatorname{color}[4]=0$, set pi $[4]=1$, color $[4]=1$, s_prev[4] $=1$, s_last $=4$, break the iteration.
9. $s \_$last $=4, u=1$, s_last ! $=u$, proceed to Step 5 .
10. Set $u=4$ and go to Step 2 .
11. $\operatorname{color}[4]==1, d[4]==0$, increment time by 1 , time $=3$, set $d[4]=3$, and set color $[4]=1$.
12. Iterate through each element v in range(6):
$-v=0, A[4,0]=0$, continue.
$-v=1, A[4,1]=0$, continue.
$-\mathrm{v}=2, \mathrm{~A}[4,2]=0$, continue.
$-\mathrm{v}=3, \mathrm{~A}[4,3]=1$, color $[3]=0$, set $\mathrm{pi}[3]=4$, color $[3]=1$, s_prev[3] $=4$, s_last $=3$, break the iteration.
13. s_last $=3, u=4$, s_last ! $=u$, proceed to Step 5 .
14. Set $u=3$ and go to Step 2 .
15. $\operatorname{color}[3]==1, \mathrm{~d}[3]==0$, increment time by 1 , time $=4$, set $\mathrm{d}[3]=4$, and set color $[3]=1$.
16. Iterate through each element $v$ in range(6):
$-v=0, A[3,0]=0$, continue.
$-v=1, A[3,1]=1$, color $[1]=1$, continue.
$-v=2, A[3,2]=0$, continue.
$-v=3, A[3,3]=0$, continue.
$-v=4, A[3,4]=0$, continue.
$-v=5, A[3,5]=0$, continue.
17. s_last $=3, u=3$, s_last $==u$, set color[ 3$]=2$, increment time by 1 , time $=5$, s_prev[3] !=3, set pr $=s \_$prev[3] $=4$, s_prev $[3]=3$, s_last $=4$.
18. Set $u=4$ and go to Step 2 .
19. color $[4]==1, d[4]==3$, continue.
20. Iterate through each element $v$ in range(6):
$-\mathrm{v}=0, \mathrm{~A}[4,0]=0$, continue.
$-v=1, A[4,1]=0$, continue.
$-v=2, A[4,2]=0$, continue.
$-v=3, A[4,3]=1$, color $[3]=2$, continue.
$-v=4, A[4,4]=0$, continue.
$-v=5, A[4,5]=0$, continue.
21. s_last $=4, u=4$, s_last $==u$, set color[4] $=2$, increment time by 1 , time $=6$, s_prev[4] ! $=4$, set pr $=$ s_prev[4] $=1, s \_$prev $[4]=4$, s_last $=1$.
22. Set $u=1$ and go to Step 2 .
23. $\operatorname{color}[1]==1, \mathrm{~d}[1]==2$, continue .
24. Iterate through each element $v$ in range(6):
$-v=0, A[1,0]=0$, continue.
$-v=1, A[1,1]=0$, continue.
$-v=2, A[1,2]=0$, continue.
$-v=3, A[1,3]=0$, continue.
$-v=4, A[1,4]=1$, color $[4]=2$, continue.
$-v=5, A[1,5]=0$, continue.
25. s_last $=1, u=1$, s_last $==u$, set color[1] = 2 , increment time by 1 , time $=7$, s_prev[1] == 1, assert s_prev[s_last] $==s$ last, increment $s$ by $1, s=1$.
26. $s=1,1<6$.
27. color $[1]==2$, increment $s$ by $1, s=2$.
28. $s=2,2<6$.
29. color[2] $==0$, set s_last $=2, u=2$, and $v=2$.
30. Increment time by 1 , time $=8$, set $d[2]=8$, and set color[2] $=1$.
31. Iterate through each element $v$ in range(6):
$-\mathrm{v}=0, \mathrm{~A}[2,0]=0$, continue.
$-v=1, A[2,1]=0$, continue.
$-v=2, A[2,2]=0$, continue.
$-\mathrm{v}=3, \mathrm{~A}[2,3]=0$, continue.
$-\mathrm{V}=4, \mathrm{~A}[2,4]=1$, color $[4]=2$, continue.
$-v=5, A[2,5]=1$, color[5] $=0$, set pi $[5]=2$, color[5] $=1$, s_prev[5] $=2$, s_last $=5$, break the iteration.
32. s_last $=5, u=2$, s_last ! $=u$, proceed to Step 5 .
33. Set $u=5$ and go to Step 2 .
34. color[5] $==1, d[5]==0$, increment time by 1 , time $=9$, set $d[5]=9$, and set color[5] $=1$.
35. Iterate through each element $v$ in range(6):

$$
\begin{aligned}
& -v=0, A[5,0]=0, \text { continue } . \\
& -v=1, A[5,1]=0, \text { continue } . \\
& -v=2, A[5,2]=0, \text { continue. } \\
& -v=3, A[5,3]=0, \text { continue. } \\
& -v=4, A[5,4]=0, \text { continue. } \\
& -v=5, A[5,5]=1, \text { color }[5]=1, \text { continue. }
\end{aligned}
$$

36. s_last $=5, u=5$, s_last $==u$, set color[5] $=2$, increment time by 1 , time $=10$, s_prev[5] $==5$, assert s_prev[s_last] == s_last, increment s by $1, \mathrm{~s}=3$.
37. $s=3,3<6$.
38. color $[3]==2$, increment $s$ by $1, s=4$.
39. $s=4,4<6$.
40. color[4] $==2$, increment $s$ by $1, s=5$.
41. $s=5,5<6$.
42. color[5] $==2$, increment $s$ by $1, s=6$.
43. $s=6$, go to Step 6 .
44. Print the array pi: $[0,0,2,4,1,2]$.

Table 20: The prompt of depth first search and the response of gpt-4.

## Prompt

Execute the following instructions.
Initial: Set the array $p$ of length $N-1=3: p[0]=0.19, p[1]=0.04, p[2]=0.11$ and $q$ of length $N=4: q[0]=0.24$, $\mathrm{q}[1]=0.20, \mathrm{q}[2]=0.11, \mathrm{q}[3]=0.10$ respectively.
Set the matrix e and wof size $4 \times 4$ with all elements initialized to 0 .
Set maxint: 66666666.
Step 1: Initialize e and w diagonals:
i. For $i$ in range 0 to 3 (inclusive), do the following:
a. Set e[i, $]=q[i]$.
b. Set $w[i, i]=q[i]$.

Step 2: Set L: 1.
Step 3: Is $L<4$ ? If $L$ is equal to or greater than 4, go to Step 6. Otherwise:
i. Set upper_i: 4 - L.
ii. Set i: 0 .
iii. Go to Step 4.

Step 4: Is i < upper_i? If i is equal to or greater than upper_ i , increment L by 1 and go to Step 3. Otherwise:
i. Set $j$ : $i+L$.
ii. Set e[i, j] = maxint.
iii. Set $w[i, j]=w[i, j-1]+p[j-1]+q[j]$.
$i v$. Set $r$ : $i$.
v. Go to Step 5.

Step 5: Is $r$ < $j$ ? If $r$ is equal to or greater than $j$, increment $i$ by 1 and go to Step 4. Otherwise:
$i$. What is the value of $i$ ? Recall and print it, then calculate $t=e[i, r]+e[r+1, j]+w[i, j]$.
ii. Set e[i, j] = min(e[i, j], t).
iii. Increment $r$ by 1 .
iv. Go to Step 5.

Step 6: Print the value of e[0, N-1].
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $i=0,0<=3, e[0][0]=q[0]=0.24, w[0][0]=q[0]=0.24$.
2. $\mathrm{i}=1,1<=3, \mathrm{e}[1][1]=\mathrm{q}[1]=0.20, \mathrm{w}[1][1]=\mathrm{q}[1]=0.20$.
3. $i=2,2<=3, e[2][2]=q[2]=0.11, w[2][2]=q[2]=0.11$.
4. $\mathrm{i}=3,3<=3, \mathrm{e}[3][3]=\mathrm{q}[3]=0.10, \mathrm{w}[3][3]=\mathrm{q}[3]=0.10$.
5. $L=1, L<4$, upper_ $i=4-1=3, i=0$.
6. $i=0,0<3, j=0+1=1$, $e[0][1]=$ maxint $=66666666, w[0][1]=w[0][0]+p[0]+q[1]=0.24+0.19+0.20=$ 0.63 .
7. $r=0, r<1, i=0, t=e[0][0]+e[1][1]+w[0][1]=0.24+0.20+0.63=1.07, e[0][1]=\min (66666666,1.07)=$ 1.07.
8. $r=1, r>=1, i=1, i<3$.
9. $i=1,1<3, j=1+1=2, e[1][2]=$ maxint $=66666666, w[1][2]=w[1][1]+p[1]+q[2]=0.20+0.04+0.11=$ 0.35 .
10. $r=1, r<2, i=1, t=e[1][1]+e[2][2]+w[1][2]=0.20+0.11+0.35=0.66, e[1][2]=\min (66666666,0.66)=$ 0.66 .
11. $r=2, r>=2, i=2, i<3$.
12. $i=2,2<3, j=2+1=3, e[2][3]=$ maxint $=66666666, w[2][3]=w[2][2]+p[2]+q[3]=0.11+0.11+0.10=$ 0.32 .
13. $r=2, r<3, i=2, t=e[2][2]+e[3][3]+w[2][3]=0.11+0.10+0.32=0.53, e[2][3]=\min (66666666,0.53)=$ 0.53 .
14. $r=3, r>=3, i=3, i\rangle=3, L=2, L\langle 4$, upper_ $i=4-2=2, i=0$.
15. $i=0,0<2, j=0+2=2, e[0][2]=$ maxint $=66666666, w[0][2]=w[0][1]+p[1]+q[2]=0.63+0.04+0.11=$ 0.78 .
16. $\mathrm{r}=0, \mathrm{r}<2, \mathrm{i}=0, \mathrm{t}=\mathrm{e}[0][0]+\mathrm{e}[1][2]+\mathrm{w}[0][2]=0.24+0.66+0.78=1.68, \mathrm{e}[0][2]=\min (66666666,1.68)=$ 1.68.
17. $r=1, r<2, i=0, t=e[0][1]+e[2][2]+w[0][2]=1.07+0.11+0.78=1.96, e[0][2]=\min (1.68,1.96)=1.68$. 18. $r=2, r\rangle=2, i=1, i<2$.
```
19. \(\mathrm{i}=1,1<2, \mathrm{j}=1+2=3, \mathrm{e}[1][3]=\) maxint \(=66666666, \mathrm{w}[1][3]=\mathrm{w}[1][2]+\mathrm{p}[2]+\mathrm{q}[3]=0.35+0.11+0.10=\)
0.56 .
20. \(r=1, r<3, i=1, t=e[1][1]+e[2][3]+w[1][3]=0.20+0.53+0.56=1.29, e[1][3]=\min (66666666,1.29)=\)
1.29
21. \(r=2, r<3, i=1, t=e[1][2]+e[3][3]+w[1][3]=0.66+0.10+0.56=1.32, e[1][3]=\min (1.29,1.32)=1.29\).
22. \(r=3, r\rangle=3, i=2, i\rangle=2, L=3, L\langle 4\), upper_ \(i=4-3=1, i=0\).
23. \(\mathrm{i}=0,0<1, \mathrm{j}=0+3=3, \mathrm{e}[0][3]=\) maxint \(=66666666, \mathrm{w}[0][3]=\mathrm{w}[0][2]+\mathrm{p}[2]+\mathrm{q}[3]=0.78+0.11+0.10=\)
0.99 .
24. \(r=0, r<3, i=0, t=e[0][0]+e[1][3]+w[0][3]=0.24+1.29+0.99=2.52, e[0][3]=\min (66666666,2.52)=\)
2.52
25. \(r=1, r<3, i=0, t=e[0][1]+e[2][3]+w[0][3]=1.07+0.53+0.99=2.59, e[0][3]=\min (2.52,2.59)=2.52\).
26. \(r=2, r<3, i=0, t=e[0][2]+e[3][3]+w[0][3]=1.68+0.10+0.99=2.77, e[0][3]=\min (2.52,2.77)=2.52\).
27. \(r=3, r\rangle=3, i=1, i\rangle=1, L=4, L\rangle=4\).
28. Print \(\mathrm{e}[0][3]=2.52\).
```

Table 21: The prompt of optimal binary search tree and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the adjacency matrix $\mathrm{A}: \mathrm{A}[0,0]=0, \mathrm{~A}[0,1]=0, \mathrm{~A}[0,2]=1, \mathrm{~A}[0,3]=1$
$A[1,0]=0, A[1,1]=0, A[1,2]=1, A[1,3]=1$
$A[2,0]=1, A[2,1]=1, A[2,2]=0, A[2,3]=1$
$A[3,0]=1, A[3,1]=0, A[3,2]=1, A[3,3]=0$.
Set the number of nodes $\mathrm{N}: 4$.
Initialize the following arrays:

- color: [1, 0, 0, 0].
- d: [0, 6666, 6666, 6666].

Set the source node: source $=0$.
Step 1: Create an empty queue $Q$ and add the source node to it.
Step 2: Check if the queue $Q$ is empty. If it is empty, proceed to Step 7. Otherwise, continue to Step 3.
Step 3: Remove the first element from the queue and assign it to the variable $u$.
Step 4: Set $\mathrm{i}=0$.
Step 5: If $\mathrm{i}>=4$, go to Step 6; otherwise:
i. Check if $\mathrm{A}[\mathrm{u}, \mathrm{i}]!=0$. If $\mathrm{A}[\mathrm{u}, \mathrm{i}]==0$, increment i by 1 and go to Step 5 .
ii. If color $[i]==0$, update the following values:

- $\operatorname{color}[i]=1$
$-d[i]=d[u]+1$
- pi[i] = u
- Append node ito the queue Q .
iii. Increment i by 1 and go to Step 5 .

Step 6: Update color[u] = 2 and go back to Step 2.
Step 7: When the queue $Q$ is empty, return the list d containing the shortest path distances from the source node to all other nodes.

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $Q=[0]$
2. $Q$ is not empty, proceed to step 3 .
3. $u=0, Q=[]$
4. $i=0$
5. i < 4, check A[u, i]:
i. $A[0,0]==0$, increment ito 1 .
ii. $A[0,1]==0$, increment i to 2 .
iii. $A[0,2]!=0$, color[2] $==0$, update values:

- color[2] = 1
$-\mathrm{d}[2]=\mathrm{d}[0]+1=1$
- pi[2] = 0
- $\mathrm{Q}=[2]$
iv. Increment ito 3.

```
v. \(A[0,3]!=0\), color \([3]==0\), update values:
    - color[3] = 1
    \(-\mathrm{d}[3]=\mathrm{d}[0]+1=1\)
    - pi[3] = 0
    \(-\mathrm{Q}=[2,3]\)
6. color \([0]=2\)
2. \(Q\) is not empty, proceed to step 3 .
3. \(u=2, Q=[3]\)
4. \(i=0\)
5. i < 4, check A[u, i]:
    i. \(A[2,0]!=0\), color \([0]==2\), increment \(i\) to 1 .
    ii. \(\mathrm{A}[2,1]!=0\), color \([1]==0\), update values:
        - color[1] = 1
        \(-\mathrm{d}[1]=\mathrm{d}[2]+1=2\)
        - pi[1] = 2
        - \(\mathrm{Q}=[3,1]\)
    iii. Increment ito 2.
    iv. \(A[2,2]==0\), increment i to 3 .
    v. \(A[2,3]!=0\), color[3] \(==1\), increment \(i\) to 4 .
6. color[2] = 2
2. \(Q\) is not empty, proceed to step 3 .
3. \(u=3, Q=[1]\)
4. \(i=0\)
5. i < 4, check A[u, i]:
    i. \(A[3,0]!=0\), color \([0]==2\), increment \(i\) to 1 .
    ii. \(A[3,1]==0\), increment \(i\) to 2 .
    iii. \(A[3,2]!=0\), color[2] \(==2\), increment i to 3 .
    iv. \(A[3,3]==0\), increment \(i\) to 4 .
6. color \([3]=2\)
2. \(Q\) is not empty, proceed to step 3 .
3. \(u=1, Q=[]\)
4. \(i=0\)
5. i < 4, check \(A[u, i]:\)
    i. \(A[1,0]==0\), increment \(i\) to 1 .
    ii. \(A[1,1]==0\), increment \(i\) to 2 .
    iii. \(A[1,2]!=0\), color[2] \(==2\), increment i to 3 .
    iv. \(A[1,3]!=0\), color \([3]==2\), increment i to 4 .
6. \(\operatorname{color}[1]=2\)
2. \(Q\) is empty, proceed to step 7 .
7. Return the list \(\mathrm{d}:[0,2,1,1]\)
```

Table 22: The prompt of breadth first search and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When updating an array, use concrete values rather than variables.
Initial: Set the square matrix $A$ of size $4 \times 4$ :
$A[0,0]=0, A[0,1]=0, A[0,2]=0, A[0,3]=1$
$A[1,0]=1, A[1,1]=0, A[1,2]=0, A[1,3]=0$
$A[2,0]=0, A[2,1]=0, A[2,2]=0, A[2,3]=0$
$A[3,0]=1, A[3,1]=0, A[3,2]=1, A[3,3]=0$.
Set color: color $[0]=0$, color $[1]=0$, color $[2]=0, \operatorname{color}[3]=0$.
Set topo: topo[0] $=0$, topo[1] $=1$, topo[2] $=2$, topo[3] $=3$.
Set s_prev: $s \_p r e v[0]=0, s \_p r e v[1]=1, s \_p r e v[2]=2, ~ s \_p r e v[3]=3$.
Set topo_head: 0.
Set s: 0 .
Step 1: Is $s$ < 4? If $s$ is equal to 4 , go to Step 8. Otherwise:
i. If color $[s]==0$, set s_last $=s, u=s$, go to Step 2 .
ii. If color $[s]!=0$, increment $s$ by 1 , and go to Step 1 .

Step 2: What is the value of color[u]? Print it. Check if color $[u]==0$.
i. If color $[u]==0$, set color $[u]=1$.
ii. If color[u] != 0 , go to Step 3 .

Step 3: Iterate through each element $v$ in range $(N)$. After the iteration of $v$, go to Step 4.
i. If $A[u, v]!=0$, check if color $[v]==0$.
a. If color $[\mathrm{v}]==0$, set color $[\mathrm{v}]=1, \mathrm{~s} \_$prev $[\mathrm{v}]=\mathrm{s} \_$last, and $\mathrm{s} \_$last $=\mathrm{v}$. Then, break the iteration and go to Step 4.
b. If color $[v]!=0$, continue the iteration of $v$.
ii. If $A[u, v]==0$, continue the iteration of $v$.

Step 4: What are the values of s_last and u? Print them. Is s_last equal to $u$ ?
i. If $s$ _last $==u$, set color[u] $=2$ and go to Step 5 .
ii. If s_last != u, proceed to Step 7 .

Step 5: What is the value of topo_head? What is the value of color[topo_head]? Print it with the format "color[topo_head] = color[i. If color[topo_head] $==2$, set topo[u] as the value of topo_head, and print the updated array of topo. Then, reset topo_head $=u$.
ii. If color[topo_head] ! $=2$, go to Step 6 .

Step 6: What is the value of s_prev[u]? Print it. Is s_prev[u] equal to $u$ ?
i. If $s \_\operatorname{prev}[u]==u$, break the loop and go to Step 1 .
ii. If s_prev[u] !=u, set pr as the value of s_prev[s_last], then set s_prev[s_last] = s_last, and s_last = pr. Go to Step 7.

Step 7: Set $\mathrm{u}=$ s_last and go to Step 2.
Step 8: Print the array of topo.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. etc.):

1. $s=0,0<4$. Since color $[0]==0$, set $s$ last $=0, u=0$, go to Step 2.
2. $\operatorname{color}[u]=\operatorname{color}[0]=0$. Set color $[0]=1$.
3. Iterate through each element v in range(4):
$-v=0: A[0,0]==0$, continue the iteration.
$-v=1: A[0,1]==0$, continue the iteration.
$-v=2: A[0,2]==0$, continue the iteration.
$-\mathrm{v}=3$ : $\mathrm{A}[0,3]!=0$, color $[3]==0$, set color $[3]=1$, $s \_\operatorname{prev}[3]=0$, s_last $=3$, break the iteration.
4. s_last $=3, u=0$, s_last $!=u$, go to Step 7 .
5. Set $u=3$, go to Step 2 .
6. $\operatorname{color}[u]=\operatorname{color}[3]=1$. Set color $[3]=2$.
7. Iterate through each element $v$ in range(4):
$-\mathrm{v}=0: \mathrm{A}[3,0]!=0$, color $[0]!=0$, continue the iteration.
$-v=1: A[3,1]==0$, continue the iteration.
$-\mathrm{v}=2: \mathrm{A}[3,2]!=0$, color[2] $==0$, set color[2] $=1$, $s \_\operatorname{prev}[2]=3$, $s$ last $=2$, break the iteration.
8. s_last $=2, u=3$, s_last $!=u$, go to Step 7 .
9. Set $u=2$, go to Step 2 .
10. $\operatorname{color}[u]=\operatorname{color}[2]=1$. Set $\operatorname{color}[2]=2$.
11. Iterate through each element $v$ in range(4):
$-v=0: A[2,0]==0$, continue the iteration.
$-v=1: A[2,1]==0$, continue the iteration.
$-v=2: A[2,2]==0$, continue the iteration.
$-v=3: A[2,3]==0$, continue the iteration.
12. $s_{\_}$last $=2, u=2$, s_last $==u$, set color[2] $=2$, go to Step 5 .
13. topo_head $=0$, color[topo_head] $=$ color $[0]=1$, go to Step 6 .
14. s_prev[u] = s_prev[2] = 3, s_prev[u] ! $u$, set pr = s_prev[s_last] = s_prev[2] = 3, set s_prev[s_last] = s_prev[2]
$=2$, s_last $=$ pr $=3$, go to Step 7 .
15. Set $u=3$, go to Step 2.
16. $\operatorname{color}[u]=\operatorname{color}[3]=2$, go to Step 3 .
17. Iterate through each element $v$ in range(4):
$-\mathrm{v}=0: \mathrm{A}[3,0]!=0$, color $[0]!=0$, continue the iteration.
$-v=1: A[3,1]==0$, continue the iteration.
$-\mathrm{v}=2: \mathrm{A}[3,2]!=0$, color $[2]!=0$, continue the iteration.
$-v=3: A[3,3]==0$, continue the iteration.
18. s_last $=3, u=3$, s_last $==u$, set color $[3]=2$, go to Step 5 .
19. topo_head $=0$, color[topo_head] $=$ color $[0]=1$, go to Step 6 .
20. s_prev[u] = s_prev[3] = 0, s_prev[u] !=u, set pr =s_prev[s_last] = s_prev[3] = 0, set s_prev[s_last] = s_prev[3] $=3$, s_last $=$ pr $=0$, go to Step 7 .
21. Set $u=0$, go to Step 2 .
22. $\operatorname{color}[u]=\operatorname{color}[0]=1$, go to Step 3 .
23. Iterate through each element $v$ in range(4):
$-v=0: A[0,0]==0$, continue the iteration.
$-v=1: A[0,1]==0$, continue the iteration.
$-v=2: A[0,2]==0$, continue the iteration.
$-v=3: A[0,3]!=0$, color $[3]!=0$, continue the iteration.
24. s_last $=0, u=0$, s_last $==u$, set color $[0]=2$, go to Step 5 .
25. topo_head $=0$, color[topo_head] $=$ color $[0]=2$, set topo $[u]=$ topo $[0]=0$, print topo, reset topo_head $=0$.
26. $s \_\operatorname{prev}[u]=s \_\operatorname{prev}[0]=0, \mathrm{~s} \_\operatorname{prev}[u]==u$, break the loop and go to Step 1 .
27. $s=1,1<4$. Since color $[1]==0$, set $s$ last $=1, u=1$, go to Step 2 .
28. $\operatorname{color}[u]=\operatorname{color}[1]=0$. Set color $[1]=1$.
29. Iterate through each element $v$ in range(4):
$-\mathrm{v}=0: \mathrm{A}[1,0]!=0$, color $[0]!=0$, continue the iteration.
$-v=1: A[1,1]==0$, continue the iteration.
$-v=2: A[1,2]==0$, continue the iteration.
$-v=3: A[1,3]==0$, continue the iteration.
30. s_last $=1, u=1$, s_last $==u$, set color $[1]=2$, go to Step 5 .
31. topo_head $=0$, color $[$ topo_head $]=$ color $[0]=2$, set topo $[u]=$ topo $[1]=0$, print topo, reset topo_head $=1$.
32. $s \_\operatorname{prev}[u]=s \_\operatorname{prev}[1]=1$, $s \_\operatorname{prev}[u]==u$, break the loop and go to Step 1 .
33. $s=2,2<4$. Since color[2] != 0 , increment $s$ by 1 , and go to Step 1 .
34. $s=3,3<4$. Since color $[3]!=0$, increment $s$ by 1 , and go to Step 1 .
35. $s=4, s==4$, go to Step 8 .
36. Print the array of topo: $[0,0,2,3]$

The final topo array is $[0,0,2,3]$.
Table 23: The prompt of topological sort and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the square matrix A of size $3 \times 3$ :
$A[0,0]=0, A[0,1]=1, A[0,2]=1$
$A[1,0]=1, A[1,1]=0, A[1,2]=0$
$A[2,0]=1, A[2,1]=0, A[2,2]=0$.
Set color: color $[0]=0, \operatorname{color}[1]=0, \operatorname{color}[2]=0$.
Set pi: pi $[0]=0, \mathrm{pi}[1]=1, \mathrm{pi}[2]=2$.
Set $\mathrm{d}: \mathrm{d}[0]=0, \mathrm{~d}[1]=0, \mathrm{~d}[2]=0$.
Set s_prev: s_prev[0] = 0, s_prev[1] = 1, s_prev[2] = 2 .
Set time: 0 .
Set low: $\operatorname{low}[0]=0, \operatorname{low}[1]=0, \operatorname{low}[2]=0$.
Set child_cnt: child_cnt[0] $=0$, child_cnt[1] $=0$, child_cnt[2] $=0$.
Set is_cut: is_cut $[0]=0$, is_cut $[1]=0$, is_cut[2] $=0$.
Step 1: Initialize the variable $u$ to 0 and variable s_last to 0 .
Step 2: Start the while loop, and perform the following sub-steps:
Step 2.1: If $\mathrm{d}[\mathrm{u}]$ is 0 :
a. Increment time by 1.
b. Set d[u] to time.
c. Set low[u] to time.
d. Set color[u] to 1 .

Step 2.2: Iterate through variable v from 0 to 2 (inclusive), and for each v:
a. If $A[u, v]$ is not 0 :
i. If color[v] is 0 :

1. Set pi[v] to $u$.
2. Set color[v] to 1.
3. Print s_last and set s_prev[v] to s_last.
4. Set s_last to v .
5. Increment child_cnt[u].
6. Break the $v$ iteration loop and go to Step 2.3.
ii. If color[v] is not 0 :
7. Calculate bne_v_pi_u = v - pi[u] and present the result.
8. If bne_v_pi_u is not 0 , set low[u] to the minimum of low[u] and $d[v]$.

Step 2.3: Calculate beq_s_last_u = s_last -u and present the result.
a. If beq_s_last_u is equal to 0 :
i. Set color[u] to 2.
ii. Increment time by 1.
b. If beq_s_last_u is not 0 , go to Step 2.8.

Step 2.4: Iterate through variable $v$ from 0 to 2 (inclusive), and for each $v$ :
a. Print the value of pi[v] and $u$. Calculate beq_pi_v_u = pi[v]-u and present the result.
b. If beq_pi_v_u is equal to 0 :
i. Go to Step 2.4.1.
ii. Go back to the iteration of $v$.

## Step 2.4.1:

a. Set low[u] to the minimum of low[u] and low[v].
b. Print the values of $u$ and pi[u]. Calculate bne_u_pi_u $=u-p i[u]$ and present the result.
c. IS bne_u_pi_u NON-ZERO OR NOT?
i. If bne_u_pi_u is not 0 :

1. Print the values of low[v] and d[u]. Calculate bge_low_v_d_u=low[v]-d[u] and present the result.
2. If bge_low_v_d_u >=0, set is_cut[u] to 1 .
ii. If bne_u_pi_u is 0 exactly, pass.

Step 2.5: Calculate beq_u_pi_u = u - pi[u] and present the result.
a. If beq_u_pi_u is equal to 0 :

1. Calculate bge_cnt $=$ child_cnt[u] -2 and present the result.
2. If bge_cnt $>=0$, set is_cut[ $u$ ] to 1 .
b. If beq_u_pi_u is not equal to 0 , pass.

Step 2.6: Print the value of s_prev[u]. Then, calculate beq_u_s_prev_u =u - s_prev[u] and present the result. a. If beq_u_s_prev_u is equal to 0 , break the main loop and go to Step 3 .

Step 2.7: Swap s_prev[s_last] and s_last:
a. Set temp to s_prev[s_last].
b. Set s_prev[s_last] to s_last.
c. Set s_last to temp.

Step 2.8: Set u to s_last and go to Step 2.1.
Step 3: Print the is_cut array.

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. etc.):

1. Step 1 , set $u=0$ and s_last $=0$.
2. Step 2, enter the while loop.
3. Step 2.1, since $d[0]=0$, increment time to 1 , set $d[0]=1$, $\operatorname{low}[0]=1$, and color $[0]=1$.
4. Step 2.2, iterate through $v$ from 0 to 2 . For $v=0, A[0,0]=0$, so continue to $v=1$. For $v=1, A[0,1]=1$, and color[1] = 0, so set pi[1] = 0, color[1] = 1, print s_last ( 0 ), set s_prev[1] = 0, set s_last = 1, increment child_cnt[0] to 1 , and break the $v$ iteration loop.
5. Step 2.3, calculate beq_s_last_u = $1-0=1$, which is not 0 , so go to Step 2.8.
6. Step 2.8 , set $u=$ s_last $=1$ and go to Step 2.1.
7. Step 2.1, since $d[1]=0$, increment time to 2 , set $d[1]=2$, $\operatorname{low}[1]=2$, and color[1] $=1$.
8. Step 2.2, iterate through $v$ from 0 to 2 . For $v=0, A[1,0]=1$, but color $[0]=1$, so calculate bne_v_pi_u = 0-0= 0 , and since it is 0 , continue to $v=1$. For $v=1, A[1,1]=0$, so continue to $v=2$. For $v=2, A[1,2]=0$, so the $v$ iteration loop ends.
9. Step 2.3, calculate beq_s_last_u $=1-1=0$, which is equal to 0 , so set color[1] $=2$ and increment time to 3 .
10. Step 2.4, iterate through $v$ from 0 to 2. For $v=0$, print pi[ 0$]$ ( 0 ) and $u(1)$, calculate beq_pi_v_u=0-1=-1, which is not 0 , so continue to $v=1$. For $v=1$, print pi[1] ( 0 ) and $u(1)$, calculate beq_pi_v_u=0-1=-1, which is not 0 , so continue to $v=2$. For $v=2$, print pi[2] (2) and $u(1)$, calculate beq_pi_v_u=2-1=1, which is not 0 , so the $v$ iteration loop ends.
11. Step 2.5 , calculate beq_u_pi_u $=1-0=1$, which is not 0 , so pass.
12. Step 2.6, print s_prev[1] (0), calculate beq_u_s_prev_u =1-0 = 1, which is not 0 , so continue to Step 2.7.
13. Step 2.7, swap s_prev[s_last] and s_last: set temp = s_prev[1] (0), set s_prev[1] = 1, set s_last = temp (0).
14. Step 2.8, set $u=s$ last $=0$ and go to Step 2.1.
15. Step 2.1, since $d[0]$ is not 0 , skip to Step 2.2.
16. Step 2.2, iterate through $v$ from 0 to 2 . For $v=0, A[0,0]=0$, so continue to $v=1$. For $v=1, A[0,1]=1$, but color $[1]=2$, so calculate bne_v_pi_u = $1-0=1$, and since it is not 0 , set low[0] = min(low[0], d[1]) $=\min (1,2)$ $=1$. Continue to $v=2$. For $v=2, A[0,2]=1$, and color[2] $=0$, so set pi[2] $=0$, color[2] $=1$, print s_last ( 0 ), set s_prev[2] $=0$, set s_last $=2$, increment child_cnt[0] to 2, and break the v iteration loop.
17. Step 2.3, calculate beq_s_last_u $=2-0=2$, which is not 0 , so go to Step 2.8.
18. Step 2.8, set $u=$ s_last $=2$ and go to Step 2.1.
19. Step 2.1, since $d[2]=0$, increment time to 4 , set $d[2]=4$, $\operatorname{low}[2]=4$, and color[2] $=1$.
20. Step 2.2, iterate through $v$ from 0 to 2 . For $v=0, A[2,0]=1$, but color $[0]=1$, so calculate bne_v_pi_u $=0-0$ $=0$, and since it is 0 , continue to $v=1$. For $v=1, A[2,1]=0$, so continue to $v=2$. For $v=2, A[2,2]=0$, so the $v$ iteration loop ends.
21. Step 2.3, calculate beq_s_last_u $=2-2=0$, which is equal to 0 , so set color[2] $=2$ and increment time to 5 .
22. Step 2.4, iterate through $v$ from 0 to 2. For $v=0$, print pi $[0]$ ( 0 ) and $u(2)$, calculate beq_pi_v_u = 0-2 $=-2$, which is not 0 , so continue to $v=1$. For $v=1$, print pi[1] ( 0 ) and $u(2)$, calculate beq_pi_v_u=0-2=-2, which is not 0 , so continue to $v=2$. For $v=2$, print pi[2] ( 0 ) and $u(2)$, calculate beq_pi_v_u=0-2=-2, which is not 0 , so the $v$ iteration loop ends.
23. Step 2.5, calculate beq_u_pi_u=2-0=2, which is not 0 , so pass.
24. Step 2.6, print s_prev[2] (0), calculate beq_u_s_prev_u $=2-0=2$, which is not 0 , so continue to Step 2.7.
25. Step 2.7, swap s_prev[s_last] and s_last: set temp = s_prev[2] (0), set s_prev[2] = 2, set s_last = temp (0).
26. Step 2.8, set $u=$ s_last $=0$ and go to Step 2.1.
27. Step 2.1, since $d[0]$ is not 0 , skip to Step 2.2.
28. Step 2.2, iterate through $v$ from 0 to 2 . For $v=0, A[0,0]=0$, so continue to $v=1$. For $v=1, A[0,1]=1$, but color[1] $=2$, so calculate bne_v_pi_u=1-0=1, and since it is not 0 , set low $[0]=\min (\operatorname{low}[0], \mathrm{d}[1])=\min (1,2)=1$. Continue to $v=2$. For $v=2, A[0,2]=1$, but color[ 2$]=2$, so calculate bne_v_pi_u=2-0=2, and since it is not 0 , set low[0] $=\min (\operatorname{low}[0], d[2])=\min (1,4)=1$.
29. Step 2.3, calculate beq_s_last_u $=0-0=0$, which is equal to 0 , so set color[ 0$]=2$ and increment time to 6 .
30. Step 2.4, iterate through $v$ from 0 to 2. For $v=0$, print pi $[0](0)$ and $u(0)$, calculate beq_pi_v_u=0-0=0, which is equal to 0 , so go to Step 2.4.1. For $v=1$, print pi[1] ( 0 ) and $u(0)$, calculate beq_pi_v_u $=0-0=0$, which is equal to 0 , so go to Step 2.4.1. For $v=2$, print pi[2] ( 0 ) and $u(0)$, calculate beq_pi_v_u=0-0=0, which is equal to 0, so go to Step 2.4.1.
31. Step 2.4.1, for $v=0$, $\operatorname{low}[0]=\min (\operatorname{low}[0], \operatorname{low}[0])=\min (1,1)=1$, bne_u_pi_u=0-0=0, so pass. For $v=1$, $\operatorname{low}[0]=\min (\operatorname{low}[0], \operatorname{low}[1])=\min (1,2)=1$, bne_u_pi_u=0-0=0, so pass. For $v=2$, low[0] $=\min (\operatorname{low}[0]$, low[2]) $=\min (1,4)=1$, bne_u_pi_u $=0-0=0$, so pass.
32. Step 2.5, calculate beq_u_pi_u $=0-0=0$, which is equal to 0 , so calculate bge_cnt $=$ child_cnt $[0]-2=2-2$ $=0$, which is $>=0$, so set is_cut[0] to 1 .
33. Step 2.6, print s_prev[0] (0), calculate beq_u_s_prev_u $=0-0=0$, which is equal to 0 , so break the main loop and go to Step 3.
34. Step 3, print the is_cut array: $[1,0,0]$.

The final is_cut array is $[1,0,0]$.
Table 24: The prompt of articulation points and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the square matrix $A$ of size $3 \times 3$ :
$A[0,0]=0, A[0,1]=1, A[0,2]=1$
$A[1,0]=1, A[1,1]=0, A[1,2]=0$
$A[2,0]=1, A[2,1]=0, A[2,2]=0$.
Set color: $\operatorname{color}[0]=0, \operatorname{color}[1]=0, \operatorname{color}[2]=0$.
Set pi: pi[0] = 0, pi[1] = 1, pi[2] = 2 .
Set $d: d[0]=0, d[1]=0, d[2]=0$.
Set s_prev: s_prev[0] $=0$, s_prev[1] $=1, s \_p r e v[2]=2$.
Set time: 0 .
Set low: $\operatorname{low}[0]=0, \operatorname{low}[1]=0, \operatorname{low}[2]=0$.
Set is_bridge: [].
Step 1: Initialize the variable u to 0 and variable s_last to 0 .
Step 2: Start the while loop, and perform the following sub-steps:
Step 2.1: If $d[u]$ is 0 :
a. Increment time by 1.
b. Set d[u] to time.
c. Set low[u] to time.
d. Set color[u] to 1 .

Step 2.2: Iterate through variable v from 0 to 2 (inclusive), and for each v :
a. If $A[u, v]$ is not 0 :
i. If color[v] is 0 :

1. Set pi[v] to u.
2. Set color[v] to 1.
3. Print s_last and set s_prev[v] to s_last.
4. Set s_last to $v$.
5. Break the viteration loop and go to Step 2.3.
ii. If color[v] is not 0 :
6. Calculate bne_v_pi_u = v-pi[u] and present the result.
7. If bne_v_pi_u is not 0 , set low[u] to the minimum of low[u] and $d[v]$.
8. If bne_v_pi_u is 0 exactly, pass.

Step 2.3: Calculate beq_s_last_u = s_last - $u$ and present the result.
a. If beq_s_last_u is equal to 0 :
i. Set color[u] to 2.
ii. Increment time by 1.
b. If beq_s_last_u is not 0 , go to Step 2.7.

Step 2.4: Iterate through variable v from 0 to 2 (inclusive), and for each v:
a. Print the value of $p i[v]$ and $u$. Calculate beq_pi_v_u $=p i[v]-u$ and present the result.
b. If beq_pi_v_u is equal to 0 :
i. Go to Step 2.4.1.
ii. Go back to the iteration of $v$.

## Step 2.4.1:

a. Set low[u] to the minimum of low[u] and low[v].
b. Print the values of low[v] and d[u]. Calculate bg_low_v_d_u = low[v]-d[u] and present the result. i. If bg_low_v_d_u>0, append ( $u, v$ ) to the list bridges.
ii. If bg_low_v_d_u <= 0 , pass.

Step 2.5: Print the value of s_prev[u]. Then, calculate beq_u_s_prev_u =u-s_prev[u] and present the result.
a. If beq_u_s_prev_u is equal to 0 , break the while loop and go to Step 3 .

Step 2.6: Swap s_prev[s_last] and s_last:
a. Set temp to s_prev[s_last].
b. Set s_prev[s_last] to s_last.
c. Set s_last to temp.

Step 2.7: Set u to s_last and go to Step 2.1.
Step 3: Print the list bridges.

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. etc.):

1. Step 1 , set $u=0$ and s_last $=0$.
2. Step 2, enter the while loop.
3. Step 2.1, since $d[0]$ is 0 :
a. Increment time to 1 .
b. Set d[0] to 1 .
c. Set low[0] to 1 .
d. Set color[0] to 1 .
4. Step 2.2, iterate through $v$ from 0 to 2 :
a. For $v=0, A[0,0]$ is 0 , so continue to the next $v$.
b. For $v=1, A[0,1]$ is 1 :
i. color[1] is 0 , so:
5. Set pi[1] to 0.
6. Set color[1] to 1.
7. Print s_last ( 0 ) and set s_prev[1] to 0 .
8. Set s_last to 1 .
9. Break the $v$ iteration loop.
10. Step 2.3, calculate beq_s_last_u=1-0=1, which is not 0 , so go to Step 2.7.
11. Step 2.7, set u to s_last (1) and go to Step 2.1.
12. Step 2.1, since $d[1]$ is 0 :
a. Increment time to 2.
b. Set d[1] to 2.
c. Set low[1] to 2.
d. Set color[1] to 1 .
13. Step 2.2, iterate through $v$ from 0 to 2 :
a. For $v=0, A[1,0]$ is 1 :
i. color $[0]$ is 1 , so:
14. Calculate bne_v_pi_u $=0-\mathrm{pi}[1]=0-0=0$, which is 0 , so pass.
b. For $v=1, A[1,1]$ is 0 , so continue to the next $v$.
c. For $v=2, A[1,2]$ is 0 , so continue to the next $v$.
15. Step 2.3, calculate beq_s_last_u = 1-1 = 0 , which is 0 , so:
a. Set color[1] to 2 .
b. Increment time to 3 .
16. Step 2.4, iterate through $v$ from 0 to 2 :
a. For $v=0$, print pi $[0]$ ( 0 ) and $u(1)$, calculate beq_pi_v_u $=$ pi $[0]-u=0-1=-1$, which is not 0 .
b. For $v=1$, print pi[1] (0) and $u(1)$, calculate beq_pi_v_u $=$ pi[1] $-u=0-1=-1$, which is not 0 .
c. For $v=2$, print pi[2] (2) and $u(1)$, calculate beq_pi_v_u=pi[2]-u=2-1=1, which is not 0 .
17. Step 2.5, print s_prev[1] (0), calculate beq_u_s_prev_u $=1-\mathrm{s} \_$prev[1] $=1-0=1$, which is not 0 .
18. Step 2.6, swap s_prev[s_last] and s_last:
a. Set temp to s_prev[1] (0).
b. Set s_prev[1] to s_last (1).
c. Set s_last to temp (0).
19. Step 2.7, set u to s_last (0) and go to Step 2.1.
20. Step 2.1, since $d[0]$ is not 0 , skip this step.
21. Step 2.2, iterate through $v$ from 0 to 2 :
a. For $v=0, A[0,0]$ is 0 , so continue to the next $v$.
b. For $v=1, A[0,1]$ is 1 :
i. color[1] is 2 , so:
22. Calculate bne_v_pi_u = $1-\mathrm{pi}[0]=1-0=1$, which is not 0 , so set low[0] to $\min (\operatorname{low}[0], d[1])=\min (1,2)$ $=1$.
c. For $\mathrm{v}=2, \mathrm{~A}[0,2]$ is 1 :
i. color[2] is 0 , so:
23. Set pi[2] to 0 .
24. Set color[2] to 1.
25. Print s_last ( 0 ) and set s_prev[2] to 0 .
26. Set s_last to 2.
27. Break the $v$ iteration loop.
28. Step 2.3, calculate beq_s_last_u $=2-0=2$, which is not 0 , so go to Step 2.7.
29. Step 2.7, set u to s_last (2) and go to Step 2.1.
30. Step 2.1, since $\mathrm{d}[2]$ is 0 :
a. Increment time to 4.
b. Set d[2] to 4.
c. Set low[2] to 4.
d. Set color[2] to 1.
31. Step 2.2, iterate through $v$ from 0 to 2 :
a. For $\mathrm{v}=0, \mathrm{~A}[2,0]$ is 1 :
i. color[0] is 1 , so:
32. Calculate bne_v_pi_u = 0-pi[2] =0-0=0, which is 0 , so pass.
b. For $v=1, A[2,1]$ is 0 , so continue to the next $v$.
c. For $v=2, A[2,2]$ is 0 , so continue to the next $v$.
33. Step 2.3, calculate beq_s_last_u $=2-2=0$, which is 0 , so:
a. Set color[2] to 2.
b. Increment time to 5 .
34. Step 2.4, iterate through $v$ from 0 to 2 :
a. For $v=0$, print pi $[0]$ (0) and $u(2)$, calculate beq_pi_v_u $=$ pi $[0]-u=0-2=-2$, which is not 0 .
b. For $v=1$, print pi[1] (0) and $u(2)$, calculate beq_pi_v_u $=$ pi $[1]-u=0-2=-2$, which is not 0 .
c. For $v=2$, print pi[2] (0) and $u(2)$, calculate beq_pi_v_u=pi[2]-u=0-2=-2, which is not 0 .
35. Step 2.5, print s_prev[2] (0), calculate beq_u_s_prev_u $=2-\mathrm{s} \_$prev[2] $=2-0=2$, which is not 0 .
36. Step 2.6, swap s_prev[s_last] and s_last:
a. Set temp to s_prev[2] (0).
b. Set s_prev[2] to s_last (2).
c. Set s_last to temp (0).
37. Step 2.7, set u to s_last (0) and go to Step 2.1.
38. Step 2.1, since $d[0]$ is not 0 , skip this step.
39. Step 2.2, iterate through $v$ from 0 to 2 :
a. For $v=0, A[0,0]$ is 0 , so continue to the next $v$.
b. For $v=1, A[0,1]$ is 1 :
i. color[1] is 2, so:
40. Calculate bne_v_pi_u $=1-\mathrm{pi}[0]=1-0=1$, which is not 0 , so set low[0] to $\min (\operatorname{low}[0], d[1])=\min (1,2)$ $=1$.
c. For $v=2, A[0,2]$ is 1 :
i. color[2] is 2, so:
41. Calculate bne_v_pi_u $=2-\mathrm{pi}[0]=2-0=2$, which is not 0 , so set $\operatorname{low}[0]$ to $\min (\operatorname{low}[0], d[2])=\min (1,4)$ $=1$.
42. Step 2.3, calculate beq_s_last_u $=0-0=0$, which is 0 , so:
a. Set color[0] to 2.
b. Increment time to 6 .
43. Step 2.4, iterate through $v$ from 0 to 2 :
a. For $v=0$, print pi[0] (0) and $u(0)$, calculate beq_pi_v_u $=$ pi[ $[0]-\mathrm{u}=0-0=0$, which is 0 , so go to Step 2.4.1.
i. Step 2.4.1:
a. Set low[0] to $\min (\operatorname{low}[0]$, $\operatorname{low}[0])=\min (1,1)=1$.
b. Print low[0] (1) and d[0] (1), calculate bg_low_v_d_u = low[0]-d[0]=1-1=0, which is $<=0$, so pass.
b. For $v=1$, print pi[1] ( 0 ) and $u(0)$, calculate beq_pi_v_u=pi[1]-u=0-0=0, which is 0 , so go to Step 2.4.1.
i. Step 2.4.1:
a. Set low[0] to $\min (\operatorname{low}[0]$, $\operatorname{low}[1])=\min (1,2)=1$.
b. Print low[1] (2) and d[0] (1), calculate bg_low_v_d_u=low[1]-d[0]=2-1=1, which is $>0$, so append
$(0,1)$ to the list bridges.
c. For $v=2$, print pi[2] ( 0 ) and $u(0)$, calculate beq_pi_v_u $=$ pi[2] $-u=0-0=0$, which is 0 , so go to Step 2.4.1.
i. Step 2.4.1:
a. Set low[0] to $\min (\operatorname{low}[0]$, $\operatorname{low}[2])=\min (1,4)=1$.
b. Print low[2] (4) and d[0] (1), calculate bg_low_v_d_u = low[2] - d[0] = 4-1 = 3, which is $>0$, so append $(0,2)$ to the list bridges.
44. Step 2.5, print s_prev[0] (0), calculate beq_u_s_prev_u $=0-$ s_prev[0] $=0-0=0$, which is 0 , so break the while loop and go to Step 3.
45. Step 3, print the list bridges: $[(0,1),(0,2)]$.

The list of bridges is $[(0,1),(0,2)]$.
Table 25: The prompt of bridges and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the square matrix $A$ of size $3 \times 3$ :
$A[0,0]=0, A[0,1]=1, A[0,2]=1$
$A[1,0]=1, A[1,1]=0, A[1,2]=0$
$A[2,0]=0, A[2,1]=0, A[2,2]=0$.
Set color: color $[0]=0$, color $[1]=0$, color $[2]=0$.
Set $\mathrm{d}: \mathrm{d}[0]=0, \mathrm{~d}[1]=0, \mathrm{~d}[2]=0$.
Set $\mathrm{f}: \mathrm{f}[0]=0, \mathrm{f}[1]=0, \mathrm{f}[2]=0$.
Set s_prev: s_prev[0] = 0, s_prev[1] = 1, s_prev[2] $=2$.
Set $B: B[0,0]=0, B[0,1]=1, B[0,2]=0$
$\mathrm{B}[1,0]=1, \mathrm{~B}[1,1]=0, \mathrm{~B}[1,2]=0$
$\mathrm{B}[2,0]=1, \mathrm{~B}[2,1]=0, \mathrm{~B}[2,2]=0$.
Set $s c c \_i d: s c c \_i d[0]=0, \operatorname{scc} \_i d[1]=1, s c c \_i d[2]=2$.
Step 1: Initialize variable time to 0.
Step 2: Iterate through the variable s from 0 to 2 (inclusive), and for each s:
Step 2.1: Check if color[s] is equal to 0 . If true, perform the following steps:
Step 2.2: Set s_last to s.
Step 2.3: Set u to s.
Step 2.4: Set v to s.

Step 2.5: Start the while loop, and perform the following sub-steps:
Step 2.5.1: If color[ $u$ ] is 0 or $d[u]$ is 0 :
a. Increment time by 1 .
b. Set d[u] to time.
c. Set color[u] to 1 .

Otherwise, do nothing.
Step 2.5.2: Iterate through the variable $v$ from 0 to 2 (inclusive), and for each $v$ :
a. If $A[u, v]$ is not 0 , then check the value of color[v]:
i. If color $[v]$ is 0 :

1. Set color[v] to 1.
2. Set s_prev[v] to s_last.
3. Set s_last to v .
4. Break the $v$ iteration loop.
i. If color[ v$]$ is 1 or is 2 :
5. Continue the $v$ iteration loop.

Step 2.5.3: Calculate beq_s_last_u = s_last $-u$ and present the result.
a. If beq_s_last_u is equal to 0 :
i. Set color[u] to 2.
ii. Increment time by 1.
iii. Set $f[u]$ to time.
iv. Go to Step 2.5.4.
b. If beq_s_last_u is not equal to 0 , go to Step 2.5.5

Step 2.5.4: Calculate beq_s_prev_u_u =s_prev[u]-u and present the result.
a. If beq_s_prev_u_u is equal to 0 : break the while loop and go to the next iteration of s.
b. If beq_s_prev_u_u is not equal to 0 :

Step 2.5.4.1: Swap s_prev[s_last] and s_last:
a. Print the value of s_last and s_prev[s_last].
b. Set temp to s_prev[s_last].
c. Set s_prev[s_last] to s_last.
d. Set s_last to temp.

Step 2.5.5: Set u to s_last and go back to the beginning of the while loop, which is Step 2.5.1
Step 3: Reinitialize color to color[0] $=0$, color $[1]=0, \operatorname{color}[2]=0$. Set $s \_p r e v$ to $s \_p r e v[0]=0, s \_p r e v[1]=1$, s_prev[2] = 2 .

Step 4: Argsort f array in descending order. Perform the following sub-steps:
Step 4.1: Print each element of the f array along with its index in the format (fij, i) for i in the range of 0 to 2 .
Step 4.2: Sort the pairs (f[i], i) in descending order based on f[i]. Reorder the pairs according to the sorted f[i] values.

Step 4.3: Extract the index $i$, which is the second element from each sorted pair, and create the visit_order array.

Step 4.4: Print the visit_order array.
Step 5: Iterate through the variable s in visit_order, and for each s:
Step 5.1: Check if color[s] is equal to 0 . If true, perform the following steps:
Step 5.2: Set s_last to s.
Step 5.3: Set u to s.
Step 5.4: Set v to s.

Step 5.5: Start the while loop, and perform the following sub-steps:
Step 5.5.1: Set scc_id[u] to s.
Step 5.5.2: If color[u] is 0 or $d[u]$ is 0 :
a. Increment time by 1 .
b. Set d[u] to time.
c. Set color[u] to 1 .

Otherwise, do nothing.

Step 5.5.3: Iterate through the variable v from 0 to 2 (inclusive), and for each v :
a. If $B[u, v]$ is not 0 , then check the value of color[v]:
i. If color $[v]$ is 0 :

1. Set color[v] to 1.
2. Set s_prev[v] to s_last.
3. Set s_last to v .
4. Break the $v$ iteration loop.
ii. If color[v] is 1 or is 2 : Continue the $v$ iteration loop.

Step 5.5.4: Calculate beq_s_last_u = s_last $-u$ and present the result.
a. If beq_s_last_u is equal to 0 :
i. Set color[u] to 2.
ii. Increment time by 1.
iii. Set $f[u]$ to time.
b. If beq_s_last_u is not equal to 0 , go to Step 5.5.6

Step 5.5.5: Calculate beq_s_prev_u_u = s_prev[u] - u and present the result.
a. If beq_s_prev_u_u is equal to 0 : break the while loop and go to the next iteration of $s$.
b. If beq_s_prev_u_u is not equal to 0 :

Step 5.5.5.1: Swap s_prev[s_last] and s_last:
a. Print the value of $s$ _last and $s \_p r e v\left[s \_l a s t\right]$.
b. Set temp to s_prev[s_last].
c. Set s_prev[s_last] to s_last.
d. Set s_last to temp.

Step 5.5.6: Set $u$ to $s \_l a s t ~ a n d ~ g o ~ b a c k ~ t o ~ t h e ~ b e g i n n i n g ~ o f ~ t h e ~ w h i l e ~ l o o p, ~ w h i c h ~ i s ~ S t e p ~ 5.5 .1 . ~$
Step 6: Print the scc_id array by iterating over its elements.

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. etc.):

1. Step 1 , set time $=0$.
2. Step 2, iterate s from 0 to 2.
3. Step 2.1, for $s=0$, color $[0]=0$, so proceed to Step 2.2.
4. Step 2.2, set s_last $=0$.
5. Step 2.3, set $u=0$.
6. Step 2.4, set $v=0$.
7. Step 2.5, start the while loop.
8. Step 2.5.1, color $[0]=0$ and $d[0]=0$, so increment time to 1 , set $d[0]=1$, and set color $[0]=1$.
9. Step 2.5.2, iterate $v$ from 0 to 2 .
10. Step 2.5.2.a, for $v=0, A[0,0]=0$, so continue to $v=1$.
11. Step 2.5.2.a, for $v=1, A[0,1]=1$, so color[1] $=0$, set color[1] $=1$, s_prev[1] = 0 , s_last = 1, and break the $v$ loop.
12. Step 2.5.3, beq_s_last_u $=1-0=1$, so go to Step 2.5.5.
13. Step 2.5.5, set $u=1$.
14. Step 2.5.1, color[1] $=1$ and d[1] $=0$, so increment time to 2 , set $d[1]=2$, and set color $[1]=1$.
15. Step 2.5.2, iterate $v$ from 0 to 2.
16. Step 2.5.2.a, for $v=0, A[1,0]=1$, so color $[0]=1$, continue to $v=1$.
17. Step 2.5.2.a, for $v=1, A[1,1]=0$, so continue to $v=2$.
18. Step 2.5.2.a, for $v=2, A[1,2]=0$, so continue.
19. Step 2.5.3, beq_s_last_u=1-1=0, so set color[1] = 2 , increment time to 3 , set $f[1]=3$, and go to Step 2.5.4.
20. Step 2.5.4, beq_s_prev_u_u $=0-1=-1$, so go to Step 2.5.4.1.
21. Step 2.5.4.1, swap s_prev[s_last] and s_last, set temp $=$ s_prev[1] $=0$, s_prev[1] $=1$, s_last $=0$.
22. Step 2.5.5, set u=0.
23. Step 2.5.1, color $[0]=1$ and $d[0]=1$, so continue to Step 2.5.2.
24. Step 2.5.2, iterate $v$ from 0 to 2.
25. Step 2.5.2.a, for $v=0, A[0,0]=0$, so continue to $v=1$.
26. Step 2.5.2.a, for $v=1, A[0,1]=1$, so color $[1]=2$, continue to $v=2$.
27. Step 2.5.2.a, for $v=2, A[0,2]=1$, so color $[2]=0$, set color $[2]=1$, $s \_$prev $[2]=0$, s_last $=2$, and break the $v$ loop.
28. Step 2.5.3, beq_s_last_u $=2-0=2$, so go to Step 2.5.5.
29. Step 2.5.5, set $u=2$.
30. Step 2.5.1, color[2] $=1$ and d[2] $=0$, so increment time to 4 , set $d[2]=4$, and set color[2] $=1$.
31. Step 2.5.2, iterate $v$ from 0 to 2 .
32. Step 2.5.2.a, for $v=0, A[2,0]=0$, so continue to $v=1$.
33. Step 2.5.2.a, for $v=1, A[2,1]=0$, so continue to $v=2$.
34. Step 2.5.2.a, for $v=2, A[2,2]=0$, so continue.
35. Step 2.5.3, beq_s_last_u $=2-2=0$, so set color[2] $=2$, increment time to 5 , set $f[2]=5$, and go to Step 2.5.4.
36. Step 2.5.4, beq_s_prev_u_u = 0-2 =-2, so go to Step 2.5.4.1.
37. Step 2.5.4.1, swap s_prev[s_last] and s_last, set temp $=$ s_prev[2] $=0$, s_prev[2] $=2$, s_last $=0$.
38. Step 2.5.5, set $u=0$.
39. Step 2.5.1, color $[0]=1$ and $d[0]=1$, so continue to Step 2.5.2.
40. Step 2.5.2, iterate $v$ from 0 to 2.
41. Step 2.5.2.a, for $v=0, A[0,0]=0$, so continue to $v=1$.
42. Step 2.5.2.a, for $v=1, A[0,1]=1$, so color $[1]=2$, continue to $v=2$.
43. Step 2.5.2.a, for $v=2, A[0,2]=1$, so color $[2]=2$, continue.
44. Step 2.5.3, beq_s_last_u $=0-0=0$, so set color $[0]=2$, increment time to 6 , set $f[0]=6$, and go to Step 2.5.4.
45. Step 2.5.4, beq_s_prev_u_u $=0-0=0$, so break the while loop and go to the next iteration of s .
46. Step 2.1, for $s=1$, $\operatorname{color}[1]=2$, so continue to $s=2$.
47. Step 2.1, for $s=2$, color[2] $=2$, so continue.
48. Step 3, reinitialize color to color $[0]=0$, color $[1]=0$, color $[2]=0$, and set s_prev to s_prev[ $[0]=0$, s_prev $[1]=1$, s_prev[2] $=2$.
49. Step 4, argsort f array in descending order.
50. Step 4.1, print $(f[0], 0)=(6,0),(f[1], 1)=(3,1),(f[2], 2)=(5,2)$.
51. Step 4.2, sort the pairs in descending order: $(6,0),(5,2),(3,1)$.
52. Step 4.3, create visit_order array: $[0,2,1]$.
53. Step 4.4, print visit_order: $[0,2,1]$.
54. Step 5, iterate s in visit_order.
55. Step 5.1, for $s=0$, color[0] $=0$, so proceed to Step 5.2
56. Step 5.2, set s_last $=0$.
57. Step 5.3, set $u=0$.
58. Step 5.4, set $v=0$.
59. Step 5.5, start the while loop.
60. Step 5.5.1, set scc_id[0] $=0$.
61. Step 5.5.2, color $[0]=0$ and $\mathrm{d}[0]=0$, so increment time to 7 , set $\mathrm{d}[0]=7$, and set color $[0]=1$.
62. Step 5.5.3, iterate $v$ from 0 to 2.
63. Step 5.5.3.a, for $v=0, B[0,0]=0$, so continue to $v=1$.
64. Step 5.5.3.a, for $v=1, B[0,1]=1$, so color $[1]=0$, set color $[1]=1$, $s \_$prev $[1]=0$, s_last $=1$, and break the $v$ loop.
65. Step 5.5.4, beq_s_last_u $=1-0=1$, so go to Step 5.5.6.
66. Step 5.5.6, set $u=1$.
67. Step 5.5.1, set scc_id[1] $=0$.
68. Step 5.5.2, color $[1]=1$ and $\mathrm{d}[1]=0$, so increment time to 8 , set $\mathrm{d}[1]=8$, and set color[1] = 1 .
69. Step 5.5.3, iterate $v$ from 0 to 2.
70. Step 5.5.3.a, for $\mathrm{v}=0, \mathrm{~B}[1,0]=1$, so color $[0]=1$, continue to $\mathrm{v}=1$.
71. Step 5.5.3.a, for $v=1, B[1,1]=0$, so continue to $v=2$.
72. Step 5.5.3.a, for $v=2, B[1,2]=0$, so continue.
73. Step 5.5.4, beq_s_last_u $=1-1=0$, so set color $[1]=2$, increment time to 9 , set $f[1]=9$, and go to Step 5.5.5
74. Step 5.5.5, beq_s_prev_u_u =0-1=-1, so go to Step 5.5.5.1.
75. Step 5.5.5.1, swap s_prev[s_last] and s_last, set temp $=$ s_prev[1] $=0$, s_prev[1] $=1$, s_last $=0$.
76. Step 5.5.6, set $u=0$.
77. Step 5.5.1, set scc_id[0] $=0$.
78. Step 5.5.2, color $[0]=1$ and $d[0]=7$, so continue to Step 5.5.3.
79. Step 5.5.3, iterate $v$ from 0 to 2.
80. Step 5.5.3.a, for $v=0, B[0,0]=0$, so continue to $v=1$.
81. Step 5.5.3.a, for $v=1, B[0,1]=1$, so color $[1]=2$, continue to $v=2$.
82. Step 5.5.3.a, for $v=2, B[0,2]=0$, so continue.
83. Step 5.5.4, beq_s_last_u = 0-0=0, so set color[0] = 2, increment time to 10 , set f[0] = 10, and go to Step 5.5.5.
84. Step 5.5 .5 , beq_s_prev_u_u $=0-0=0$, so break the while loop and go to the next iteration of s .
85. Step 5.1, for $\mathrm{s}=2$, color[2] $=0$, so proceed to Step 5.2.
86. Step 5.2, set s_last $=2$.
87. Step 5.3 , set $u=2$.
88. Step 5.4 , set $v=2$.
89. Step 5.5, start the while loop.
90. Step 5.5.1, set scc_id[2] = 2.
91. Step 5.5.2, color[2] $=0$ and $\mathrm{d}[2]=0$, so increment time to 11 , set $\mathrm{d}[2]=11$, and set color[2] $=1$.
92. Step 5.5.3, iterate $v$ from 0 to 2.
93. Step 5.5.3.a, for $v=0, B[2,0]=1$, so color $[0]=2$, continue to $v=1$.
94. Step 5.5.3.a, for $v=1, B[2,1]=0$, so continue to $v=2$.
95. Step 5.5.3.a, for $v=2, B[2,2]=0$, so continue.
96. Step 5.5.4, beq_s_last_u =2-2 $=0$, so set color[2] $=2$, increment time to 12 , set f[2] $=12$, and go to Step 5.5.5.
97. Step 5.5.5, beq_s_prev_u_u = 2-2 = 0, so break the while loop and go to the next iteration of s.
98. Step 5.1, for $s=1, \operatorname{color}[1]=2$, so continue.
99. Step 6, print scc_id array: [0, 0, 2].

The final scc_id array is $[0,0,2]$.
Table 26: The prompt of strongly connected components and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the list of distances between vertices, $\operatorname{Ix}, \mathrm{ly}, \mathrm{w}: \operatorname{Ix}[0]=0, \operatorname{Ix}[1]=2, \operatorname{Ix}[2]=0, \operatorname{Ix}[3]=1, \operatorname{Ix}[4]=1, \operatorname{Ix}[5]=$ $0, \operatorname{ly}[0]=3, \operatorname{ly}[1]=3, \operatorname{ly}[2]=2, \operatorname{ly}[3]=2, \operatorname{ly}[4]=3, \operatorname{ly}[5]=1, w[0]=1, w[1]=1, w[2]=2, w[3]=3, w[4]=4, w[5]$ $=5$, with the length of $M=6$. Set $N=4$ to represent the number of vertices. Set pi as an array of indices from 0 to $\mathrm{N}-1$ : pi $[0]=0, \mathrm{pi}[1]=1, \mathrm{pi}[2]=2, \mathrm{pi}[3]=3$. Set variables weight_sum to 0 and cnt to 0 .

Step 1.1: Assign k to the value of x .
Step 1.2: While $\mathrm{pi}[\mathrm{x}]$ is not equal to x , set $\mathrm{x}=\mathrm{pi}[\mathrm{x}]$, then goto Step 1.2.
Step 1.3: While pi $[k]$ is not equal to $k$, set $w=p i[k]$, set $p i[k]=x$, and set $k=w$, then goto Step 1.3.
Step 1.4: Return the final value of $x$.
Step 2.1: Set x to u and goto Step 1.1.
Step 2.2: Assign the returned value to root_u.
Step 2.3: Set x to v and goto Step 1.1.
Step 2.4: Assign the returned value to root_v.
Step 2.5: Check if root_u is not equal to root_v.
a. If True, set pi[root_u] = root_v and return True.
b. If False, return False.

Step 3: Set i to 0.
Step 3.1: If i is less than 6, goto Step 3.2. Otherwise, goto Step 4.
Step 3.2: Assign $u$ to $\mathrm{Ix}[\mathrm{i}]$, and $v$ to the value at index $i$ in the ly list.
Step 3.3: Goto Step 2.1. If the function returns True, perform these sub-steps:
i. Add $w[i]$ to weight_sum.
ii. Increment ent by 1.
iii. Check if cnt equals 3. If True, go to Step 4.

Step 3.4: Increment i by 1.
Step 3.5: Goto Step 3.1.
Step 4: Print the value of weight_sum.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc., and remember, the next number of 59 is 60 ):

1. In Step $3, i=0$.
2. In Step 3.2, $u=\operatorname{lx}[0]=0, v=\operatorname{ly}[0]=3$.
3. In Step 2.1, $\mathrm{x}=\mathrm{u}=0$, and we go to Step 1.1.
4. In Step 1.1, $\mathrm{k}=\mathrm{x}=0$.
5. In Step 1.2, pi $[x]=\mathrm{pi}[0]=0$, so $\mathrm{x}=0$.
6. In Step 1.3, pi[k] $=$ pi $[0]=0$, so $k=0$.
7. In Step 1.4, we return $x=0$.
8. In Step 2.2, root_u = 0 .
9. In Step 2.3, $x=v=3$, and we go to Step 1.1.
10. In Step 1.1, $\mathrm{k}=\mathrm{x}=3$.
11. In Step 1.2, pi $[x]=p i[3]=3$, so $x=3$.
12. In Step 1.3, pi[k] $=\mathrm{pi}[3]=3$, so $k=3$.
13. In Step 1.4, we return $x=3$.
14. In Step 2.4, root_v $=3$.
15. In Step 2.5, root_u is not equal to root_v, so we set pi[root_u] = pi[0] = 3 and return True.
16. In Step 3.3.i, we add $w[0]=1$ to weight_sum, making weight_sum $=1$.
17. In Step 3.3.ii, we increment cnt by 1, making $\mathrm{cnt}=1$.
18. In Step 3.4, we increment $i$ by 1 , making $i=1$.
19. In Step 3.2, $u=\operatorname{lx}[1]=2, v=\operatorname{ly}[1]=3$.
20. In Step 2.1, $x=u=2$, and we go to Step 1.1.
21. In Step 1.1, $\mathrm{k}=\mathrm{x}=2$.
22. In Step 1.2, pi[x] $=\mathrm{pi}[2]=2$, so $x=2$.
23. In Step 1.3, pi[k] $=$ pi $[2]=2$, so $k=2$.
24. In Step 1.4, we return $x=2$.
25. In Step 2.2, root_u = 2 .
26. In Step 2.3, $x=v=3$, and we go to Step 1.1.
27. In Step 1.1, $\mathrm{k}=\mathrm{x}=3$.
28. In Step 1.2, $\mathrm{pi}[\mathrm{x}]=\mathrm{pi}[3]=3$, so $\mathrm{x}=3$.
29. In Step 1.3, pi[k] $=\mathrm{pi}[3]=3$, so $\mathrm{k}=3$.
30. In Step 1.4, we return $x=3$.
31. In Step 2.4, root_v = 3 .
32. In Step 2.5, root_u is not equal to root_v, so we set pi[root_u] $=$ pi[2] $=3$ and return True.
33. In Step 3.3.i, we add $w[1]=1$ to weight_sum, making weight_sum $=2$.
34. In Step 3.3.ii, we increment cnt by 1, making $\mathrm{cnt}=2$.
35. In Step 3.4, we increment i by 1, making $i=2$.
36. In Step 3.2, $u=1 x[2]=0, v=\operatorname{ly}[2]=2$.
37. In Step 2.1, $x=u=0$, and we go to Step 1.1.
38. In Step 1.1, $\mathrm{k}=\mathrm{x}=0$.
39. In Step 1.2, pi $[x]=\mathrm{pi}[0]=3$, so $\mathrm{x}=3$.
40. In Step 1.3, pi[k] $=$ pi $[0]=3$, so $k=0$.
41. In Step 1.4, we return $x=3$.
42. In Step 2.2, root_u $=3$.
43. In Step 2.3, $x=\bar{v}=2$, and we go to Step 1.1.
44. In Step 1.1, $\mathrm{k}=\mathrm{x}=2$.
45. In Step 1.2, pi $[x]=\mathrm{pi}[2]=3$, so $\mathrm{x}=3$.
46. $\ln$ Step 1.3, pi$[k]=p i[2]=3$, so $k=2$.
47. In Step 1.4, we return $x=3$.
48. In Step 2.4, root_v $=3$.
49. In Step 2.5, root_u is equal to root_v, so we return False.
50. In Step 3.4, we increment $i$ by 1 , making $i=3$.
51. In Step 3.2, $u=\operatorname{lx}[3]=1, v=\operatorname{ly}[3]=2$.
52. In Step 2.1, $x=u=1$, and we go to Step 1.1.
53. In Step 1.1, $\mathrm{k}=\mathrm{x}=1$.
54. In Step 1.2, pi $[x]=p i[1]=1$, so $x=1$.
55. In Step 1.3, pi[k] $=p i[1]=1$, so $k=1$.
56. In Step 1.4, we return $x=1$.
57. In Step 2.2, root_u $=1$.
58. In Step 2.3, $x=\bar{v}=2$, and we go to Step 1.1.
59. In Step 1.1, $\mathrm{k}=\mathrm{x}=2$.
60. In Step 1.2, pi $[x]=p i[2]=3$, so $x=3$.
61. In Step 1.3, pi[k] $=$ pi $[2]=3$, so $k=2$.
62. In Step 1.4, we return $x=3$.
63. In Step 2.4, root_v $=3$.
64. In Step 2.5, root_u is not equal to root_v, so we set pi[root_u] = pi[1] = 3 and return True.
65. In Step 3.3.i, we add $w[3]=3$ to weight_sum, making weight_sum $=5$.
66. In Step 3.3.ii, we increment cnt by 1, making cnt $=3$.
67. In Step 4, we print the value of weight_sum, which is 5 .

The value of weight_sum is 5 .
Table 27: The prompt of mst kruskal and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the adjacency matrix $A$ with the size $4 \times 4$ :
$\mathrm{A}[0,0]=0, \mathrm{~A}[0,1]=3, \mathrm{~A}[0,2]=5, \mathrm{~A}[0,3]=4$
$A[1,0]=3, A[1,1]=0, A[1,2]=6, A[1,3]=0$
$A[2,0]=5, A[2,1]=6, A[2,2]=0, A[2,3]=3$
$A[3,0]=4, A[3,1]=0, A[3,2]=3, A[3,3]=0$,
where $\mathrm{N}=4$ is the number of vertices. Set the start vertex $\mathrm{s}=0$.
Set variables key, mark, and pi as arrays of zeros with 4 elements:
key: $\operatorname{key}[0]=0, \operatorname{key}[1]=0, \operatorname{key}[2]=0, \operatorname{key}[3]=0$,
mark: $\operatorname{mark}[0]=0, \operatorname{mark}[1]=0, \operatorname{mark}[2]=0, \operatorname{mark}[3]=0$,
pi: pi $[0]=0$, pi $[1]=0$, pi $[2]=0$, pi $[3]=0$,
Set the array of in_queue: in_queue[0] = 1 , in_queue[1] = 0 , in_queue[2] $=0$, in_queue[3] = 0 .
Step 1: Assign k to 0.
Step 2.1: Assign u to -1.
Step 2.2: Assign i to 0.
Step 2.2.1: If i is less than 4, go to Step 2.2.2. Otherwise, go to Step 2.3.
Step 2.2.2: Check if in_queue[i] equals 1. If True, go to Step 2.2.3.
Step 2.2.3: Check if $u$ equals -1. If True, assign ito $u$. Then, go to Step 2.2.5.
Step 2.2.4: What are the value of key[i] and key[u]? Then, what is the result of key[i] - key[u]? Is it negative? If True, assign ito $u$.
Step 2.2.5: Increment i by 1, and go to Step 2.2.1.
Step 2.3: Check if u equals -1 .
a. If True, go to Step 3.

Step 2.4: Set Mark[u] to 1.
Step 2.5: Set in_queue[u] to 0.
Step 2.6: Set v to 0.
Step 2.6.1: If $v$ is less than 4, go to Step 2.6.2. Otherwise, go to Step 2.6.
Step 2.6.2: Check if $\mathrm{A}[\mathrm{u}, \mathrm{v}]$ does not equal to 0 . If True, perform these sub-steps:
a. Check if (mark[v] equals 0 .
a.1. If True, then what are the values of $A[u, v]$ and key[v]? Check either (in_queue[v] equals 0 ) OR (A[u, $v]$ - key[v] is less than 0 ) is True.
i. If either is True, set pi[v] to $u$, and
ii. Set key[v] to $A[u, v]$, and
iii. Set in_queue[v] to 1 .

Step 2.6.3: Increment v by 1, and go to Step 2.6.1.
Step 2.7: Increment k by 1. If k < 4, go to Step 2.1. Otherwise, go to Step 3.
Step 3: Print the array of pi.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc., and remember, the next number of 59 is 60 ):

1. In Step 1, $\mathrm{k}=0$.
2. In Step 2.1, $u=-1$.
3. In Step 2.2, $i=0$.
4. In Step 2.2.1, i < 4, so go to Step 2.2.2.
5. In Step 2.2.2, in_queue[0] = 1, so go to Step 2.2.3.
6. In Step 2.2.3, $u=-1$, so assign $i$ to $u, u=0$.
7. In Step 2.2.5, increment $i$ by $1, i=1$.
8. In Step 2.2.1, i < 4, so go to Step 2.2.2.
9. In Step 2.2.2, in_queue[1] = 0, so go to Step 2.2.5.
10. In Step 2.2.5, increment $i$ by $1, i=2$.
11. In Step 2.2.1, i < 4, so go to Step 2.2.2.
12. In Step 2.2.2, in_queue[2] $=0$, so go to Step 2.2.5.
13. In Step 2.2.5, increment $i$ by $1, i=3$.
14. In Step 2.2.1, $i<4$, so go to Step 2.2.2.
15. In Step 2.2.2, in_queue[3] $=0$, so go to Step 2.2.5.
16. In Step 2.2.5, increment $i$ by $1, i=4$.
17. In Step 2.2.1, $i>=4$, so go to Step 2.3.
18. In Step 2.3, u!=-1, so go to Step 2.4.
19. In Step 2.4, Mark[0] = 1 .
20. In Step 2.5, in_queue[0] $=0$.
21. In Step 2.6, v=0.
22. In Step 2.6.1, v < 4, so go to Step 2.6.2.
23. In Step 2.6.2, $A[0,0]=0$, so go to Step 2.6.3.
24. In Step 2.6.3, increment $v$ by $1, v=1$.
25. In Step 2.6.1, v < 4, so go to Step 2.6.2.
26. In Step 2.6.2, $\mathrm{A}[0,1]$ ! $=0$, so perform sub-steps:
a. mark[1] $=0$, so perform sub-steps:
a.1. $A[0,1]=3$, key $[1]=0$, in_queue $[1]=0$, so perform sub-steps:
i. $\mathrm{pi}[1]=0$,
ii. $k e y[1]=3$,
iii. in_queue[1] = 1 .
27. In Step 2.6.3, increment $v$ by $1, v=2$.
28. In Step 2.6.1, v < 4, so go to Step 2.6.2.
29. In Step 2.6.2, A[0, 2] != 0, so perform sub-steps:
a. $\operatorname{mark}[2]=0$, so perform sub-steps:
a.1. $A[0,2]=5$, key $[2]=0$, in_queue[2] $=0$, so perform sub-steps:
i. $\mathrm{pi}[2]=0$,
ii. $\operatorname{key}[2]=5$,
iii. in_queue[2] $=1$.
30. In Step 2.6.3, increment v by $1, \mathrm{v}=3$.
31. In Step 2.6.1, $\mathrm{v}<4$, so go to Step 2.6.2.
32. In Step 2.6.2, $\mathrm{A}[0,3]$ ! $=0$, so perform sub-steps:
a. $\operatorname{mark}[3]=0$, so perform sub-steps:
a.1. $A[0,3]=4$, key $[3]=0$, in_queue $[3]=0$, so perform sub-steps:
i. $\mathrm{pi}[3]=0$,
ii. $\operatorname{key}[3]=4$,
iii. in_queue[3] $=1$.
33. In Step 2.6.3, increment v by 1, v=4.
34. In Step 2.6.1, $v>=4$, so go to Step 2.7.
35. In Step 2.7, increment k by $1, k=1, k<4$, so go to Step 2.1.
36. In Step 2.1, $u=-1$.
37. In Step 2.2, $i=0$.
38. In Step 2.2.1, i < 4, so go to Step 2.2.2.
39. In Step 2.2.2, in_queue[0] $=0$, so go to Step 2.2.5.
40. In Step 2.2.5, increment $i$ by $1, i=1$.
41. In Step 2.2.1, $i<4$, so go to Step 2.2.2.
42. In Step 2.2.2, in_queue[1] = 1, so go to Step 2.2.3.
43. In Step 2.2.3, $u=-1$, so assign $i$ to $u, u=1$.
44. In Step 2.2.5, increment $i$ by $1, i=2$.
45. In Step 2.2.1, i < 4, so go to Step 2.2.2.
46. In Step 2.2.2, in_queue[2] $=1$, so go to Step 2.2.4.
47. In Step 2.2.4, $\operatorname{key}[i]=5, \operatorname{key}[u]=3$, $\operatorname{key}[i]-\operatorname{key}[u]=2$, not negative, so go to Step 2.2.5 .
48. In Step 2.2.5, increment i by $1, i=3$.
49. In Step 2.2.1, $\mathrm{i}<4$, so go to Step 2.2.2.
50. In Step 2.2.2, in_queue[3] = 1, so go to Step 2.2.4.
51. In Step 2.2.4, $\operatorname{key}[i]=4, \operatorname{key}[u]=3, \operatorname{key}[i]-\operatorname{key}[u]=1$, not negative, so go to Step 2.2.5.
52. In Step 2.2.5, increment i by $1, i=4$.
53. In Step 2.2.1, i >=4, so go to Step 2.3.
54. In Step 2.3, u $!=-1$, so go to Step 2.4.
55. In Step 2.4, Mark[1] = 1.
56. In Step 2.5, in_queue[1] = 0 .
57. In Step 2.6, v=0.
58. In Step 2.6.1, v < 4, so go to Step 2.6.2.
59. In Step 2.6.2, A[1, 0] != 0, so perform sub-steps:
a. $\operatorname{mark}[0]=1$, so go to Step 2.6.3.
60. In Step 2.6.3, increment $v$ by $1, v=1$.
61. In Step 2.6.1, v < 4, so go to Step 2.6.2.
62. In Step 2.6.2, A[1, 1] $=0$, so go to Step 2.6.3.
63. In Step 2.6.3, increment $v$ by 1, $v=2$.
64. In Step 2.6.1, v < 4, so go to Step 2.6.2.
65. In Step 2.6.2, A[1, 2] != 0, so perform sub-steps:
a. mark[2] $=0$, so perform sub-steps:
a.1. A[1, 2] $=6$, $\operatorname{key[2]~}=5$, in_queue[2] $=1$, so go to Step 2.6.3.
66. In Step 2.6.3, increment $v$ by $1, v=3$.
67. In Step 2.6.1, v < 4, so go to Step 2.6.2.
68. In Step 2.6.2, $\mathrm{A}[1,3]=0$, so go to Step 2.6.3.
69. In Step 2.6.3, increment $v$ by $1, v=4$.
70. In Step 2.6.1, v >=4, so go to Step 2.7.
71. In Step 2.7, increment k by $1, \mathrm{k}=2, \mathrm{k}<4$, so go to Step 2.1.
72. In Step 2.1, $u=-1$.
73. In Step 2.2, $\mathbf{i}=0$.
74. In Step 2.2.1, i < 4, so go to Step 2.2.2.
75. In Step 2.2.2, in_queue[0] = 0 , so go to Step 2.2.5
76. In Step 2.2.5, increment i by $1, i=1$.
77. In Step 2.2.1, $\mathrm{i}<4$, so go to Step 2.2.2.
78. In Step 2.2.2, in_queue[1] $=0$, so go to Step 2.2.5
79. In Step 2.2.5, increment i by $1, i=2$.
80. In Step 2.2.1, i < 4, so go to Step 2.2.2.
81. In Step 2.2.2, in_queue[2] = 1, so go to Step 2.2.3.
82. In Step 2.2.3, $u=-1$, so assign it to $u, u=2$.
83. In Step 2.2.5, increment $i$ by $1, i=3$.
84. In Step 2.2.1, i < 4, so go to Step 2.2.2.
85. In Step 2.2.2, in_queue[3] = 1, so go to Step 2.2.4.
86. In Step 2.2.4, $\operatorname{key}[i]=4, \operatorname{key}[u]=5, \operatorname{key}[i]-\operatorname{key}[u]=-1$, negative, so assign $i$ to $u, u=3$.
87. In Step 2.2.5, increment i by $1, i=4$.
88. In Step 2.2.1, i >=4, so go to Step 2.3.
89. In Step 2.3, $u!=-1$, so go to Step 2.4.
90. In Step 2.4, Mark[3] = 1 .
91. In Step 2.5, in_queue[3] = 0 .
92. In Step 2.6, v=0.
93. In Step 2.6.1, v < 4, so go to Step 2.6.2.
94. In Step 2.6.2, A[3, 0] != 0, so perform sub-steps:
a. $\operatorname{mark}[0]=1$, so go to Step 2.6.3.
95. In Step 2.6.3, increment $v$ by $1, v=1$.
96. In Step 2.6.1, v < 4, so go to Step 2.6.2.
97. In Step 2.6.2, $\mathrm{A}[3,1]=0$, so go to Step 2.6.3.
98. In Step 2.6.3, increment $v$ by $1, v=2$.
99. In Step 2.6.1, v < 4, so go to Step 2.6.2.
100. In Step 2.6.2, $\mathrm{A}[3,2]$ ! $=0$, so perform sub-steps:
a. mark[2] $=0$, so perform sub-steps:
a.1. $A[3,2]=3$, key[2] $=5$, in_queue[2] $=1$, so perform sub-steps:
i. $\mathrm{pi}[2]=3$,
ii. $k e y[2]=3$,
```
            iii. in_queue[2] = 1.
101. In Step 2.6.3, increment v by 1, v=3.
102. In Step 2.6.1, v < 4, so go to Step 2.6.2.
103. In Step 2.6.2, A[3, 3] = 0, so go to Step 2.6.3.
104. In Step 2.6.3, increment v by 1, v=4.
105. In Step 2.6.1, v >= 4, so go to Step 2.7.
106. In Step 2.7, increment k by 1, k=3,k < 4, so go to Step 2.1.
107. In Step 2.1, u=-1.
108. In Step 2.2, i= 0.
109. In Step 2.2.1, i < 4, so go to Step 2.2.2.
110. In Step 2.2.2, in_queue[0] = 0, so go to Step 2.2.5.
111. In Step 2.2.5, increment i by 1, i=1.
112. In Step 2.2.1, i < 4, so go to Step 2.2.2.
113. In Step 2.2.2, in_queue[1] = 0, so go to Step 2.2.5.
114. In Step 2.2.5, increment i by 1, i=2.
115. In Step 2.2.1, i < 4, so go to Step 2.2.2.
116. In Step 2.2.2, in_queue[2] = 1, so go to Step 2.2.3.
117. In Step 2.2.3, u=-1, so assign i to u, u=2.
118. In Step 2.2.5, increment i by 1, i=3.
119. In Step 2.2.1, i < 4, so go to Step 2.2.2.
120. In Step 2.2.2, in_queue[3] = 0, so go to Step 2.2.5.
121. In Step 2.2.5, increment i by 1, i=4.
122. In Step 2.2.1, i >= 4, so go to Step 2.3.
123. In Step 2.3, u != -1, so go to Step 2.4.
124. In Step 2.4, Mark[2] = 1.
125. In Step 2.5, in_queue[2] = 0.
126. In Step 2.6, v=0.
127. In Step 2.6.1, v < 4, so go to Step 2.6.2.
128. In Step 2.6.2, A[2, 0] != 0, so perform sub-steps:
    a. mark[0] = 1, so go to Step 2.6.3
129. In Step 2.6.3, increment v by 1, v=1.
130. In Step 2.6.1, v < 4, so go to Step 2.6.2.
131. In Step 2.6.2, A[2, 1] != 0, so perform sub-steps:
    a. mark[1] = 1, so go to Step 2.6.3.
132. In Step 2.6.3, increment v by 1, v=2.
133. In Step 2.6.1, v < 4, so go to Step 2.6.2
134. In Step 2.6.2, A[2, 2] = 0, so go to Step 2.6.3.
135. In Step 2.6.3, increment v by 1, v=3.
136. In Step 2.6.1, v < 4, so go to Step 2.6.2.
137. In Step 2.6.2, A[2, 3] != 0, so perform sub-steps:
    a. mark[3] = 1, so go to Step 2.6.3
138. In Step 2.6.3, increment v by 1, v=4.
139. In Step 2.6.1, v >= 4, so go to Step 2.7.
140. In Step 2.7, increment k by 1,k=4,k>=4, so go to Step 3.
141. In Step 3, print the array of pi: pi[0] = 0, pi[1] = 0, pi[2] = 3, pi[3] = 0.
```

Table 28: The prompt of mst prim and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.
Initial: Set the adjacency matrix A with the size $4 \times 4$ :
$\mathrm{A}[0,0]=0, \mathrm{~A}[0,1]=0, \mathrm{~A}[0,2]=6, \mathrm{~A}[0,3]=6$
$A[1,0]=0, A[1,1]=0, A[1,2]=4, A[1,3]=0$
$A[2,0]=6, A[2,1]=4, A[2,2]=0, A[2,3]=3$
$A[3,0]=6, A[3,1]=0, A[3,2]=3, A[3,3]=0$,
where $\mathrm{N}=4$ is the number of vertices. Set the start vertex $\mathrm{s}=0$.
Set variables $d$ and mask as arrays of zeros with 4 elements:
$\mathrm{d}: \mathrm{d}[0]=0, \mathrm{~d}[1]=0, \mathrm{~d}[2]=0, \mathrm{~d}[3]=0$,
$\operatorname{mask}: \operatorname{mask}[0]=1, \operatorname{mask}[1]=0, \operatorname{mask}[2]=0, \operatorname{mask}[3]=0$,
Step 1: Make a copy of $d$ and mask named prev_d and prev_mask. Set the boolean variable all_equal to True.
Step 2: Set $U$ equal to 0 .
Step 2.1: If $U$ is less than 4, perform Step 2.2. Otherwise, go to Step 3.
Step 2.2: If and prev_mask[U] equals 1 , set $V$ equal to 0 . Otherwise, increment $U$ and return to Step 2.1.
Step 2.3: If V is less than 4, perform Step 2.4. Otherwise, return to Step 2 and increment U .
Step 2.4: Check if and $\mathrm{A}[\mathrm{U}, \mathrm{V}]$ is not 0 .
a. If True:
i. Calculate new_d by adding prev_d[U] and A[U, V].
ii. Calculate the difference between new_d and $d[V]$. Then, is it negative? Please check.
iii. If (mask[V] equals 0 ) or (the difference is negative):

- Update d[V] with the value of new_d.
- Set all_equal to False.
iv. Set mask[V] to 1.

Step 2.5: Increment V and return to Step 2.3.
Step 3: If all_equal is False, go back to Step 1; Otherwise, go to Step 4.
Step 4: Print the array d.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc., and remember, the next number of 59 is 60 ):

1. In Step 1, copy from d, prev_d is: prev_d[0] = 0, prev_d[1] = 0, prev_d[2] = 0, prev_d[3] = 0. Copy from mask, prev_mask is: prev_mask[0] = 1 , prev_mask[1] $=0$, prev_mask[2] $=0$, prev_mask[3] $=0$.
2. Set all_equal to True.
3. In Step 2, set $U=0$.
4. In Step 2.1, since $U(0)$ is less than 4, proceed to Step 2.2.
5. In Step 2.2, prev_mask[0] equals 1, so set $V=0$.
6. In Step 2.3, since $V(0)$ is less than 4, proceed to Step 2.4.
7. In Step 2.4, $\mathrm{A}[0,0]$ is 0 , so skip to Step 2.5.
8. In Step 2.5, increment $V$ to 1 and return to Step 2.3.
9. In Step 2.3, since $V(1)$ is less than 4, proceed to Step 2.4.
10. In Step 2.4, A[0, 1] is 0 , so skip to Step 2.5 .
11. In Step 2.5, increment V to 2 and return to Step 2.3.
12. In Step 2.3, since $V(2)$ is less than 4, proceed to Step 2.4.
13. In Step 2.4, $A[0,2]$ is not 0 (it is 6 ).
14. Calculate new_d: prev_d[0] $+\mathrm{A}[0,2]=0+6=6$.
15. Calculate the difference: new_d-d[2] $=6-0=6$, which is not negative.
16. Since mask[2] equals 0 , update $d[2]$ with the value of new_d (6) and set all_equal to False.
17. Set mask[2] to 1.
18. In Step 2.5, increment V to 3 and return to Step 2.3.
19. In Step 2.3, since $V(3)$ is less than 4, proceed to Step 2.4.
20. In Step 2.4, $\mathrm{A}[0,3]$ is not 0 (it is 6 ).
21. Calculate new_d: prev_d[0] $+\mathrm{A}[0,3]=0+6=6$.
22. Calculate the difference: new_d $-d[3]=6-0=6$, which is not negative.
23. Since mask[3] equals 0 , update $d[3]$ with the value of new_d (6) and set all_equal to False.
24. Set mask[3] to 1.
25. In Step 2.5, increment V to 4 and return to Step 2.3.
26. In Step 2.3, since $\mathrm{V}(4)$ is not less than 4, return to Step 2 and increment U .
27. In Step 2, set $U=1$.
28. In Step 2.1, since $U(1)$ is less than 4, proceed to Step 2.2.
29. In Step 2.2, prev_mask[1] equals 0 , so increment $U$ to 2 and return to Step 2.1.
30. In Step 2.1, since $U(2)$ is less than 4, proceed to Step 2.2.
31. In Step 2.2, prev_mask[2] equals 0, so increment $U$ to 3 and return to Step 2.1.
32. In Step 2.1, since $U(3)$ is less than 4, proceed to Step 2.2.
33. In Step 2.2, prev_mask[3] equals 0 , so increment $U$ to 4 and return to Step 2.1.
34. In Step 2.1, since $U(4)$ is not less than 4, proceed to Step 3.
35. In Step 3, since all_equal is False, go back to Step 1.
36. In Step 1, copy from d, prev_d is: prev_d[0] $=0$, prev_d[1] $=0$, prev_d[2] $=6$, prev_d[3] $=6$. Copy from mask, prev_mask is: prev_mask[0] = 1, prev_mask[1] = 0, prev_mask[2] = 1, prev_mask[3] = 1 .
37. Set all_equal to True.
38. In Step 2, set $U=0$.
39. In Step 2.1, since $U(0)$ is less than 4, proceed to Step 2.2.
40. In Step 2.2, prev_mask[0] equals 1 , so set $V=0$.
41. In Step 2.3, since $V(0)$ is less than 4, proceed to Step 2.4.
42. In Step 2.4, A[0, 0] is 0 , so skip to Step 2.5.
43. In Step 2.5, increment V to 1 and return to Step 2.3.
44. In Step 2.3, since $V(1)$ is less than 4, proceed to Step 2.4.
45. In Step 2.4, A[0, 1] is 0 , so skip to Step 2.5.
46. In Step 2.5, increment V to 2 and return to Step 2.3.
47. In Step 2.3, since $V(2)$ is less than 4, proceed to Step 2.4.
48. In Step 2.4, $\mathrm{A}[0,2]$ is not 0 (it is 6 ).
49. Calculate new_d: prev_d $[0]+\mathrm{A}[0,2]=0+6=6$.
50. Calculate the difference: new_d-d[2] $=6-6=0$, which is not negative.
51. Since mask[2] equals 1 and the difference is not negative, skip to Step 2.5.
52. In Step 2.5, increment $V$ to 3 and return to Step 2.3.
53. In Step 2.3, since V (3) is less than 4, proceed to Step 2.4.
54. In Step 2.4, $\mathrm{A}[0,3]$ is not 0 (it is 6 ).
55. Calculate new_d: prev_d $[0]+\mathrm{A}[0,3]=0+6=6$.
56. Calculate the difference: new_d $-\mathrm{d}[3]=6-6=0$, which is not negative.
57. Since mask[3] equals 1 and the difference is not negative, skip to Step 2.5.
58. In Step 2.5, increment V to 4 and return to Step 2.3.
59. In Step 2.3, since $V(4)$ is not less than 4, return to Step 2 and increment $U$.
60. In Step 2, set $U=1$.
61. In Step 2.1, since $U(1)$ is less than 4, proceed to Step 2.2.
62. In Step 2.2, prev_mask[1] equals 0 , so increment $U$ to 2 and return to Step 2.1.
63. In Step 2.1, since $U(2)$ is less than 4, proceed to Step 2.2.
64. In Step 2.2, prev_mask[2] equals 1 , so set $V=0$.
65. In Step 2.3, since $V(0)$ is less than 4, proceed to Step 2.4.
66. In Step 2.4, A[2, 0] is not 0 (it is 6 ).
67. Calculate new_d: prev_d[2] $+\mathrm{A}[2,0]=6+6=12$.
68. Calculate the difference: new_d-d[0]=12-0=12, which is not negative.
69. Since mask[0] equals 1 and the difference is not negative, skip to Step 2.5.
70. In Step 2.5, increment $V$ to 1 and return to Step 2.3.
71. In Step 2.3, since V (1) is less than 4, proceed to Step 2.4.
72. In Step 2.4, A[2, 1] is not 0 (it is 4).
73. Calculate new_d: prev_d[2] $+\mathrm{A}[2,1]=6+4=10$.
74. Calculate the difference: new_d $-\mathrm{d}[1]=10-0=10$, which is not negative.
75. Since mask[1] equals 0 , update $d[1]$ with the value of new_d (10) and set all_equal to False.
76. Set mask[1] to 1.
77. In Step 2.5, increment V to 2 and return to Step 2.3.
78. In Step 2.3, since V (2) is less than 4, proceed to Step 2.4.
79. In Step 2.4, $\mathrm{A}[2,2]$ is 0 , so skip to Step 2.5.
80. In Step 2.5, increment V to 3 and return to Step 2.3.
81. In Step 2.3, since V (3) is less than 4, proceed to Step 2.4.
82. In Step 2.4, $\mathrm{A}[2,3]$ is not 0 (it is 3 ).
83. Calculate new_d: prev_d[2] $+\mathrm{A}[2,3]=6+3=9$.
84. Calculate the difference: new_d-d[3]=9-6=3, which is not negative.
85. Since mask[3] equals 1 and the difference is not negative, skip to Step 2.5.
86. In Step 2.5, increment $\vee$ to 4 and return to Step 2.3.
87. In Step 2.3, since $\mathrm{V}(4)$ is not less than 4, return to Step 2 and increment U .
88. In Step 2, set $U=3$.
89. In Step 2.1, since $U(3)$ is less than 4, proceed to Step 2.2.
90. In Step 2.2, prev_mask[3] equals 1 , so set $\mathrm{V}=0$.
91. In Step 2.3, since $V(0)$ is less than 4, proceed to Step 2.4.
```
92. In Step 2.4, \(\mathrm{A}[3,0]\) is not 0 (it is 6 ).
93. Calculate new_d: prev_d[3] \(+\mathrm{A}[3,0]=6+6=12\).
94. Calculate the difference: new_d-d[0]=12-0=12, which is not negative.
95. Since mask[0] equals 1 and the difference is not negative, skip to Step 2.5.
96. In Step 2.5, increment \(V\) to 1 and return to Step 2.3.
97. In Step 2.3, since \(V(1)\) is less than 4, proceed to Step 2.4.
98. In Step 2.4, \(A[3,1]\) is 0 , so skip to Step 2.5.
99. In Step 2.5, increment V to 2 and return to Step 2.3.
100. In Step 2.3, since \(V(2)\) is less than 4, proceed to Step 2.4.
101. In Step 2.4, \(A[3,2]\) is not 0 (it is 3 ).
102. Calculate new_d: prev_d[3] \(+\mathrm{A}[3,2]=6+3=9\).
103. Calculate the difference: new_d-d[2] \(=9-6=3\), which is not negative.
104. Since mask[2] equals 1 and the difference is not negative, skip to Step 2.5.
105. In Step 2.5, increment \(V\) to 3 and return to Step 2.3.
106. In Step 2.3, since V (3) is less than 4, proceed to Step 2.4.
107. In Step 2.4, \(\mathrm{A}[3,3]\) is 0 , so skip to Step 2.5.
108. In Step 2.5, increment \(V\) to 4 and return to Step 2.3.
109. In Step 2.3, since \(V(4)\) is not less than 4, return to Step 2 and increment \(U\).
110. In Step 2, set \(U=4\).
111. In Step 2.1, since \(U(4)\) is not less than 4, proceed to Step 3.
112. In Step 3, since all_equal is False, go back to Step 1.
113. In Step 1, copy from d, prev_d is: prev_d[0] = 0, prev_d[1] = 10, prev_d[2] = 6, prev_d[3] \(=6\). Copy from
mask, prev_mask is: prev_mask[0] = 1 , prev_mask[1] = 1, prev_mask[2] = 1 , prev_mask[3] = 1 .
114. Set all_equal to True.
115. In Step 2, set \(U=0\).
116. In Step 2.1, since \(U(0)\) is less than 4, proceed to Step 2.2.
117. In Step 2.2, prev_mask[0] equals 1 , so set \(\mathrm{V}=0\).
118. In Step 2.3, since \(V(0)\) is less than 4, proceed to Step 2.4.
119. In Step 2.4, A[0, 0] is 0 , so skip to Step 2.5.
120. In Step 2.5, increment V to 1 and return to Step 2.3.
121. In Step 2.3, since \(V(1)\) is less than 4, proceed to Step 2.4.
122. In Step 2.4, \(\mathrm{A}[0,1]\) is 0 , so skip to Step 2.5.
123. In Step 2.5, increment \(V\) to 2 and return to Step 2.3.
124. In Step 2.3, since \(V(2)\) is less than 4, proceed to Step 2.4.
125. In Step 2.4, \(\mathrm{A}[0,2]\) is not 0 (it is 6 ).
126. Calculate new_d: prev_d[0] \(\mathrm{A}[0,2]=0+6=6\).
127. Calculate the difference: new_d-d[2] \(=6-6=0\), which is not negative.
128. Since mask[2] equals 1 and the difference is not negative, skip to Step 2.5.
129. In Step 2.5, increment \(V\) to 3 and return to Step 2.3.
130. In Step 2.3, since \(V(3)\) is less than 4, proceed to Step 2.4.
131. In Step 2.4, \(\mathrm{A}[0,3]\) is not 0 (it is 6 ).
132. Calculate new_d: prev_d[0] \(+\mathrm{A}[0,3]=0+6=6\).
133. Calculate the difference: new_d-d[3]=6-6=0, which is not negative.
134. Since mask[3] equals 1 and the difference is not negative, skip to Step 2.5.
135. In Step 2.5, increment \(V\) to 4 and return to Step 2.3.
136. In Step 2.3, since \(V(4)\) is not less than 4, return to Step 2 and increment \(U\).
137. In Step 2, set \(U=1\).
138. In Step 2.1, since \(U(1)\) is less than 4, proceed to Step 2.2.
139. In Step 2.2, prev_mask[1] equals 1 , so set \(V=0\).
140. In Step 2.3, since \(V(0)\) is less than 4, proceed to Step 2.4.
141. In Step 2.4, \(\mathrm{A}[1,0]\) is 0 , so skip to Step 2.5.
142. In Step 2.5, increment \(V\) to 1 and return to Step 2.3.
143. In Step 2.3, since \(V(1)\) is less than 4, proceed to Step 2.4.
144. In Step 2.4, \(\mathrm{A}[1,1]\) is 0 , so skip to Step 2.5.
145. In Step 2.5, increment \(V\) to 2 and return to Step 2.3.
146. In Step 2.3, since \(V(2)\) is less than 4, proceed to Step 2.4.
147. In Step 2.4, A[1, 2] is not 0 (it is 4).
148. Calculate new_d: prev_d[1] \(+\mathrm{A}[1,2]=10+4=14\).
149. Calculate the difference: new_d-d[2] = 14-6=8, which is not negative.
150. Since mask[2] equals 1 and the difference is not negative, skip to Step 2.5.
151. In Step 2.5, increment \(V\) to 3 and return to Step 2.3.
152. In Step 2.3, since \(V(3)\) is less than 4, proceed to Step 2.4.
153. In Step 2.4, A[1, 3] is 0 , so skip to Step 2.5.
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154. In Step 2.5, increment V to 4 and return to Step 2.3.
155. In Step 2.3, since V (4) is not less than 4, return to Step 2 and increment U.
156. In Step 2, set U=2.
157. In Step 2.1, since U(2) is less than 4, proceed to Step 2.2.
158. In Step 2.2, prev_mask[2] equals 1, so set V = 0.
159. In Step 2.3, since V (0) is less than 4, proceed to Step 2.4.
160. In Step 2.4, A[2, 0] is not 0 (it is 6).
161. Calculate new_d: prev_d[2] + A[2, 0] = 6 + 6 = 12.
162. Calculate the difference: new_d-d[0] = 12-0=12, which is not negative.
163. Since mask[0] equals }1\mathrm{ and the difference is not negative, skip to Step 2.5.
164. In Step 2.5, increment V to }1\mathrm{ and return to Step 2.3.
165. In Step 2.3, since V (1) is less than 4, proceed to Step 2.4.
166. In Step 2.4, A[2, 1] is not 0 (it is 4).
167. Calculate new_d: prev_d[2] + A[2, 1] = 6 + 4 = 10.
168. Calculate the difference: new_d-d[1] = 10-10=0, which is not negative.
169. Since mask[1] equals }1\mathrm{ and the difference is not negative, skip to Step 2.5.
170. In Step 2.5, increment V to 2 and return to Step 2.3.
171. In Step 2.3, since V (2) is less than 4, proceed to Step 2.4.
172. In Step 2.4, A[2, 2] is 0, so skip to Step 2.5.
173. In Step 2.5, increment V to 3 and return to Step 2.3.
174. In Step 2.3, since V (3) is less than 4, proceed to Step 2.4.
175. In Step 2.4, A[2, 3] is not 0 (it is 3).
176. Calculate new_d: prev_d[2] + A[2, 3] =6 + 3 = 9.
177. Calculate the difference: new_d-d[3] =9-6 = 3, which is not negative.
178. Since mask[3] equals }1\mathrm{ and the difference is not negative, skip to Step 2.5.
179. In Step 2.5, increment V to 4 and return to Step 2.3.
180. In Step 2.3, since V (4) is not less than 4, return to Step 2 and increment U.
181. In Step 2, set U = 3.
182. In Step 2.1, since U(3) is less than 4, proceed to Step 2.2.
183. In Step 2.2, prev_mask[3] equals 1, so set V=0.
184. In Step 2.3, since V (0) is less than 4, proceed to Step 2.4.
185. In Step 2.4, A[3, 0] is not 0 (it is 6).
186. Calculate new_d: prev_d[3] + A[3, 0] = 6+6 = 12.
187. Calculate the difference: new_d-d[0] = 12-0=12, which is not negative.
188. Since mask[0] equals }1\mathrm{ and the difference is not negative, skip to Step 2.5.
189. In Step 2.5, increment V to }1\mathrm{ and return to Step 2.3.
190. In Step 2.3, since V (1) is less than 4, proceed to Step 2.4.
191. In Step 2.4, A[3, 1] is 0, so skip to Step 2.5.
192. In Step 2.5, increment V to 2 and return to Step 2.3.
193. In Step 2.3, since V (2) is less than 4, proceed to Step 2.4.
194. In Step 2.4, A[3, 2] is not 0 (it is 3).
195. Calculate new_d: prev_d[3] + A[3, 2] = 6 + 3 = 9.
196. Calculate the difference: new_d-d[2] = 9-6 = 3, which is not negative.
197. Since mask[2] equals }1\mathrm{ and the difference is not negative, skip to Step 2.5.
198. In Step 2.5, increment V to 3 and return to Step 2.3.
199. In Step 2.3, since V (3) is less than 4, proceed to Step 2.4.
200. In Step 2.4, A[3, 3] is 0, so skip to Step 2.5.
201. In Step 2.5, increment V to 4 and return to Step 2.3.
202. In Step 2.3, since V (4) is not less than 4, return to Step 2 and increment U.
203. In Step 2, set U=4.
204. In Step 2.1, since U (4) is not less than 4, proceed to Step 3.
205. In Step 3, since all_equal is True, proceed to Step 4.
206. In Step 4, print the array d: d[0] = 0,d[1] = 10, d[2] = 6, d[3] = 6.
```

Table 29: The prompt of bellman ford and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the adjacency matrix A with the size $4 \times 4$ :
$\mathrm{A}[0,0]=0, \mathrm{~A}[0,1]=0, \mathrm{~A}[0,2]=5, \mathrm{~A}[0,3]=4$
$A[1,0]=0, A[1,1]=0, A[1,2]=6, A[1,3]=5$
$A[2,0]=5, A[2,1]=6, A[2,2]=0, A[2,3]=4$
$A[3,0]=4, A[3,1]=5, A[3,2]=4, A[3,3]=0$,
where $N=4$ is the number of vertices. Set the start vertex $s=0$.
Set variables d, mark, and in_queue as arrays of zeros with 4 elements:
$d: d[0]=0, d[1]=0, d[2]=0, d[3]=0$,
mark: $\operatorname{mark}[0]=0, \operatorname{mark}[1]=0, \operatorname{mark}[2]=0, \operatorname{mark}[3]=0$,
in_queue: in_queue[0] = 1 , in_queue[1] = 0 , in_queue[2] = 0 , in_queue[3] = 0 .
Step 1: Assign k to 0.
Step 2.1: Assign u to -1.
Step 2.2: Assign i to 0.
Step 2.2.1: If i is less than 4, go to Step 2.2.2. Otherwise, go to Step 2.3.
Step 2.2.2: Check if in_queue[i] equals 1. If True, go to Step 2.2.3.
Step 2.2.3: Check if $u$ equals -1 . If True, assign $i$ to $u$. Then, go to Step 2.2.5.
Step 2.2.4: What are the value of $d[i]$ and $d[u]$ ? Then, what is the result of $d[i]-d[u]$ ? Is it negative? If True, assign ito $u$.
Step 2.2.5: Increment i by 1, and go to Step 2.2.1.
Step 2.3: Check if u equals -1 .
a. If True, go to Step 3.

Step 2.4: Set mark[u] to 1.
Step 2.5: Set in_queue[u] to 0.
Step 2.6: Assign v to 0 .
Step 2.6.1: If $v$ is less than 4 , go to Step 2.6.2. Otherwise, go to Step 2.7.
Step 2.6.2: Check if $\mathrm{A}[\mathrm{u}, \mathrm{v}]$ does not equal to 0 . If True, perform these sub-steps:
a. Calculate new_d by adding d[u] and A[u,v].
b. Calculate the difference between new_d and $\mathrm{d}[\mathrm{v}]$. Then, is it negative?
c. Check if mark[v] equals 0 . If True, then what are the values of in_queue[v]? Check (in_queue[v] equals

0 ) OR (the difference is less than 0 ) is True.
i. If either is True, set $d[v]$ to the value of new_d, and
ii. Set in_queue[v] to 1.

Step 2.6.3: Increment v by 1, and go to Step 2.6.1.
Step 2.7: Increment k by 1. If k < 4, go to Step 2.1. Otherwise, go to Step 3.
Step 3: Print the array of d .
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. In Step 1, $\mathrm{k}=0$.
2. In Step 2.1, $\mathrm{u}=-1$.
3. In Step 2.2, $i=0$.
4. In Step 2.2.1, i < 4, so go to Step 2.2.2.
5. In Step 2.2.2, in_queue[0] = 1, so go to Step 2.2.3.
6. In Step 2.2.3, $u=-1$, so assign ito $u, u=0$.
7. In Step 2.2.5, increment $i$ by $1, i=1$.
8. In Step 2.2.1, i < 4, so go to Step 2.2.2.
9. In Step 2.2.2, in_queue[1] = 0, so go to Step 2.2.5.
10. In Step 2.2.5, increment $i$ by $1, i=2$.
11. In Step 2.2.1, i < 4, so go to Step 2.2.2.
12. In Step 2.2.2, in_queue[2] $=0$, so go to Step 2.2.5
13. In Step 2.2.5, increment i by $1, i=3$.
14. In Step 2.2.1, i < 4, so go to Step 2.2.2.
15. In Step 2.2.2, in_queue[3] $=0$, so go to Step 2.2.5
16. In Step 2.2.5, increment i by $1, i=4$.
17. In Step 2.2.1, i >=4, so go to Step 2.3.
18. In Step 2.3, u !=-1, so go to Step 2.4.
19. In Step 2.4, set mark[0] $=1$.
20. In Step 2.5, set in_queue[0] $=0$.
21. In Step 2.6, v=0.
22. In Step 2.6.1, v < 4, so go to Step 2.6.2.
23. In Step 2.6.2, $\mathrm{A}[0,0]=0$, so go to Step 2.6.3.
24. In Step 2.6.3, increment v by $1, v=1$.
25. In Step 2.6.1, $\mathrm{v}<4$, so go to Step 2.6.2.
26. In Step 2.6.2, $\mathrm{A}[0,1]=0$, so go to Step 2.6.3.
27. In Step 2.6.3, increment v by 1, v=2.
28. In Step 2.6.1, v < 4, so go to Step 2.6.2.
29. In Step 2.6.2, $A[0,2]=5$, so perform sub-steps:
a. new_d $=d[0]+A[0,2]=0+5=5$.
b. new_d $-d[2]=5-0=5$, which is not negative.
c. $\operatorname{mark}[2]=0$, in_queue[2] $=0$, so set d[2] $=5$ and in_queue[2] $=1$.
30. In Step 2.6.3, increment $v$ by $1, v=3$.
31. In Step 2.6.1, $\mathrm{v}<4$, so go to Step 2.6.2.
32. In Step 2.6.2, $\mathrm{A}[0,3]=3$, so perform sub-steps:
a. new_d $=d[0]+A[0,3]=0+3=3$.
b. new_d $-d[3]=3-0=3$, which is not negative.
c. $\operatorname{mark}[3]=0$, in_queue[3] $=0$, so set $\mathrm{d}[3]=3$ and in_queue $[3]=1$.
33. In Step 2.6.3, increment $v$ by 1, $v=4$.
34. In Step 2.6.1, v>=4, so go to Step 2.7.
35. In Step 2.7, increment k by $1, \mathrm{k}=1$.
36. In Step 2.1, $u=-1$.
37. In Step 2.2, $i=0$.
38. In Step 2.2.1, i < 4, so go to Step 2.2.2.
39. In Step 2.2.2, in_queue[0] $=0$, so go to Step 2.2.5.
40. In Step 2.2.5, increment $i$ by $1, i=1$.
41. In Step 2.2.1, i < 4, so go to Step 2.2.2.
42. In Step 2.2.2, in_queue[1] $=0$, so go to Step 2.2.5.
43. In Step 2.2.5, increment $i$ by $1, i=2$.
44. In Step 2.2.1, $i<4$, so go to Step 2.2.2.
45. In Step 2.2.2, in_queue[2] $=1$, so go to Step 2.2.3.
46. In Step 2.2.3, $u=-1$, so assign $i$ to $u, u=2$.
47. In Step 2.2.5, increment $i$ by $1, i=3$.
48. In Step 2.2.1, i < 4, so go to Step 2.2.2.
49. In Step 2.2.2, in_queue[3] $=1$, so go to Step 2.2.4.
50. In Step 2.2.4, $d[i]=3, d[u]=5, d[i]-d[u]=-2$, which is negative, so assign $i$ to $u, u=3$.
51. In Step 2.2.5, increment i by $1, i=4$.
52. In Step 2.2.1, i >=4, so go to Step 2.3.
53. In Step 2.3, u!=-1, so go to Step 2.4.
54. In Step 2.4, set mark[3] = 1 .
55. In Step 2.5, set in_queue[3] $=0$.
56. In Step 2.6, $v=0$.
57. In Step 2.6.1, v < 4, so go to Step 2.6.2.
58. In Step 2.6.2, $\mathrm{A}[3,0]=3$, so perform sub-steps:
a. new_d $=d[3]+A[3,0]=3+3=6$.
b. new_d $-d[0]=6-0=6$, which is not negative.
c. $\operatorname{mark}[0]=1$, in_queue $[0]=0$, so go to Step 2.6.3.
59. In Step 2.6.3, increment $v$ by $1, v=1$.
60. In Step 2.6.1, v < 4, so go to Step 2.6.2.
61. In Step 2.6.2, $A[3,1]=6$, so perform sub-steps:
a. new_d $=d[3]+A[3,1]=3+6=9$.
b. new_d $-d[1]=9-0=9$, which is not negative.
c. $\operatorname{mark}[1]=0$, in_queue[1] $=0$, so set d[1] = 9 and in_queue[1] $=1$.
62. In Step 2.6.3, increment v by $1, \mathrm{v}=2$.
63. In Step 2.6.1, v < 4, so go to Step 2.6.2.
64. In Step 2.6.2, A[3, 2] $=5$, so perform sub-steps:
a. new_d $=d[3]+A[3,2]=3+5=8$.
b. new_d $-d[2]=8-5=3$, which is not negative.
c. $\operatorname{mark}[2]=0$, in_queue[2] $=1$, so go to Step 2.6.3.
65. In Step 2.6.3, increment $v$ by $1, v=3$.
66. In Step 2.6.1, v < 4, so go to Step 2.6.2.
67. In Step 2.6.2, $A[3,3]=0$, so go to Step 2.6.3.
68. In Step 2.6.3, increment $v$ by $1, v=4$.
69. In Step 2.6.1, v >=4, so go to Step 2.7.
70. In Step 2.7, increment k by $1, \mathrm{k}=2$.
```
71. In Step 2.1, u=-1.
72. In Step 2.2, i= 0.
73. In Step 2.2.1, i < 4, so go to Step 2.2.2.
74. In Step 2.2.2, in_queue[0] = 0, so go to Step 2.2.5.
75. In Step 2.2.5, increment i by 1, i=1.
76. In Step 2.2.1, i < 4, so go to Step 2.2.2.
77. In Step 2.2.2, in_queue[1] = 1, so go to Step 2.2.3.
78. In Step 2.2.3, u=-1, so assign i to }\textrm{u},\textrm{u}=1\mathrm{ .
79. In Step 2.2.5, increment i by 1, i=2.
80. In Step 2.2.1, i < 4, so go to Step 2.2.2.
81. In Step 2.2.2, in_queue[2] = 1, so go to Step 2.2.4.
82. In Step 2.2.4, d[i] = 5, d[u] = 9, d[i] - d[u] = -4, which is negative, so assign i to u,u=2.
83. In Step 2.2.5, increment i by 1,i=3.
84. In Step 2.2.1, i < 4, so go to Step 2.2.2.
85. In Step 2.2.2, in_queue[3] = 0, so go to Step 2.2.5.
86. In Step 2.2.5, increment i by 1, i=4.
87. In Step 2.2.1, i >= 4, so go to Step 2.3.
88. In Step 2.3, u != -1, so go to Step 2.4.
89. In Step 2.4, set mark[2] = 1.
90. In Step 2.5, set in_queue[2] = 0.
91. In Step 2.6, v=0.
92. In Step 2.6.1, v < 4, so go to Step 2.6.2.
93. In Step 2.6.2, A[2, 0] = 5, so perform sub-steps:
    a. new_d=d[2] + A[2, 0] = 5 + 5 = 10.
    b. new_d -d[0] = 10-0 = 10, which is not negative.
    c. mark[0] = 1, in_queue[0] = 0, so go to Step 2.6.3.
94. In Step 2.6.3, increment v by 1, v=1.
95. In Step 2.6.1, v < 4, so go to Step 2.6.2.
96. In Step 2.6.2, A[2, 1] = 0, so go to Step 2.6.3.
97. In Step 2.6.3, increment v by 1, v=2.
98. In Step 2.6.1, v < 4, so go to Step 2.6.2.
99. In Step 2.6.2, A[2, 2] = 0, so go to Step 2.6.3.
100. In Step 2.6.3, increment v by 1, v=3.
101. In Step 2.6.1, v < 4, so go to Step 2.6.2.
102. In Step 2.6.2, A[2, 3] = 5, so perform sub-steps:
    a. new_d=d[2] + A[2, 3] = 5 + 5 = 10.
    b. new_d-d[3] = 10-3=7, which is not negative.
    c. mark[3] = 1, in_queue[3] = 0, so go to Step 2.6.3.
103. In Step 2.6.3, increment v by 1, v=4.
104. In Step 2.6.1, v >= 4, so go to Step 2.7.
105. In Step 2.7, increment k by 1,k=3.
106. In Step 2.1, u=-1.
107. In Step 2.2, i= 0.
108. In Step 2.2.1, i < 4, so go to Step 2.2.2.
109. In Step 2.2.2, in_queue[0] = 0, so go to Step 2.2.5.
110. In Step 2.2.5, increment i by 1, i=1.
111. In Step 2.2.1, i < 4, so go to Step 2.2.2.
112. In Step 2.2.2, in_queue[1] = 1, so go to Step 2.2.3.
113. In Step 2.2.3, u=-1, so assign i to }u,u=1\mathrm{ .
114. In Step 2.2.5, increment i by 1, i=2.
115. In Step 2.2.1, i < 4, so go to Step 2.2.2.
116. In Step 2.2.2, in_queue[2] = 0, so go to Step 2.2.5
117. In Step 2.2.5, increment i by 1, i=3.
118. In Step 2.2.1, i < 4, so go to Step 2.2.2.
119. In Step 2.2.2, in_queue[3] = 0, so go to Step 2.2.5.
120. In Step 2.2.5, increment i by 1, i=4.
121. In Step 2.2.1, i >= 4, so go to Step 2.3.
122. In Step 2.3, u != -1, so go to Step 2.4.
123. In Step 2.4, set mark[1] = 1.
```

```
124. In Step 2.5, set in_queue[1] = 0.
125. In Step 2.6, v=0.
126. In Step 2.6.1, v < 4, so go to Step 2.6.2.
127. In Step 2.6.2, A[1, 0] = 0, so go to Step 2.6.3.
128. In Step 2.6.3, increment v by 1, v=1.
129. In Step 2.6.1, v < 4, so go to Step 2.6.2.
130. In Step 2.6.2, A[1, 1] = 0, so go to Step 2.6.3.
131. In Step 2.6.3, increment v by 1, v=2.
132. In Step 2.6.1, v < 4, so go to Step 2.6.2.
133. In Step 2.6.2, A[1, 2] = 0, so go to Step 2.6.3.
134. In Step 2.6.3, increment v by 1, v=3.
135. In Step 2.6.1, v < 4, so go to Step 2.6.2.
136. In Step 2.6.2, A[1, 3] = 6, so perform sub-steps:
    a. new_d=d[1] + A[1, 3] = 9 + 6=15.
    b. new_d-d[3]=15-3=12, which is not negative.
    c. mark[3] = 1, in_queue[3] = 0, so go to Step 2.6.3.
137. In Step 2.6.3, increment v by 1, v=4.
138. In Step 2.6.1, v >= 4, so go to Step 2.7.
139. In Step 2.7, increment k by 1, k=4.
140. In Step 3, print the array of d: [0, 9, 5, 3].
```

Table 30: The prompt of dijkstra and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating a matrix at some index, use concrete values rather than just variables.
Initial: Set the distance matrix dist with the size $4 \times 4$ :
$\operatorname{dist}[0,0]=0, \operatorname{dist}[0,1]=3, \operatorname{dist}[0,2]=6, \operatorname{dist}[0,3]=2$
$\operatorname{dist}[1,0]=4, \operatorname{dist}[1,1]=0, \operatorname{dist}[1,2]=3, \operatorname{dist}[1,3]=6$
$\operatorname{dist}[2,0]=6, \operatorname{dist}[2,1]=2, \operatorname{dist}[2,2]=0, \operatorname{dist}[2,3]=3$
$\operatorname{dist}[3,0]=5, \operatorname{dist}[3,1]=1, \operatorname{dist}[3,2]=4, \operatorname{dist}[3,3]=0$,
where $V=4$ is the number of vertices.
Step 1: Set k equal to 0.
Step 1.1: If k < 4, perform Step 2. Otherwise, go to Step 4.
Step 2: Set i equal to 0.
Step 2.1: If i < 4, perform Step 2.2. Otherwise, go to Step 1 and increment k.
Step 2.2: Compute i-k and check if it's non-zero. If True, perform Step 3. Otherwise, go to Step 2 and increment i .
Step 3: Set $j$ equal to 0.
Step 3.1: If j < 4, perform Step 3.2. Otherwise, go to Step 2 and increment i .
Step 3.2: Compute j - k and check if it's non-zero:
a. If True, Compute j-i and check if it's non-zero:
i. If True, perform Step 3.3.
i. If False, go to Step 3 and increment $j$.
b. If False, go to Step 3 and increment j.

Step 3.2.1: If True, perform Step 3.3. Otherwise, go to Step 3 and increment j.
Step 3.3.1: Calculate dist_k as dist[i, k] + dist[k, j].
Step 3.3.2: Set dist[i, j] as min(dist[i, j], dist_k).
Step 3.4: Increment j and return to Step 3.1.
Step 4: Print the distance matrix dist by iterating over its elements, displaying each value as "dist[i, j$]=$ dist ij ".
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Step $1, \mathrm{k}=0$.
2. Step 1.1, k < 4, so proceed to Step 2.
3. Step 2, $i=0$.
4. Step 2.1, i < 4, so proceed to Step 2.2.
5. Step 2.2, $\mathrm{i}-\mathrm{k}=0$, so increment i and return to Step 2.1.
6. Step 2.1, $i=1, i<4$, so proceed to Step 2.2.
7. Step 2.2, $i-k=1$, so proceed to Step 3.
8. Step 3, j = 0 .

## 9. Step 3.1, j < 4, so proceed to Step 3.2.

10. Step 3.2, $\mathrm{j}-\mathrm{k}=0$, so increment j and return to Step 3.1.
11. Step 3.1, $\mathrm{j}=1, \mathrm{j}<4$, so proceed to Step 3.2.
12. Step 3.2, $j-k=1$, so proceed to Step 3.2.1.
13. Step 3.2.1, $\mathrm{j}-\mathrm{i}=0$, so increment j and return to Step 3.1.
14. Step 3.1, $\mathrm{j}=2, \mathrm{j}<4$, so proceed to Step 3.2.
15. Step 3.2, $\mathrm{j}-\mathrm{k}=2$, so proceed to Step 3.2.1.
16. Step 3.2.1, j-i=1, so proceed to Step 3.3.
17. Step 3.3.1, dist_k $=\operatorname{dist}[1,0]+\operatorname{dist}[0,2]=4+6=10$.
18. Step 3.3.2, dist[1, 2] $=\min (\operatorname{dist}[1,2]$, dist_k $)=\min (3,10)=3$.
19. Step 3.4, increment $j$ and return to Step 3.1.
20. Step 3.1, $\mathrm{j}=3, \mathrm{j}<4$, so proceed to Step 3.2.
21. Step 3.2, $j-k=3$, so proceed to Step 3.2.1.
22. Step 3.2.1, j - i = 2, so proceed to Step 3.3.
23. Step 3.3.1, dist_k $=\operatorname{dist}[1,0]+\operatorname{dist}[0,3]=4+2=6$.
24. Step 3.3.2, dist[1, 3] $=\min (\operatorname{dist}[1,3]$, dist_k) $=\min (6,6)=6$.
25. Step 3.4, increment $j$ and return to Step 3.1.
26. Step 3.1, $j=4, j>=4$, so increment $i$ and return to Step 2.1.
27. Step 2.1, $i=2, i<4$, so proceed to Step 2.2.
28. Step 2.2, $i-k=2$, so proceed to Step 3.
29. Step $3, \mathrm{j}=0$.
30. Step 3.1, j < 4, so proceed to Step 3.2.
31. Step 3.2, $\mathrm{j}-\mathrm{k}=0$, so increment j and return to Step 3.1.
32. Step 3.1, $\mathrm{j}=1, \mathrm{j}<4$, so proceed to Step 3.2.
33. Step 3.2, $\mathrm{j}-\mathrm{k}=1$, so proceed to Step 3.2.1.
34. Step 3.2.1, $\mathrm{j}-\mathrm{i}=-1$, so proceed to Step 3.3.
35. Step 3.3.1, dist_k $=\operatorname{dist}[2,0]+\operatorname{dist}[0,1]=6+3=9$.
36. Step 3.3.2, dist[2, 1] $=\min \left(\operatorname{dist[2,1],~dist\_ k)~}=\min (2,9)=2\right.$.
37. Step 3.4, increment $j$ and return to Step 3.1.
38. Step 3.1, $\mathbf{j}=2, \mathrm{j}<4$, so proceed to Step 3.2.
39. Step 3.2, $\mathrm{j}-\mathrm{k}=2$, so proceed to Step 3.2.1.
40. Step 3.2.1, $j-i=0$, so increment $j$ and return to Step 3.1.
41. Step 3.1, $\mathrm{j}=3, \mathrm{j}<4$, so proceed to Step 3.2.
42. Step 3.2, $\mathrm{j}-\mathrm{k}=3$, so proceed to Step 3.2.1.
43. Step 3.2.1, j - i = 1, so proceed to Step 3.3.
44. Step 3.3.1, dist_k $=\operatorname{dist}[2,0]+\operatorname{dist}[0,3]=6+2=8$.
45. Step 3.3.2, dist[2, 3] $=\min (\operatorname{dist}[2,3]$, dist_k $)=\min (3,8)=3$.
46. Step 3.4, increment $j$ and return to Step 3.1.
47. Step 3.1, $j=4, j>=4$, so increment $i$ and return to Step 2.1.
48. Step 2.1, $i=3, i<4$, so proceed to Step 2.2.
49. Step 2.2, $i-k=3$, so proceed to Step 3.
50. Step 3, j = 0 .
51. Step 3.1, j < 4, so proceed to Step 3.2.
52. Step 3.2, j-k=0, so increment jand return to Step 3.1.
53. Step 3.1, $\mathrm{j}=1, \mathrm{j}<4$, so proceed to Step 3.2.
54. Step 3.2, $\mathrm{j}-\mathrm{k}=1$, so proceed to Step 3.2.1.
55. Step 3.2.1, $\mathrm{j}-\mathrm{i}=-2$, so proceed to Step 3.3.
56. Step 3.3.1, dist_k $=\operatorname{dist}[3,0]+\operatorname{dist}[0,1]=5+3=8$.
57. Step 3.3.2, dist[3, 1] $=\min (\operatorname{dist}[3,1]$, dist_k) $=\min (1,8)=1$.
58. Step 3.4, increment $j$ and return to Step 3.1.
59. Step 3.1, $\mathrm{j}=2, \mathrm{j}<4$, so proceed to Step 3.2.
60. Step 3.2, $\mathrm{j}-\mathrm{k}=2$, so proceed to Step 3.2.1.
61. Step 3.2.1, $\mathrm{j}-\mathrm{i}=-1$, so proceed to Step 3.3.
62. Step 3.3.1, dist $k=\operatorname{dist}[3,0]+\operatorname{dist}[0,2]=5+6=11$.
63. Step 3.3.2, dist[3, 2] $=\min (\operatorname{dist}[3,2]$, dist_k $)=\min (4,11)=4$.
64. Step 3.4, increment $j$ and return to Step 3.1.
65. Step 3.1, $\mathrm{j}=3, \mathrm{j}<4$, so proceed to Step 3.2.
66. Step 3.2, $\mathrm{j}-\mathrm{k}=3$, so proceed to Step 3.2.1.
67. Step 3.2.1, $\mathbf{j}-\mathrm{i}=0$, so increment j and return to Step 3.1.
68. Step 3.1, $j=4, j>=4$, so increment $i$ and return to Step 2.1.
69. Step 2.1, $i=4, i>=4$, so increment $k$ and return to Step 1.1.
70. Step $1.1, k=1, k<4$, so proceed to Step 2.
```
71. Step 2, i=0.
72. Step 2.1, i < 4, so proceed to Step 2.2.
73. Step 2.2, i - k= -1, so proceed to Step 3.
74. Step 3, j= 0.
75. Step 3.1, j < 4, so proceed to Step 3.2.
76. Step 3.2, j - k= -1, so increment j and return to Step 3.1.
77. Step 3.1, j=1, j < 4, so proceed to Step 3.2.
78. Step 3.2, j - k=0, so increment j and return to Step 3.1.
79. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
80. Step 3.2, j - k = 1, so proceed to Step 3.2.1.
81. Step 3.2.1, j - i = 2, so proceed to Step 3.3.
82. Step 3.3.1, dist_k = dist[0, 1] + dist[1, 2] = 3 + 3 = 6.
83. Step 3.3.2, dist[0, 2] = min(dist[0, 2], dist_k) = min}(6,6)=6
84. Step 3.4, increment j and return to Step 3.1.
85. Step 3.1, j=3, j < 4, so proceed to Step 3.2.
86. Step 3.2, j - k = 2, so proceed to Step 3.2.1.
87. Step 3.2.1, j - i = 3, so proceed to Step 3.3.
88. Step 3.3.1, dist_k = dist[0, 1] + dist[1, 3] = 3 + 6 = 9.
89. Step 3.3.2, dist[0, 3] = min(dist[0, 3], dist_k) = min}(2,9)=2
90. Step 3.4, increment j and return to Step 3.1.
91. Step 3.1, j=4, j >= 4, so increment i and return to Step 2.1.
92. Step 2.1, i=1, i < 4, so proceed to Step 2.2.
93. Step 2.2, i - k=0, so increment i and return to Step 2.1.
94. Step 2.1, i=2, i < 4, so proceed to Step 2.2.
95. Step 2.2, i-k=1, so proceed to Step 3.
96. Step 3, j= 0.
97. Step 3.1, j < 4, so proceed to Step 3.2.
98. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
99. Step 3.1, j= 1, j < 4, so proceed to Step 3.2.
100. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
101. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
102. Step 3.2, j - k=1, so proceed to Step 3.2.1.
103. Step 3.2.1, j-i=0, so increment j and return to Step 3.1.
104. Step 3.1, j=3,j < 4, so proceed to Step 3.2.
105. Step 3.2, j - k = 2, so proceed to Step 3.2.1.
106. Step 3.2.1, j-i=1, so proceed to Step 3.3.
107. Step 3.3.1, dist_k = dist[2, 1] + dist[1, 3] = 2 + 6 = 8.
108. Step 3.3.2, dist[2, 3] = min(dist[2, 3], dist_k) = min(3, 8) = 3.
109. Step 3.4, increment j and return to Step 3.1.
110. Step 3.1, j=4,j >= 4, so increment i and return to Step 2.1.
111. Step 2.1, i=3,i<4, so proceed to Step 2.2.
112. Step 2.2, i-k=2, so proceed to Step 3.
113. Step 3, j= 0.
114. Step 3.1, j < 4, so proceed to Step 3.2.
115. Step 3.2, j - k=-1, so increment j and return to Step 3.1.
116. Step 3.1, j=1, j < 4, so proceed to Step 3.2.
117. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
118. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
119. Step 3.2, j - k=1, so proceed to Step 3.2.1.
120. Step 3.2.1, j - i = -1, so proceed to Step 3.3.
121. Step 3.3.1, dist_k = dist[3, 1] + dist[1, 2] = 1 + 3 = 4.
122. Step 3.3.2, dist[3, 2] = min(dist[3, 2], dist_k) = min}(4,4)=4
123. Step 3.4, increment j and return to Step 3.1.
124. Step 3.1, j=3, j < 4, so proceed to Step 3.2.
125. Step 3.2, j - k = 2, so proceed to Step 3.2.1.
126. Step 3.2.1, j - i= 0, so increment j and return to Step 3.1.
127. Step 3.1, j=4,j>=4, so increment i and return to Step 2.1.
128. Step 2.1, i=4,i>=4, so increment k and return to Step 1.1.
129. Step 1.1, k=2, k < 4, so proceed to Step 2.
130. Step 2, i= 0.
131. Step 2.1, i < 4, so proceed to Step 2.2.
132. Step 2.2, i k = -2, so proceed to Step 3.
```

```
133. Step 3, j = 0.
134. Step 3.1, j < 4, so proceed to Step 3.2.
135. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
136. Step 3.1, j= 1, j < 4, so proceed to Step 3.2.
137. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
138. Step 3.1, j=2,j < 4, so proceed to Step 3.2.
139. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
140. Step 3.1, j=3,j < 4, so proceed to Step 3.2.
141. Step 3.2, j - k = 1, so proceed to Step 3.2.1.
142. Step 3.2.1, j - i = 3, so proceed to Step 3.3.
143. Step 3.3.1, dist_k = dist[0, 2] + dist[2, 3] =6 + 3 = 9.
144. Step 3.3.2, dist[0, 3] = min(dist[0, 3], dist_k) = min(2, 9) =2.
145. Step 3.4, increment j and return to Step 3.1.
146. Step 3.1, j=4, j >= 4, so increment i and return to Step 2.1.
147. Step 2.1, i=1,i<4, so proceed to Step 2.2.
148. Step 2.2, i - k = -1, so proceed to Step 3.
149. Step 3, j = 0.
150. Step 3.1, j < 4, so proceed to Step 3.2.
151. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
152. Step 3.1, j=1,j < 4, so proceed to Step 3.2.
153. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
154. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
155. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
156. Step 3.1, j=3, j < 4, so proceed to Step 3.2.
157. Step 3.2, j - k = 1, so proceed to Step 3.2.1.
158. Step 3.2.1, j-i=2, so proceed to Step 3.3.
159. Step 3.3.1, dist_k = dist[1, 2] + dist[2, 3] = 3 + 3 = 6.
160. Step 3.3.2, dist[1, 3] = min(dist[1, 3], dist_k) = min(6,6) =6.
161. Step 3.4, increment j and return to Step 3.1.
162. Step 3.1, j=4, j >= 4, so increment i and return to Step 2.1.
163. Step 2.1, i=2, i<4, so proceed to Step 2.2.
164. Step 2.2, i-k=0, so increment i and return to Step 2.1.
165. Step 2.1, i=3, i<4, so proceed to Step 2.2.
166. Step 2.2, i-k=1, so proceed to Step 3.
167. Step 3, j= 0.
168. Step 3.1, j < 4, so proceed to Step 3.2.
169. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
170. Step 3.1, j=1, j < 4, so proceed to Step 3.2.
171. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
172. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
173. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
174. Step 3.1, j=3, j < 4, so proceed to Step 3.2.
175. Step 3.2, j - k=1, so proceed to Step 3.2.1.
176. Step 3.2.1, j-i=0, so increment j and return to Step 3.1.
177. Step 3.1, j=4,j >= 4, so increment i and return to Step 2.1.
178. Step 2.1, i=4,i>=4, so increment k and return to Step 1.1.
179. Step 1.1, k=3,k<4, so proceed to Step 2.
180. Step 2, i = 0.
181. Step 2.1, i < 4, so proceed to Step 2.2.
182. Step 2.2, i-k = -3, so proceed to Step 3.
183. Step 3, j= 0.
184. Step 3.1, j < 4, so proceed to Step 3.2.
185. Step 3.2, j-k=-3, so increment j and return to Step 3.1.
186. Step 3.1, j=1, j < 4, so proceed to Step 3.2.
187. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
188. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
189. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
190. Step 3.1, j=3,j < 4, so proceed to Step 3.2.
191. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
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192. Step 3.1, j= 4, j >= 4, so increment i and return to Step 2.1.
193. Step 2.1, i=1,i< 4, so proceed to Step 2.2.
194. Step 2.2, i-k =-2, so proceed to Step 3.
195. Step 3, j = 0.
196. Step 3.1, j < 4, so proceed to Step 3.2.
197. Step 3.2, j - k = -3, so increment j and return to Step 3.1.
198. Step 3.1, j= 1, j < 4, so proceed to Step 3.2.
199. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
200. Step 3.1, j=2, j < 4, so proceed to Step 3.2.
201. Step 3.2, j - k = -1, so increment j and return to Step 3.1.
202. Step 3.1, j=3,j < 4, so proceed to Step 3.2.
203. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
204. Step 3.1, j=4, j >= 4, so increment i and return to Step 2.1.
205. Step 2.1, i=2, i< 4, so proceed to Step 2.2.
206. Step 2.2, i-k = -1, so proceed to Step 3.
207. Step 3, j = 0.
208. Step 3.1, j < 4, so proceed to Step 3.2.
209. Step 3.2, j - k = -3, so increment j and return to Step 3.1.
210. Step 3.1, j= 1, j < 4, so proceed to Step 3.2.
211. Step 3.2, j - k = -2, so increment j and return to Step 3.1.
212. Step 3.1, j=2,j < 4, so proceed to Step 3.2.
213. Step 3.2, j-k =-1, so increment j and return to Step 3.1.
214. Step 3.1, j=3, j < 4, so proceed to Step 3.2.
215. Step 3.2, j - k = 0, so increment j and return to Step 3.1.
216. Step 3.1, j=4,j >= 4, so increment i and return to Step 2.1.
217. Step 2.1, i=3,i<4, so proceed to Step 2.2.
218. Step 2.2, i - k = 0, so increment i and return to Step 2.1.
219. Step 2.1, i=4,i >= 4, so increment k and return to Step 1.1.
220. Step 1.1,k=4, k >= 4, so proceed to Step 4.
221. Step 4, print the distance matrix dist:
dist[0, 0] = 0
dist[0,1] = 3
dist[0, 2] = 6
dist[0, 3] = 2
dist[1, 0] = 4
dist[1, 1] = 0
dist[1, 2] = 3
dist[1,3] = 6
dist[2, 0] = 6
dist[2, 1] = 2
dist[2, 2] = 0
dist[2,3] = 3
dist[3, 0] = 5
dist[3, 1] = 1
dist[3, 2] = 4
dist[3, 3] = 0
```

Table 31: The prompt of floyd warshall and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial: Given a pattern string pat of length M and a text string txt of length N .
pat: $\operatorname{pat}[0]=A, \operatorname{pat}[1]=A, \operatorname{pat}[2]=A, M=3$.
$\operatorname{txt}: \operatorname{txt}[0]=\mathrm{C}, \operatorname{txt}[1]=\mathrm{B}, \mathrm{txt}[2]=\mathrm{A}, \operatorname{txt}[3]=\mathrm{B}, \mathrm{N}=4$.
Create an empty result list 'res'.
Step 1: Set the variable upper_i to $\mathrm{N}-\mathrm{M}+1$.
Step 2: Set i to 0.
Step 3: If i < upper_i, execute the following sequence of sub-steps. Otherwise, go to Step 4.
Step 3.1: Set j to 0 . Set pos to i .
Step 3.2: If $j$ < $M$, execute in the sequence of sub-steps. Otherwise, go to Step 3.4.
a. If txt[pos] and pat[j] are not equal, go to Step 3.4.
b. Increment j, increment pos, and go back to Step 3.2.

Step 3.3: Append $i$ to the result list 'res'. Print the list 'res'.
Step 3.4: Increment i and go back to Step 3.
Step 4: Print the list 'res'.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Step 1, upper_i $=\mathrm{N}-\mathrm{M}+1=4-3+1=2$.
2. Step 2, i=0.
3. Step 3, i < upper_i (0<2), so proceed to Step 3.1.
4. Step 3.1, $\mathrm{j}=0$, pos $=\mathrm{i}=0$.
5. Step 3.2, j < $\mathrm{M}(0<3)$, so proceed to sub-steps:
a. $\operatorname{txt}[\operatorname{pos}]=\operatorname{txt}[0]=C, \operatorname{pat}[j]=\operatorname{pat}[0]=A$, not equal, so go to Step 3.4.
6. Step 3.4, increment $i(i=1)$ and go back to Step 3.
7. Step 3, i < upper_i (1 < 2), so proceed to Step 3.1.
8. Step 3.1, $\mathrm{j}=0$, pos $=\mathrm{i}=1$.
9. Step 3.2, j < $\mathrm{M}(0<3)$, so proceed to sub-steps:
a. $\operatorname{txt}[p o s]=\operatorname{txt}[1]=B, \operatorname{pat}[j]=\operatorname{pat}[0]=A$, not equal, so go to Step 3.4.
10. Step 3.4, increment $\mathrm{i}(\mathrm{i}=2)$ and go back to Step 3.
11. Step 3 , $i$ is not less than upper_ $i(2$ is not less than 2 ), so proceed to Step 4.
12. Step 4, print the list 'res': res is empty, so the output is an empty list [].

Table 32: The prompt of naive string matcher and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial: Given a pattern string pat of length M and a text string txt of length N .
pat: $\operatorname{pat}[0]=A, \operatorname{pat}[1]=A, \operatorname{pat}[2]=A, M=3$.
$\operatorname{txt}: \operatorname{txt}[0]=A, \operatorname{txt}[1]=A, \operatorname{txt}[2]=A, \operatorname{txt}[3]=A, N=4$.
Create an array $\operatorname{lps}[]$ of length $M$ with the value of $0: \operatorname{lps}[0]=0, \operatorname{lps}[1]=0, \operatorname{lps}[2]=0$.
Step 1: Set the variable length to 0.
Step 2: Set the variable i to 1.
Step 3: While $\mathbf{i}$ < M, execute with the following sequence of sub-steps:
Step 3.1: If pat[i] and pat[length] are equal:
a. Increment length.
b. Set lps[i] equal to length.
c. Increment i.
d. go back to Step 3.

Step 3.2: If pat[i] and pat[length] are not equal and length >0:
a. Set length_prev to length -1 .
b. Recall the value of Ips[length_prev].
c. Set length equal to lps[length_prev].
d. go back to Step 3.

Step 3.3: If pat[i] and pat[length] are not equal and length is 0 :
a. Set lps[i] to 0 .
b. Increment i.
c. go back to Step 3.

Step 4: Print lps array by iterating over its elements, displaying each value as "lps[i] = lps_i".
Step 5: Initialize variables i and j to 0 , and an empty result list 'res'.
Step 6: Compute remain_txt = N-i, remain_pat = M - j, remain_diff = remain_txt - remain_pat.
While remain_diff $>=0$, execute the following sequence of sub-steps:
Step 6.1: If pat[j] and txt[i] are equal:
a. Increment i.
b. Increment j.

Step 6.2: If j becomes equal to M :
a. Calculate found_index as $\mathrm{i}-\mathrm{j}$.
b. Append found_index to res.
c. Print the list 'res'.
d. Set j to $\operatorname{lps}[j-1]$.

Step 6.3: If ( $\mathrm{i}<\mathrm{N}$ ) and (pat[j] and txt[i] are not equal):
a. If j is non-zero, set j to $\mathrm{lps}[\mathrm{j}-1 \mathrm{]}$.
b. If j is 0 , increment i .

Step 7: Print the list 'res'.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Step 1 , length $=0$.
2. Step $2, i=1$.
3. Step $3, i<M(1<3)$, enter the loop.
4. Step 3.1, pat[1] = A, pat[length] = A, they are equal.
5. Increment length, length $=1$.
6. Set $\operatorname{lps}[1]=1, \mathrm{lps}=[0,1,0]$.
7. Increment $i, i=2$.
8. Step $3, i<M(2<3)$, continue the loop.
9. Step 3.1, pat[2] = A, pat[length] = A, they are equal.
10. Increment length, length $=2$.
11. Set $\operatorname{lps}[2]=2, \mathrm{lps}=[0,1,2]$.
12. Increment $\mathrm{i}, \mathrm{i}=3$.
13. Step $3, i>=M(3>=3)$, exit the loop.
14. Step 4, print lps array: $\operatorname{lps}[0]=0, \operatorname{lps}[1]=1, \operatorname{lps}[2]=2$.
15. Step $5, i=0, j=0$, res $=[]$.
16. Step 6 , remain_txt $=4$, remain_pat $=3$, remain_diff $=1$, remain_diff $>=0$, enter the loop.
17. Step 6.1, pat[j] = A, txt[i] = A, they are equal.
18. Increment $\mathrm{i}, \mathrm{i}=1$.
19. Increment j, j=1.
20. Step 6 , remain_txt $=3$, remain pat $=2$, remain_diff $=1$, remain_diff $>=0$, continue the loop.
21. Step 6.1, pat[j] = A, txt[i] = A, they are equal.
22. Increment $\mathrm{i}, \mathrm{i}=2$.
23. Increment j, j= 2.
24. Step 6, remain_txt $=2$, remain_pat $=1$, remain_diff $=1$, remain_diff $>=0$, continue the loop.
25. Step 6.1, pat $[j]=A, \operatorname{txt}[i]=A$, they are equal.
26. Increment $\mathrm{i}, \mathrm{i}=3$.
27. Increment j, j=3.
28. Step $6.2, j=M(3=3)$, found_index $=i-j=0$, append 0 to res, res $=[0]$.
29. Print res: [ 0 ].
30. Set j to $\operatorname{lps}[\mathrm{j}-1], \mathrm{j}=\operatorname{lps}[2]=2$.
31. Step 6 , remain_txt $=1$, remain_pat $=1$, remain_diff $=0$, remain_diff $>=0$, continue the loop.
32. Step 6.1, pat $[j]=A, \operatorname{txt}[i]=A$, they are equal.
33. Increment $i, i=4$.
34. Increment j, j = 3.
35. Step 6.2, $j=M(3=3)$, found_index $=i-j=1$, append 1 to res, res $=[0,1]$.
36. Print res: $[0,1]$.
37. Set j to $\operatorname{lps}[j-1], j=\operatorname{lps}[2]=2$.
38. Step 6, remain_txt $=0$, remain_pat $=1$, remain_diff $=-1$, remain_diff $<0$, exit the loop.
39. Step 7, print res: $[0,1]$.

Table 33: The prompt of kmp matcher and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input arrays for start times $S: S[0]=0, S[1]=5, S[2]=3, S[3]=3, S[4]=2, S[5]=9, S[6]=3$,
$S[7]=5, S[8]=7$ and finish times $F: F[0]=7, F[1]=9, F[2]=9, F[3]=9, F[4]=9, F[5]=10, F[6]=11, F[7]=$ 12, $\mathrm{F}[8]=15$.
Set the length of the arrays n : 9 .
Set $\mathrm{i}=0$.
Set array A = [0].
Step 1: Initialize a loop variable $\mathrm{j}=1$.
Step 2: Compare the start time of the current activity $\mathrm{S}[\mathrm{j}]$ with the finish time of the previously selected activity F[i]. Apply the following rule:
i. If $\mathrm{S}[\mathrm{j}]>=\mathrm{F}[\mathrm{i}$, the activity can be selected. Add the index j to array A , print it , and update $\mathrm{i}=\mathrm{j}$.
ii. If $\mathrm{S}[\mathrm{j}]$ < $\mathrm{F}[\mathrm{i}$, Continue.

Step 3: Increment j by 1. If j < n , go back to Step 2. Otherwise, proceed to Step 4.
Step 4: Print array A.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $i=0, j=1$.
2. $S[1]=5, F[0]=7, S[1]<F[0]$, continue.
3. $\mathrm{j}=2$.
4. $\mathrm{S}[2]=3, \mathrm{~F}[0]=7, \mathrm{~S}[2]<\mathrm{F}[0]$, continue.
5. $\mathrm{j}=3$.
6. $S[3]=3, F[0]=7, S[3]<F[0]$, continue.
7. $\mathrm{j}=4$.
8. $S[4]=2, F[0]=7, S[4]<F[0]$, continue.
9. $\mathrm{j}=5$.
10. $S[5]=9, F[0]=7, S[5]>=F[0]$, add $j$ to $A: A=[0,5], i=5$.
11. $\mathrm{j}=6$.
12. $S[6]=3, F[5]=10, S[6]<F[5]$, continue.
13. $\mathrm{j}=7$.
14. $S[7]=5, F[5]=10, S[7]<F[5]$, continue.
15. $\mathrm{j}=8$.
16. $S[8]=7, F[5]=10, S[8]<F[5]$, continue.
17. $j=9, j>=n$, exit loop.
18. Print array A: $[0,5]$.

Table 34: The prompt of activity selection and the response of gpt-4.

## Prompt

Execute the following instructions.
Initial: Set the array $p$ of length $N=4: p[0]=5, p[1]=5, p[2]=4, p[3]=4$.
Set the matrix $m$ of size $4 \times 4$ with all elements initialized to 0 .
Set maxint: 66666666.
Set L: 2.
Step 1: Is $L<4$ ? If $L$ is equal to 4 , go to Step 5 . If $L<4$ :
i. Set i: 1.
ii. Compute upper_i: N-L + 1 .
iii. Go to Step 2.

Step 2:Is $i$ < upper_i? If $i$ is equal to upper_i, increment $L$ by 1 and go to Step 1. If $i$ < upper_ $i$ :
i. Set $\mathrm{j}: \mathrm{i}+\mathrm{L}-1$.
ii. Set $m[i, j]=$ maxint.
iii. Set k: i.
iv. Go to Step 3.

Step 3: Is $\mathrm{k}-\mathrm{j}<0$ ? If $\mathrm{k}-\mathrm{j}$ is equal to 0 , increment i by 1 and go to Step 2 . If $\mathrm{k}-\mathrm{j}<0$ :
$i$. What is $i-1$ ? What are the values of $p[i-1], p[k]$, and $p[j]$ ?
ii. Calculate product $=p[i-1]$ * $p[k]$ * $p[j]$.
iii. Calculate $\mathrm{q}=\mathrm{m}[\mathrm{i}, \mathrm{k}]+\mathrm{m}[\mathrm{k}+1, \mathrm{j}]+$ product.
iv. Calculate $\mathrm{cmp}=\mathrm{m}[\mathrm{i}, \mathrm{j}]$ - q .
v. If cmp is positive, set $m[i, j]=q$.
vi. Increment k by 1.
vii. Go to Step 3.

Step 4: Increment i by 1 and go to Step 2.
Step 5: Print the value of $m[1,3]$.
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. In Step 1, $L=2,2<4$, so we perform the following sub-steps:
i. Set $\mathrm{i}=1$.
ii. Compute upper_i $=\mathrm{N}-\mathrm{L}+1=4-2+1=3$.
iii. Go to Step 2.
2. In Step 2, $i=1,1<3$, so we perform the following sub-steps:
i. Set $\mathrm{j}=\mathrm{i}+\mathrm{L}-1=1+2-1=2$.
ii. Set $m[1,2]=$ maxint $=66666666$.
iii. Set $\mathrm{k}=1$.
iv. Go to Step 3.
3. In Step 3, $\mathrm{k}-\mathrm{j}=1-2=-1,-1<0$, so we perform the following sub-steps:
i. $i-1=1-1=0$. The values of $p[0], p[1]$, and $p[2]$ are 5,5 , and 4 , respectively.
ii. Calculate product $=p[0]$ * $p[1]$ * $p[2]=5$ * 5 * $4=100$.
iii. Calculate $q=m[1,1]+m[2,2]+$ product $=0+0+100=100$.
iv. Calculate $\mathrm{cmp}=\mathrm{m}[1,2]-\mathrm{q}=66666666-100=66666566$.
v. cmp is positive, so set $\mathrm{m}[1,2]=\mathrm{q}=100$.
vi. Increment k by $1=2$.
vii. Go to Step 3.
4. In Step 3, k-j = 2-2 = 0, so increment i by $1=2$ and go to Step 2.
5. In Step 2, $i=2,2<3$, so we perform the following sub-steps:
i. Set $\mathrm{j}=\mathrm{i}+\mathrm{L}-1=2+2-1=3$.
ii. Set $\mathrm{m}[2,3]=$ maxint $=66666666$.
iii. Set k=2.
iv. Go to Step 3.
6. In Step 3, $\mathrm{k}-\mathrm{j}=2-3=-1,-1<0$, so we perform the following sub-steps:
i. $i-1=2-1=1$. The values of $p[1], p[2]$, and $p[3]$ are 5,4 , and 4 , respectively.
ii. Calculate product $=p[1]$ * $p[2] * p[3]=5 * 4 * 4=80$.
iii. Calculate $\mathrm{q}=\mathrm{m}[2,2]+\mathrm{m}[3,3]+$ product $=0+0+80=80$.
iv. Calculate $\mathrm{cmp}=\mathrm{m}[2,3]-\mathrm{q}=66666666-80=66666586$.
v. cmp is positive, so set $\mathrm{m}[2,3]=\mathrm{q}=80$.
vi. Increment k by $1=3$.
vii. Go to Step 3.
7. In Step $3, \mathrm{k}-\mathrm{j}=3-3=0$, so increment i by $1=3$ and go to Step 2 .
8. In Step 2, $i=3,3=3$, so increment $L$ by $1=3$ and go to Step 1 .
9. In Step $1, L=3,3<4$, so we perform the following sub-steps:
i. Set $\mathrm{i}=1$.
ii. Compute upper_i $=\mathrm{N}-\mathrm{L}+1=4-3+1=2$.
iii. Go to Step 2.
10. In Step 2, $i=1,1<2$, so we perform the following sub-steps:
i. Set $\mathrm{j}=\mathrm{i}+\mathrm{L}-1=1+3-1=3$.
ii. Set $m[1,3]=$ maxint $=66666666$.
iii. Set $\mathrm{k}=1$.
iv. Go to Step 3.
11. In Step $3, \mathrm{k}-\mathrm{j}=1-3=-2,-2<0$, so we perform the following sub-steps:
i. $i-1=1-1=0$. The values of $p[0], p[1]$, and $p[3]$ are 5,5 , and 4 , respectively.
ii. Calculate product $=p[0]$ * $p[1]$ * $p[3]=5$ * 5 * $4=100$.
iii. Calculate $\mathrm{q}=\mathrm{m}[1,1]+\mathrm{m}[2,3]+$ product $=0+80+100=180$.
iv. Calculate $\mathrm{cmp}=\mathrm{m}[1,3]-\mathrm{q}=66666666-180=66666486$.
v. cmp is positive, so set $\mathrm{m}[1,3]=\mathrm{q}=180$.
vi. Increment k by $1=2$.
vii. Go to Step 3.
12. In Step $3, \mathrm{k}-\mathrm{j}=2-3=-1,-1<0$, so we perform the following sub-steps:
i. $i-1=1-1=0$. The values of $p[0], p[2]$, and $p[3]$ are 5,4 , and 4 , respectively.
ii. Calculate product $=p[0]{ }^{*} p[2] * p[3]=5 * 4 * 4=80$.
iii. Calculate $\mathrm{q}=\mathrm{m}[1,2]+\mathrm{m}[3,3]+$ product $=100+0+80=180$.
iv. Calculate $\mathrm{cmp}=\mathrm{m}[1,3]-\mathrm{q}=180-180=0$.
v. cmp is not positive, so do not update $\mathrm{m}[1,3]$.
vi. Increment k by $1=3$.
vii. Go to Step 3.
13. In Step 3, k-j=3-3=0, so increment i by $1=2$ and go to Step 2 .
14. In Step 2, $i=2,2=2$, so increment $L$ by $1=4$ and go to Step 1 .
15. In Step $1, L=4,4=4$, so go to Step 5 .
16. In Step 5, print the value of $m[1,3]=180$.

The final result is 180 .
Table 35: The prompt of matrix chain multiplication and the response of gpt-4.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial: Given two lists of numbers $X$ and $Y$ with a size of $n$, where $X$ represents the independent variables and Y represents the dependent variables.
$X: X[0]=15, X[1]=25, X[2]=30, X[3]=45, X[4]=55, X[5]=65, X[6]=75, X[7]=85, X[8]=95, n=9$.
$\mathrm{Y}: \mathrm{Y}[0]=55, \mathrm{Y}[1]=82, \mathrm{Y}[2]=98, \mathrm{Y}[3]=142, \mathrm{Y}[4]=177, \mathrm{Y}[5]=201, \mathrm{Y}[6]=235, \mathrm{Y}[7]=267, \mathrm{Y}[8]=293$.
Step 1: Compute the value of $b$ for the regression line:
Step 1.1: Initialize a variable 'sx' to 0 . Iterate over all elements of $X$ to compute the sum and store the result in 'sx'.

Step 1.2: Initialize a variable 'sy' to 0 . Iterate over all elements of $Y$ to compute the sum and store the result in 'sy'.
Step 1.3: Initialize two variables 'sxsy' and 'sx2' both to 0 . Iterate over all elements of $x$ and $y$ :
a. For each iteration, add the product of the current elements of $x$ and $y$ to ' $s x s y$ '.
b. Add the square of the current element of x to ' $\mathrm{sx2}$ '.

Step 1.4: Calculate the numerator:
a. Multiply $n$ with 'sxsy' and store the result.
b. Multiply 'sx' with 'sy' and store the result in 'sx_times_sy'.
c. Subtract 'sx_times_sy' from the previously computed result to get the final numerator.

Step 1.5: Calculate the denominator:
a. Multiply n with ' $\mathrm{sx2}$ ' and store the result.
b. Square 'sx' and store the result in 'sx_squared'.
c. Subtract 'sx_squared' from the previously computed result to get the final denominator.

Step 1.6: Divide the numerator by the denominator to compute b.
Step 2: Determine the regression line parameters:
Step 2.1: Compute the mean of $X$ and $Y$ :
a. Sum all the values in $X$ and divide by $n$ to get 'mean $X$ '.
b. Sum all the values in Y and divide by n to get 'meanY'.

Step 2.2: Compute the value of a:
a. Multiply b with 'meanX' and subtract the result from 'meanY' to get the value of a.

Step 3: Print a and b as " $\mathrm{a}, \mathrm{b}=(-$
The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Step 1.1, initialize 'sx' to 0.
2. Compute the sum of $\mathrm{X}: 15+25+30+45+55+65+75+85+95=490$.
3. Set 'sx' to 490.
4. Step 1.2, initialize 'sy' to 0.
5. Compute the sum of $\mathrm{Y}: 55+82+98+142+177+201+235+267+293=1550$.
6. Set 'sy' to 1550.
7. Step 1.3, initialize 'sxsy' and 'sx2' both to 0 .
8. Compute the sum of the product of $X$ and $Y:(15$ * 55$)+(25 * 82)+(30 * 98)+(45 * 142)+(55 * 177)+(65$

* 201$)+(75$ * 235$)+(85$ * 267 $)+(95$ * 293 $)=104965$.

9. Set 'sxsy' to 104965.
10. Compute the sum of the square of $X:\left(15^{\wedge} 2\right)+\left(25^{\wedge} 2\right)+\left(30^{\wedge} 2\right)+\left(45^{\wedge} 2\right)+\left(55^{\wedge} 2\right)+\left(65^{\wedge} 2\right)+\left(75^{\wedge} 2\right)+\left(85^{\wedge} 2\right)+$ $\left(95^{\wedge} 2\right)=33875$.
11. Set 'sx2' to 33875.
12. Step 1.4, calculate the numerator: $(9$ * 104965$)-(490 * 1550)=94485$.
13. Step 1.5, calculate the denominator: $(9$ * 33875$)-\left(490^{\wedge} 2\right)=3045$.
14. Step 1.6, compute b: $94485 / 3045=31.03$.
15. Step 2.1, compute 'meanX': $490 / 9=54.44$.
16. Compute 'meanY': $1550 / 9=172.22$.
17. Step 2.2, compute a: $(31.03$ * 54.44$)-172.22=-1460.84$.
18. Step 3 , print $a$ and $b: " a, b=(-1460.84,31.03) "$.

Table 36: The prompt of least square regression and the response of gpt-4. The correct answer shall be $(7.98,3.02)$, and the first error is at line 8.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial: Given a list of complex numbers x whose length is a power of 2 , compute its discrete Fourier transform (DFT) using the Cooley-Tukey algorithm.
$\mathrm{x}: ~[1, ~ 9, ~ 4, ~ 8, ~ 9, ~ 2, ~ 4, ~ 1] . ~$
Define the function "FFT" with the argument 'x', 'recursive_level' and 'next_step'.
Step 1: Call the "FFT" Function with the arguments 'x', 'recursive_level_x'=1, 'next_step_x'="". Inside the "FFT" function, follow these steps:

Step 2: Calculate the length of the list ' $x$ ' and assign it to the variable ' $N$ _ $x$ '.
Step 3: Check the value of ' N _x':

- If N_x equals 1, compute 'last_level' = recursive_level_x-1, return $x$, and go back to 'last_level' at 'next_step_x'.
- Otherwise, proceed to Step 4.

Step 4: Recursively calculate the discrete Fourier transform for the even and odd indexed elements of ' $x$ ':
Step 4.1: For even indices: List $x$ eeven $=x[\because 2]$, go to Step 1, call FFT(x_even, recursive_level_x_even=recursive_level_x+1, next_step_x_even="Step 4.2"), name the result T_x_even.
Step 4.2: For odd indices: List $x$ _odd $=x[1:: 2]$, go to Step 1, call FFT(x_odd, recursive_level_x_odd=recursive_level_x+1, next_step_x_odd="Step 5"), name the result T_x_odd.

Step 5: Compute half of ' $N \_x^{\prime}$ ', which is ' $N \_x$ half' $=\operatorname{int}\left(N \_x / 2\right)$.
Step 6: Compute the numeric value of factor:
Step 6.1. Initialize an empty list for 'factor'.
Step 6.2. For each integer ' $k$ ' starting from 0 up to one less than ' $N \_$_' (i.e., $0,1, \ldots, N \_x-1$ ), do the following steps:

Step 6.2.1. Compute the angle for the exponential:

- theta_k $=-2$ * $\mathrm{pi}^{*} k / N \_x$

Step 6.2.2. Compute the complex exponential for the angle:

- exp_value $=e^{\wedge}\left(i^{*}\right.$ theta_k)

Step 6.2.3. Append the computed 'exp_value' to the 'factor' list.
Step 7: Calculate ' $T$ _ $x$ ', by using the concatenation of two arrays, and present the numeric value.

- first_half = T_x_even + factor[:N_x_half] * T_x_odd.
- second_half $=\bar{T}$ _x_even + factor $\left[\mathrm{N} \_x\right.$ _half: $] * \bar{T}$ _x_odd.
$-T_{-} x=$ first_half + second_half.
Step 8: Compute 'last_level' = recursive_level_x-1, return the list $T$ _ $x$, and go back to 'last_level' at 'next_step_ $x$ ', unless the current recursive_level_x is 1 .

Perform the computation procedure step by step, adhering strictly to the outlined instructions.
Each line should be numbered sequentially with the recursion level (e.g., "level=1, 1.", "level=1, 2.", "level=2, 1.").
level=1, 1. Step 1, Call FFT(x=[1, 9, 4, 8, 9, 2, 4, 1], recursive_level=1, next_step_x=").
level $=1,2$. Step 2, Calculate the length of the list $x$ : $N \_x=8$.
level=1, 3. Step 3, Check the value of $N \_x$ : $N \_x=8$, proceed to Step 4.
level=1, 4.1. Step 4.1, For even indices: $x$ _even $=[1,4,9,4]$, call FFT(x_even, recursive_level_x_even=2, next_step_x_even="Step 4.2").
level=2, 1. Step 1, Call FFT(x=[1, 4, 9, 4], recursive_level=2, next_step_x='Step 4.2').
level=2, 2. Step 2, Calculate the length of the list $x$ : $N-x=4$.
level=2, 3. Step 3, Check the value of $N \_x$ : $N \_x=4$, proceed to Step 4.
level=2, 4.1. Step 4.1, For even indices: $x$ _even $=[1,9]$, call FFT(x_even, recursive_level_x_even=3, next_step_x_even="Step 4.2").
level=3, 1. Step 1, Call FFT(x=[1, 9], recursive_level=3, next_step_x='Step 4.2').
level=3, 2. Step 2, Calculate the length of the list $\mathrm{x}: \mathrm{N} \_\mathrm{x}=2$.
level=3, 3. Step 3, Check the value of $N \_x$ : $N \_x=2$, proceed to Step 4.
level=3, 4.1. Step 4.1, For even indices: x_even = [1], call FFT(x_even, recursive_level_x_even=4, next_step_x_even="Step 4.2").
level=4, 1. Step 1, Call FFT(x=[1], recursive_level=4, next_step_x='Step 4.2').
level $=4,2$. Step 2, Calculate the length of the list x : $\mathrm{N} \_\mathrm{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[1]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=3, 4.2. Step 4.2, For odd indices: x_odd = [9], call FFT(x_odd, recursive_level_x_odd=4, next_step_x_odd="Step 5").
level=4, 1. Step 1, Call FFT ( $x=[9]$, recursive_level=4, next_step_ $x=$ 'Step 5 ').
level $=4,2$. Step 2, Calculate the length of the list $\mathrm{x}: \mathrm{N} \mathbf{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[9]$, and go back to last_level at next_step_x = 'Step 5'.
level=3,5. Step 5, Compute half of $N \_x$ : $N \_x$ half $=\operatorname{int}(2 / 2)=1$.
level=3, 6.1. Step 6.1, Initialize an empty list for factor: factor $=[]$.
level=3, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level=3, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 2=0$.
level $=3,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ _value $=e^{\wedge}\left(\mathrm{i}^{*} 0\right)=1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level $=3,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_1 $=-2$ * pi * $1 / 2=-\mathrm{pi}$.
level $=3$, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=\mathrm{e}^{\wedge}\left(\mathrm{i}^{*}-\mathrm{pi}\right)=-1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-1]$.
level=3, 7. Step 7, Calculate T_x: first_half $=[1]+[1] *[9]=[1+9]=[10]$, second_half $=[1]+[-1] *[9]=[1-9]=$ $[-8], \mathrm{T} \_\mathrm{X}=[10,-8]$.
level=3, 8 . Step 8, Compute last_level $=2$, return T_x $=[10,-8]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=2, 4.2. Step 4.2, For odd indices: x_odd = [4], call FFT(x_odd, recursive_level_x_odd=3, next_step_x_odd="Step 5").
level=3, 1. Step 1, Call FFT( $x=[4]$, recursive_level=3, next_step_ $x=$ 'Step 5 ').
level=3, 2. Step 2, Calculate the length of the list $x$ : $N \_x=1$.
level=3, 3. Step 3, Check the value of N_x: N_x = 1, compute last_level = 2, return $x=[4]$, and go back to last_level at next_step_x = 'Step 5'.
level=2, 5 . Step 5, Compute half of $N \_x$ : $N \_x$ half $=\operatorname{int}(4 / 2)=2$.
level=2, 6.1. Step 6.1, Initialize an empty list for factor: factor = [].
level=2, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 4=0$.
level $=2,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ _value $=e^{\wedge}\left(i^{*} 0\right)=1$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_1 $=-2$ * pi * $1 / 4=-\mathrm{pi} / 2$.
level $=2,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=\mathrm{e}^{\wedge}\left(\mathrm{i}^{*}-\mathrm{p} / 2\right)=-\mathrm{i}$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-i]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_2 $=-2$ * pi * $2 / 4=-\mathrm{pi}$.
level=2, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp \_$value $=e^{\wedge}\left(i^{*}-p i\right)=-1$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-i,-1]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_3 $=-2$ * $\mathrm{pi} * 3 / 4=-3^{*} \mathrm{pi} / 2$.
level $=2,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(i^{*}-3^{*} p i / 2\right)=i$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-i,-1, i]$.
level=2, 7. Step 7, Calculate T_x: first_half $=[10,-8]+[1,-i] *[4]=[10+4,-8-4 i]=[14,-8-4 i]$, second_half $=$ $[10,-8]+[-1, i]$ * $[4]=[10-4,-8+4 i]=[6,-8+4 i], T_{-} x=[14,-8-4 i, 6,-8+4 i]$.
level=2, 8. Step 8, Compute last_level $=1$, return $T_{-} x=[14,-8-4 i, 6,-8+4 i]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=1, 4.2. Step 4.2, For odd indices: $x$ _odd $=[9,8,2,1]$, call FFT(x_odd, recursive_level_x_odd=2, next_step_x_odd="Step 5").
level=2, 1. Step 1, Call FFT(x=[9, 8, 2, 1], recursive_level=2, next_step_x='Step 5’).
level $=2,2$. Step 2, Calculate the length of the list $x$ : $N \_x=4$.
level=2, 3. Step 3, Check the value of $N \_x$ : $N \_x=4$, proceed to Step 4.
level=2, 4.1. Step 4.1, For even indices: x_even = [9, 2], call FFT(x_even, recursive_level_x_even=3, next_step_x_even="Step 4.2").
level=3, 1. Step 1, Call FFT(x=[9, 2], recursive_level=3, next_step_x='Step 4.2').
level=3, 2. Step 2, Calculate the length of the list $x: N \_x=2$.
level=3, 3. Step 3, Check the value of $N \_x$ : $N \_x=2$, proceed to Step 4.
level=3, 4.1. Step 4.1, For even indices: x_even = [9], call FFT(x_even, recursive_level_x_even=4, next_step_x_even="Step 4.2").
level=4, 1. Step 1, Call FFT(x=[9], recursive_level=4, next_step_x='Step 4.2').
level $=4,2$. Step 2, Calculate the length of the list x : $\mathrm{N} \_\mathrm{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[9]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=3, 4.2. Step 4.2, For odd indices: x_odd = [2], call FFT(x_odd, recursive_level_x_odd=4, next_step_x_odd="Step 5").
level=4, 1. Step 1, Call FFT ( $x=[2]$, recursive_level=4, next_step_ $x=$ 'Step 5 ').
level $=4,2$. Step 2, Calculate the length of the list x : $\mathrm{N} \mathbf{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[2]$, and go back to last_level at next_step_x = 'Step 5'.
level=3,5. Step 5, Compute half of $N \_x$ : $N \_x \_$half $=\operatorname{int}(2 / 2)=1$.
level=3, 6.1. Step 6.1, Initialize an empty list for factor: factor $=[]$.
level=3, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level $=3,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 2=0$.
level $=3,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ _value $=\mathrm{e}^{\wedge}\left(\mathrm{i}^{*} 0\right)=1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level $=3,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_1 $=-2$ * pi * $1 / 2=-\mathrm{pi}$.
level $=3$, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(\mathrm{i}^{*}-\mathrm{pi}\right)=-1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-1]$.
level $=3,7$. Step 7, Calculate $T_{-}$x: first_half $=[9]+[1]$ * $[2]=[9+2]=[11]$, second_half $=[9]+[-1] *[2]=[9-2]=$ [7], T_x = [11, 7].
level=3, 8. Step 8, Compute last_level $=2$, return $T \_x=[11,7]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=2, 4.2. Step 4.2, For odd indices: $x$ _odd $=[8,1]$, call FFT(x_odd, recursive_level_x_odd=3, next_step_x_odd="Step 5").
level=3, 1. Step 1, Call FFT(x=[8, 1], recursive_level=3, next_step_x='Step 5').
level=3, 2. Step 2, Calculate the length of the list x : $\mathrm{N}-\mathrm{x}=2$.
level=3, 3. Step 3, Check the value of $N \_x$ : $N \_x=2$, proceed to Step 4.
level=3, 4.1. Step 4.1, For even indices: x_even = [8], call FFT(x_even, recursive_level_x_even=4, next_step_x_even="Step 4.2").
level=4, 1. Step 1, Call FFT(x=[8], recursive_level=4, next_step_x='Step 4.2').
level $=4,2$. Step 2, Calculate the length of the list x : $\mathrm{N} \_\mathrm{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[8]$, and go back to last_level at next_step_x = 'Step 4.2'.
level=3, 4.2. Step 4.2, For odd indices: x_odd = [1], call FFT(x_odd, recursive_level_x_odd=4, next_step_x_odd="Step 5").
level=4, 1. Step 1, Call FFT(x=[1], recursive_level=4, next_step_x='Step 5').
level $=4,2$. Step 2, Calculate the length of the list $\mathrm{x}: \mathrm{N} \_\mathrm{x}=1$.
level=4, 3. Step 3, Check the value of $N \_x$ : $N \_x=1$, compute last_level $=3$, return $x=[1]$, and go back to last_level at next_step_x = 'Step 5'.
level $=3,5$. Step 5 , Compute half of N_x: N_x_half $=\operatorname{int}(2 / 2)=1$.
level=3, 6.1. Step 6.1, Initialize an empty list for factor: factor $=[]$.
level=3, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level $=3,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 2=0$.
level $=3,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(i^{*} 0\right)=1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level=3, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_1 = -2 * pi * $1 / 2=-\mathrm{pi}$.
level $=3,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(\mathrm{i}^{*}-\mathrm{pi}\right)=-1$.
level=3, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-1]$.
level $=3,7$. Step 7, Calculate $T_{\_}$x: first_half $=[8]+[1]$ * $[1]=[8+1]=[9]$, second_half $=[8]+[-1]$ * $[1]=[8-1]=$ [7], T_x = [9, 7].
level=3, 8. Step 8, Compute last_level = 2, return T_x = [9, 7], and go back to last_level at next_step_x = 'Step 5'. level=2,5. Step 5, Compute half of $N \_x$ : N_x_half $=\operatorname{int}(4 / 2)=2$.
level=2, 6.1. Step 6.1, Initialize an empty list for factor: factor $=[]$.
level=2, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 4=0$.
level=2, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(i^{*} 0\right)=1$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_1 $=-2$ * pi * $1 / 4=-\mathrm{pi} / 2$.
level=2, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(i^{*}-p i / 2\right)=-i$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-i]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_2 $=-2$ * pi * $2 / 4=-\mathrm{pi}$.
level=2, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ value $=e^{\wedge}\left(\mathrm{i}^{*}-\mathrm{pi}\right)=-1$.
level=2, 6.2.3. Step 6.2.3. Append the computed exp_value to the factor list: factor $=[1,-i,-1]$.
level=2, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_3 $=-2^{*} \mathrm{pi} * 3 / 4=-3^{*} \mathrm{pi} / 2$.
level $=2,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=\mathrm{e}^{\wedge}\left(\mathrm{i}^{\star}-3^{\star} \mathrm{p} i / 2\right)=\mathrm{i}$.
level=2, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,-i,-1, i]$.
level=2, 7. Step 7, Calculate T_x: first_half $=[11,7]+[1,-i]$ * $[9,7]=[11+9,7+7 \mathrm{i}]=[20,7+7 \mathrm{i}]$, second_half $=$ $[11,7]+[-1, i]^{*}[9,7]=[11-9,7-7 i]=[2,7-7 i], T_{-} x=[20,7+7 i, 2,7-7 i]$.
level=2, 8. Step 8, Compute last_level $=1$, return $T_{-} x=[20,7+7 i, 2,7-7 i]$, and go back to last_level at next_step_x = 'Step 5'.
level $=1,5$. Step 5 , Compute half of $N \_x$ : $N \_x$ half $=\operatorname{int}(8 / 2)=4$.
level=1, 6.1. Step 6.1, Initialize an empty list for factor: factor $=[]$.
level=1, 6.2. Step 6.2, For each integer $k$ starting from 0 up to one less than $N \_x$ (i.e., $0,1, \ldots, N \_x-1$ ):
level=1, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_0 $=-2 * \mathrm{pi}^{*} 0 / 8=0$.
level $=1,6.2 .2$. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=e^{\wedge}\left(i^{*} 0\right)=1$.
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1]$.
level $=1,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_1 $=-2 * \mathrm{pi}^{*} 1 / 8=-\mathrm{pi} / 4$.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=e^{\wedge}\left(i^{*}-p i / 4\right)=1 /$ sqrt(2) i/sqrt(2).
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 / \operatorname{sqrt}(2)-\mathrm{i} / \mathrm{sqrt}(2)]$.
level $=1,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_2 $=-2 * \mathrm{pi}^{*} 2 / 8=-\mathrm{pi} / 2$.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=\mathrm{e}^{\wedge}\left(\mathrm{i}^{*}-\mathrm{pi} / 2\right)=-\mathrm{i}$.
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 / \mathrm{sqrt}(2)-\mathrm{i} /$ sqrt(2), -i$]$.
level $=1$, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_3 $=-2$ * $\mathrm{pi} * 3 / 8=-3^{*} \mathrm{pi} / 4$.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=e^{\wedge}\left(i^{*}-3^{*} p i / 4\right)=-1 /$ sqrt(2) i/sqrt(2).
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 / \operatorname{sqrt}(2)-\mathrm{i} / \mathrm{sqrt}(2),-\mathrm{i}$, $-1 /$ sqrt(2) $-\mathrm{i} / \mathrm{sqrt}(2)]$.
level=1, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_4 $=-2$ * pi * $4 / 8=-$ pi.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: $\exp$ _value $=e^{\wedge}\left(i^{*}-p i\right)=-1$.
level $=1,6.2 .3$. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 /$ sqrt(2) $-\mathrm{i} / \mathrm{sqrt}(2),-\mathrm{i}$, $-1 /$ sqrt(2) $-\mathrm{i} /$ sqrt(2), -1$]$.
level $=1,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_5 $=-2$ * $\mathrm{pi} * 5 / 8=-5^{*} \mathrm{pi} / 4$.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=e^{\wedge}\left(i^{*}-5^{*} \mathrm{p} / 4\right)=-1 /$ sqrt(2) $+\mathrm{i} /$ sqrt(2).
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 / s q r t(2)-i / s q r t(2), ~-i$, $-1 /$ sqrt(2) $-\mathrm{i} / \mathrm{sqrt}(2),-1,-1 /$ sqrt(2) $+\mathrm{i} /$ sqrt(2)].
level $=1,6.2 .1$. Step 6.2.1, Compute the angle for the exponential: theta_6 $=-2^{*} \mathrm{pi}^{*} 6 / 8=-3^{*} \mathrm{pi} / 2$.
level=1, 6.2.2. Step 6.2.2, Compute the complex exponential for the angle: exp_value $=e^{\wedge}\left(i^{*}-3^{*} p i / 2\right)=i$.
level=1, 6.2.3. Step 6.2.3, Append the computed exp_value to the factor list: factor $=[1,1 / s q r t(2)-i / s q r t(2),-i$,
$-1 /$ sqrt(2) $-\mathrm{i} / \mathrm{sqrt}(2),-1,-1 / \mathrm{sqrt}(2)+\mathrm{i} / \mathrm{sqrt}(2)$, i$]$.

```
level=1, 6.2.1. Step 6.2.1, Compute the angle for the exponential: theta_7 =-2 * pi * \(7 / 8=-7^{*} \mathrm{pi} / 4\).
level \(=1,6.2 .2\). Step 6.2.2, Compute the complex exponential for the angle: exp_value \(=e^{\wedge}\left(i^{*}-7^{*} p i / 4\right)=1 / s q r t(2)+\)
i/sqrt(2).
level \(=1,6.2 .3\). Step 6.2.3, Append the computed exp_value to the factor list: factor \(=[1,1 / \operatorname{sqrt}(2)-\mathrm{i} / \mathrm{sqrt}(2),-i\),
\(-1 /\) sqrt(2) \(-\mathrm{i} /\) sqrt(2), \(-1,-1 /\) sqrt(2) \(+i / s q r t(2)\), i, \(1 / s q r t(2)+i / s q r t(2)]\).
level \(=1,7\). Step 7, Calculate T_x: first_half \(=[14,-8-4 i, 6,-8+4 i]+[1,1 /\) sqrt(2) \(-i /\) sqrt(2), \(-i,-1 /\) sqrt(2) \(-i /\) sqrt(2) \(]\)
* \([20,7+7 \mathrm{i}, 2,7-7 \mathrm{i}]=\left[14+20,(-8-4 \mathrm{i})+(1 / \text { sqrt(2) }-\mathrm{i} / \mathrm{sqrt}(2))^{*}(7+7 \mathrm{i}), 6+2 \mathrm{i},(-8+4 \mathrm{i})+(-1 / \text { sqrt(2) }-\mathrm{i} / \mathrm{sqrt}(2))^{*}(7-\right.\)
\(7 \mathrm{i})]=[34,-1-15 \mathrm{i}, 6+2 \mathrm{i},-15-1 \mathrm{i}]\).
level=1, 7. Step 7, Calculate T_x: second_half \(=[14,-8-4 i, 6,-8+4 i]+[-1,-1 /\) sqrt(2) \(+i / s q r t(2), i, 1 / s q r t(2)+\)
\(\mathrm{i} / \operatorname{sqrt}(2)] *[20,7+7 \mathrm{i}, 2,7-7 \mathrm{i}]=\left[14-20,(-8-4 \mathrm{i})+(-1 / \operatorname{sqrt}(2)+\mathrm{i} / \operatorname{sqrt}(2))^{*}(7+7 \mathrm{i}), 6-2 \mathrm{i},(-8+4 \mathrm{i})+(1 / \operatorname{sqrt}(2)+\right.\)
\(\left.\mathrm{i} / \mathrm{sqrt}(2))^{*}(7-7 \mathrm{i})\right]=[-6,-1+15 \mathrm{i}, 6-2 \mathrm{i},-15+1 \mathrm{i}]\).
level \(=1,7\). Step 7, Calculate \(T \_x\) : \(T \_x=\) first_half + second_half \(=[34,-1-15 i, 6+2 i,-15-1 i,-6,-1+15 i, 6-2 i\),
\(-15+1 \mathrm{i}]\).
The discrete Fourier transform of \(x\) using the Cooley-Tukey algorithm is: \([34,-1-15 i, 6+2 i,-15-1 i,-6,-1+15 i, 6\) \(-2 i,-15+1 i]\).
```

Table 37: The prompt of clrs mini numeric/discrete fourier transform and the response of gpt-4. The correct answer shall be $[(38+0 j),(-8-9.9 j),(2-2 j),(-8-9.9 j),(-2-0 j),(-8+9.9 j),(2+2 j),(-8+9.9 j)]$, and the first mistake is at "level=2, 4.2.", where the variable x_odd shall be [4, 4] rather than [4].

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial:
You are given arrays 'xs' and ' ys ' of length N , representing x and y coordinates of points.
$-\mathrm{xs}: \mathrm{xs}[0]=16.89, \mathrm{xs}[1]=15.16, \mathrm{xs}[2]=8.41, \mathrm{xs}[3]=5.18, \mathrm{xs}[4]=10.23, \mathrm{xs}[5]=8.1, \mathrm{xs}[6]=15.68, \mathrm{xs}[7]=$ 6.07, $x s[8]=9.53, \mathrm{~N}=9$.

- ys: $y s[0]=11.67, y s[1]=18.16, y s[2]=10.09, y s[3]=5.64, y s[4]=15.12, y s[5]=12.37, y s[6]=5.01, y s[7]=$ $18.19, \mathrm{ys}[8]=19.66$.

Set up:

1. Initialize an array 'in_hull' of length $N$ with all values set to zero: in_hull $[0]=0$, in_hull[1] $=0$, in_hull $[2]=0$, in_hull[3] $=0$, in_hull[ 4$]=0$, in_hull[5] $=0$, in_hull $[6]=0$, in_hull[7] $=0$, in_hull $[8]=0$.
2. Create an array 'stack_prev' filled with values from 0 to $\mathrm{N}-1$ : stack_prev[0] = 0 , stack_prev[1] = 1, stack_prev[2] $=2$, stack_prev[3] $=3$, stack_prev[4] $=4$, stack_prev[5] $=5$, stack_prev[6] $=6$, stack_prev[7] $=$ 7, stack_prev[8] = 8 .
3. Create an array 'atans' of length $N$ with all values set to zero: atans $[0]=0$, $\operatorname{atans}[1]=0, \operatorname{atans}[2]=0$, $\operatorname{atans}[3]=0, \operatorname{atans}[4]=0, \operatorname{atans}[5]=0, \operatorname{atans}[6]=0, \operatorname{atans}[7]=0, \operatorname{atans}[8]=0$.
Step 1: Define a function named 'counter_clockwise' that takes in three indices: $\mathrm{i}, \mathrm{j}$, and k.

- Compute the value: '(xs[j] - xs[i]) * $(\mathrm{ys}[\mathrm{k}]-\mathrm{ys}[\mathrm{i}])-(\mathrm{ys}[\mathrm{j}]-\mathrm{ys}[\mathrm{i}]){ }^{*}(\mathrm{xs}[\mathrm{k}]-\mathrm{xs}[\mathrm{i}])$ '.
- Return 'True' if this value is less than or equal to 0 , indicating that the three points with these indices form a counter-clockwise turn or are collinear. Otherwise, return 'False'.

Step 2: Start by setting the variable 'best' to 0 .
Step 3: Iterate over each point by its index 'í:

- If 'ys[i]' is less than 'ys[best]' OR ('ys[i]' equals 'ys[best]' AND 'xs[i]' is less than 'xs[best]'), set 'best' to i.

Step 4: Set the entry 'in_hull[best]' to 1 , indicating that the point with index 'best' is part of the convex hull.
Step 5: Set the value of 'last_stack' to 'best'.
Step 6: For every point (by its index 'i'):

- If 'i' isn't the same as 'best', compute the 2-argument arctangent of the differences 'ys[i] - ys[best]' (for y) and 'xs[i] - xs[best]' (for x), and store it in 'atans[i]'. You shall present the numeric value.

After completing the loop for Step 6:

- Assign a very negative placeholder value (-123456789) to 'atans[best]'.

Step 7: Sort the indices based on their corresponding 'atans' values and store the result in the array 'ind'.
Step 8: Restore the value of 'atans[best]' to 0.
Step 9: Traverse through all points from 1 to $\mathrm{N}-1$ by their index 'fi:

- If ' i ' is 3 or more, continuously check if points with indices 'stack_prev[last_stack]', 'last_stack', and 'ind[i]' form a counter-clockwise turn using the 'counter_clockwise' function.
- If they do, perform the following:
- Assign 'last_stack' to 'prev_last'.
- Update 'last_stack' with the value of 'stack_prev[last_stack]'.
- Set 'stack_prev[prev_last]' to 'prev_last'.
- Setting 'in_hull[prev_last]' to 0.
- Setting 'in_hull[ind[i]]' to 1.
- Update 'stack_prev[ind[i]]' with the current value of 'last_stack'.
- Update 'last_stack' with the value of 'ind[i]'.

Step 10: Print the array 'in_hull'.
$\qquad$

The computation procedure is as follows, from Step 2 to Step 10, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. Step 2, set 'best' to 0 .
2. Step 3, iterate over each point by its index if:

- For $\mathrm{i}=0, \mathrm{ys}[0]=11.67, \mathrm{xs}[0]=16.89, \mathrm{ys}[$ best $]=11.67, \mathrm{xs}[$ best $]=16.89$, no update to 'best'.
- For $\mathrm{i}=1, \mathrm{ys}[1]=18.16, \mathrm{ys}[$ best $]=11.67$, no update to 'best'.
- For $\mathrm{i}=2, \mathrm{ys}[2]=10.09$, $\mathrm{ys}[$ best $]=11.67$, no update to 'best'.
- For $\mathrm{i}=3, \mathrm{ys}[3]=5.64, \mathrm{ys}[$ best $]=11.67$, update 'best' to 3 .
- For $\mathrm{i}=4, \mathrm{ys}[4]=15.12, \mathrm{ys}[$ best $]=5.64$, no update to 'best'.
- For $\mathrm{i}=5, \mathrm{ys}[5]=12.37, \mathrm{ys}[b e s t]=5.64$, no update to 'best'.
- For $\mathrm{i}=6, \mathrm{ys}[6]=5.01$, $\mathrm{ys}[$ best $]=5.64$, update 'best' to 6 .
- For $\mathrm{i}=7, \mathrm{ys}[7]=18.19, \mathrm{ys}[$ best $=5.01$, no update to 'best'.
- For $\mathrm{i}=8, \mathrm{ys}[8]=19.66, \mathrm{ys}[$ best $]=5.01$, no update to 'best'.

3. Step 4 , set 'in_hull[best]' to 1 , so in_hull $[6]=1$.
4. Step 5, set 'last_stack' to 'best', so 'last_stack' $=6$.
5. Step 6 , for every point (by its index 'i'):

- For $\mathrm{i}=0$, compute atan2 $(\mathrm{ys}[0]-\mathrm{ys}[6], \mathrm{xs}[0]-\mathrm{xs}[6])=\operatorname{atan2}(11.67-5.01,16.89-15.68)=\operatorname{atan} 2(6.66,1.21)=$ 1.394, store it in atans[0].
- For $\mathrm{i}=1$, compute atan2 $(\mathrm{ys}[1]-\mathrm{ys}[6], \mathrm{xs}[1]-\mathrm{xs}[6])=\operatorname{atan2}(18.16-5.01,15.16-15.68)=\operatorname{atan2}(13.15,-0.52)=$ 3.054, store it in atans[1].
- For $\mathrm{i}=2$, compute atan2( $\mathrm{ys}[2]-\mathrm{ys}[6], \mathrm{xs}[2]-\mathrm{xs}[6])=\operatorname{atan2} 2(10.09-5.01,8.41-15.68)=\operatorname{atan2}(5.08,-7.27)=$ 2.469, store it in atans[2].
- For $\mathrm{i}=3$, compute $\operatorname{atan2} 2(\mathrm{ys}[3]-\mathrm{ys}[6], \mathrm{xs}[3]-\mathrm{xs}[6])=\operatorname{atan} 2(5.64-5.01,5.18-15.68)=\operatorname{atan2}(0.63,-10.5)=$ 2.937, store it in atans[3].
- For $\mathrm{i}=4$, compute $\operatorname{atan2}(\mathrm{ys}[4]-\mathrm{ys}[6], \mathrm{xs}[4]-\mathrm{xs}[6])=\operatorname{atan2}(15.12-5.01,10.23-15.68)=\operatorname{atan2}(10.11,-5.45)=$ 2.081, store it in atans[4].
- For $i=5$, compute $\operatorname{atan} 2(y s[5]-y s[6], x s[5]-x s[6])=\operatorname{atan} 2(12.37-5.01,8.1-15.68)=\operatorname{atan2}(7.36,-7.58)=$ 2.401, store it in atans[5].
- For $i=6$, skip since $i$ is the same as 'best'.
- For $\mathrm{i}=7$, compute $\operatorname{atan2}(\mathrm{ys}[7]-\mathrm{ys}[6], \mathrm{xs}[7]-\mathrm{xs}[6])=\operatorname{atan} 2(18.19-5.01,6.07-15.68)=\operatorname{atan2}(13.18,-9.61)=$ 2.174, store it in atans[7].
- For $\mathrm{i}=8$, compute $\operatorname{atan2}(\mathrm{ys}[8]-\mathrm{ys}[6], \mathrm{xs}[8]-\mathrm{xs}[6])=\operatorname{atan2}(19.66-5.01,9.53-15.68)=\operatorname{atan} 2(14.65,-6.15)=$ 1.963, store it in atans[8].

6. Assign a very negative placeholder value $(-123456789)$ to 'atans [best]', so atans[6] $=-123456789$.
7. Step 7, sort the indices based on their corresponding 'atans' values and store the result in the array 'ind': ind = $[6,0,8,4,7,2,5,3,1]$.
8. Step 8 , restore the value of 'atans[best]' to 0 , so atans $[6]=0$.
9. Step 9, traverse through all points from 1 to $\mathrm{N}-1$ by their index ' i :

- For $i=1$, ind $[i]=0$, counter_clockwise $(6,0,8)=$ True, in_hull $[0]=1$, stack_prev[0] = 6, last_stack $=0$.
- For $i=2$, ind $[i]=8$, counter_clockwise $(6,0,8)=$ True, in_hull $[8]=1$, stack_prev[8] $=0$, last_stack $=8$.
- For $i=3$, ind $[i]=4$, counter_clockwise $(0,8,4)=$ True, in_hull[4] $=1$, stack_prev[4] $=8$, last_stack $=4$.
- For $i=4$, ind $[i]=7$, counter_clockwise $(8,4,7)=$ False, in_hull[ 7$]=1$, stack_prev[7] = 4, last_stack $=7$.
- For $\mathrm{i}=5$, ind $[\mathrm{i}]=2$, counter_clockwise $(4,7,2)=$ False, prev_last $=7$, last_stack $=4$, stack_prev[7] $=7$, in_hull[ $[7]$
$=0$, in_hull[2] $=1$, stack_prev[2] $=4$, last_stack $=2$.
- For $i=6$, ind[ $[i]=5$, counter_clockwise $(4,2,5)=$ True, in_hull[5] = 1, stack_prev[5] = 2, last_stack $=5$.
- For $\mathrm{i}=7$, ind $[\mathrm{i}]=3$, counter_clockwise $(2,5,3)=$ False, prev_last $=5$, last_stack $=2$, stack_prev[5] $=5$, in_hull[5]
$=0$, in_hull[3] = 1 , stack_prev[3] $=2$, last_stack $=3$.
- For $\mathrm{i}=8$, ind[ $[\mathrm{i}]=1$, counter_clockwise $(2,3,1)=$ True, in_hull[1] = 1 , stack_prev[1] = 3, last_stack = 1 .

10. Step 10 , print the array 'in_hull': $[1,1,1,1,1,0,1,0,1]$.

Table 38: The prompt of Graham scan and the response of gpt-4. The correct answer shall be $[1,1,0,1,0,0,1,1,1]$, and the first two errors are at Step 3 and Step 6.

## Prompt

Execute the instructions step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial:
You are given arrays 'xs' and ' ys ' of length N , representing x and y coordinates of points.
$-\mathrm{xs}: \mathrm{xs}[0]=12.79, \mathrm{xs}[1]=0.5, \mathrm{xs}[2]=5.5, \mathrm{xs}[3]=4.46, \mathrm{xs}[4]=14.73, \mathrm{xs}[5]=13.53, \mathrm{xs}[6]=17.84, \mathrm{xs}[7]=$ 1.74, $\mathrm{xs}[8]=8.44, \mathrm{~N}=9$.
$-\mathrm{ys}: \mathrm{ys}[0]=0.6, \mathrm{ys}[1]=4.37, \mathrm{ys}[2]=10.11, \mathrm{ys}[3]=0.53, \mathrm{ys}[4]=3.98, \mathrm{ys}[5]=13.0, \mathrm{ys}[6]=10.9, \mathrm{ys}[7]=4.41$, $\mathrm{ys}[8]=11.79$.
Initialize an array 'in_hull' of length $N$ with all values set to zero: in_hull $[0]=0$, in_hull[1] $=0$, in_hull $[2]=0$, in_hull $[3]=0$, in_hull[ $[4]=0$, in_hull $[5]=0$, in_hull $[6]=0$, in_hull $[7]=0$, in_hull $[8]=0$.

Step 1: Define a function named 'counter_clockwise' that takes in three indices: ci, cj, and ck.
Step 1.1: Check if 'ck - ci' is equal to 0 or 'ck - cj' is equal to 0 . If it is, return 'False'.
Step 1.2: Compute and present the value: 'counter' $={ }^{\prime}(x s[c j]-x s[c i]){ }^{*}(y s[c k]-y s[c i])-(y s[c j]-y s[c i]) *(x s[c k]$ - xs[ci])'.

Step 1.3: Return 'True' if 'counter' is less than or equal to 0. Otherwise, return 'False'.
Step 2: Start by setting the variable 'best' to 0.
Step 3: Iterate over each point by its index ' i ':

- If 'ys[i]' is less than 'ys[best]' OR ('ys[i]' equals 'ys[best]' AND 'xs[i]' is less than 'xs[best]'), set 'best' to i.

Step 4: Set the entry 'in_hull[best]' to 1.
Step 5: Set 'last_point' to the value of 'best'.
Step 6: Initialize the variable 'endpoint' to 0 .
Step 7: Enter into a continuous loop until specified conditions are met:
Step 7.1: For every point (by its index 'i'):
Step 7.1.1: Go to Step 1 and call the function 'counter_clockwise' with arguments 'ci' = 'last_point', 'cj' = 'endpoint', and 'ck' = 'i'. Store the result in the variable 'flag'.
Step 7.1.2: If 'endpoint' is the same as 'last_point' OR 'flag' is 'True', then set 'endpoint' to i .
After completing the loop for the current iteration:
Step 7.2: If 'in_hull[endpoint]' is greater than 0, exit the continuous loop and go to Step 8.
Step 7.3: Otherwise:
Step 7.3.1: Set 'in_hull[endpoint]' to 1.
Step 7.3.2: Update 'last_point' with the value of 'endpoint'.
Step 7.3.3: Reset 'endpoint' to 0.
Step 7.3.4: Go back to Step 7.1.
Step 8: Print the array 'in_hull'.

Now perform the computation procedure, from Step 2 to Step 8, with each line numbered sequentially (e.g., 1 .
2. 3. 4. 5. 6. etc.):

1. Step 2, set 'best' to 0 .
2. Step 3, iterate over each point by its index ' i :

- For $\mathrm{i}=0$ : $\mathrm{ys}[0]=0.6$ is not less than $\mathrm{ys}[b e s t]=y s[0]=0.6$, and $\mathrm{xs}[0]=12.79$ is not less than $\mathrm{xs}[b e s t]=x s[0]$
= 12.79 , so 'best' remains 0 .
For $\mathrm{i}=1$ : $\mathrm{ys}[1]=4.37$ is greater than $\mathrm{ys}[\mathrm{best}]=\mathrm{ys}[0]=0.6$, so 'best' remains 0.
For $\mathrm{i}=2$ : $\mathrm{ys}[2]=10.11$ is greater than $\mathrm{ys}[b e s t]=y s[0]=0.6$, so 'best' remains 0 .
For $\mathrm{i}=3$ : $\mathrm{ys}[3]=0.53$ is less than $\mathrm{ys}[$ best $]=y s[0]=0.6$, so 'best' is set to 3 .
For $\mathrm{i}=4$ : $\mathrm{ys}[4]=3.98$ is greater than $\mathrm{ys}[$ best $]=\mathrm{ys}[3]=0.53$, so 'best' remains 3 .
For $i=5: y s[5]=13.0$ is greater than $y s[b e s t]=y s[3]=0.53$, so 'best' remains 3.
For $\mathrm{i}=6$ : $\mathrm{ys}[6]=10.9$ is greater than $\mathrm{ys}[\mathrm{best}]=\mathrm{ys}[3]=0.53$, so 'best' remains 3.
For $\mathrm{i}=7$ : $\mathrm{ys}[7]=4.41$ is greater than $\mathrm{ys}[b e s t]=y s[3]=0.53$, so 'best' remains 3 .
For $\mathrm{i}=8$ : $\mathrm{ys}[8]=11.79$ is greater than $\mathrm{ys}[$ best $]=y s[3]=0.53$, so 'best' remains 3 .

3. Step 4, set 'in_hull[best]' to 1 : in_hull[3] = 1 .
4. Step 5, set 'last_point' to the value of 'best': 'last_point' $=3$.
5. Step 6, initialize 'endpoint' to 0 : 'endpoint' $=0$.
6. Step 7, enter into a continuous loop:
7.1. For every point (by its index 'í):

- For $\mathrm{i}=0$ :


2. 'ck $-\mathrm{ci}^{\prime}=0-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=0-0$ is equal to 0 , so return 'False'.
3. 'flag' = 'False'.
4. 'endpoint' remains 0 .

- For $\mathrm{i}=1$ :

1. Call 'counter_clockwise' with 'ci' ='last_point' $=3,{ }^{\prime}{ }^{c j}$ ' $=$ 'endpoint' $=0$, and 'ck' $=1$.
2. 'ck $-\mathrm{ci}^{\prime}=1-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{4}=1-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3]){ }^{*}(y s[1]-y s[3])-(y s[0]-y s[3]){ }^{*}(x s[1]-x s[3])=(12.79-4.46){ }^{*}(4.37-$
$0.53)-(0.6-0.53) *(0.5-4.46)=8.33 * 3.84-0.07 *-3.96=31.9868-0.2772=31.7096$.
4. 'counter' $=31.7096$ is greater than 0 , so return 'False'.
5. 'flag' ='False'.
6. 'endpoint' remains 0 .

- For $\mathrm{i}=2$ :

1. Call 'counter_clockwise' with 'ci' = 'last_point' $=3,{ }^{\prime} \mathrm{cj}^{\prime}=$ 'endpoint' $=0$, and 'ck' $=2$.
2. 'ck $-\mathrm{ci}^{\prime}=2-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=2-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3])$ * $(y s[2]-y s[3])-(y s[0]-y s[3]){ }^{*}(x s[2]-x s[3])=(12.79-4.46)$ * $(10.11-$
$0.53)-(0.6-0.53) *(5.5-4.46)=8.33 * 9.58-0.07 * 1.04=79.7594-0.0728=79.6866$.
4. 'counter' $=79.6866$ is greater than 0 , so return 'False'.
5. 'flag' ='False'.
6. 'endpoint' remains 0 .

- For $\mathrm{i}=3$ :

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=3,{ }^{\prime} \mathrm{cj}^{\prime}=$ 'endpoint' $=0$, and 'ck' $=3$.
2. 'ck - ci' $=3-\overline{3}$ is equal to 0 , so return 'False'.
3. 'flag' = 'False'.
4. 'endpoint' remains 0 .

- For $\mathrm{i}=4$ :

1. Call 'counter_clockwise' with 'ci' ='last_point' $=3,{ }^{\prime}{ }^{\prime}{ }^{\prime}{ }^{\prime}=$ 'endpoint' $=0$, and 'ck' $=4$.
2. 'ck - $\mathrm{ci}^{\prime}=4-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=4-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3]){ }^{*}(y s[4]-y s[3])-(y s[0]-y s[3]){ }^{*}(x s[4]-x s[3])=(12.79-4.46){ }^{*}(3.98-$
$0.53)-(0.6-0.53) *(14.73-4.46)=8.33 * 3.45-0.07 * 10.27=28.7375-0.7189=28.0186$.
4. 'counter' $=28.0186$ is greater than 0 , so return 'False'.
5. 'flag' $=$ 'False'.
6. 'endpoint' remains 0 .

- For $\mathrm{i}=5$ :

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=3$, 'ci' $=$ 'endpoint' $=0$, and ' ${ }^{\prime} k{ }^{\prime}=5$.
2. 'ck $-\mathrm{ci}^{\prime}=5-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=5-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3]){ }^{*}(y s[5]-y s[3])-(y s[0]-y s[3]){ }^{*}(x s[5]-x s[3])=(12.79-4.46) *(13.0-$
$0.53)-(0.6-0.53)^{*}(13.53-4.46)=8.33 * 12.47-0.07 * 9.07=103.8131-0.6349=103.1782$.
4. 'counter' $=103.1782$ is greater than 0 , so return 'False'.
5. 'flag' = 'False'.
6. 'endpoint' remains 0 .

- For $\mathrm{i}=6$ :

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=3,{ }^{\prime} \mathrm{cj}$ ' $=$ 'endpoint' $=0$, and 'ck' $=6$.
2. 'ck $-\mathrm{ci}^{\prime}=6-\overline{3}$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=6-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3])^{*}(y s[6]-y s[3])-(y s[0]-y s[3]) *(x s[6]-x s[3])=(12.79-4.46) *(10.9-$
$0.53)-(0.6-0.53) *(17.84-4.46)=8.33 * 10.37-0.07 * 13.38=86.2791-0.9366=85.3425$.
4. 'counter' $=85.3425$ is greater than 0 , so return 'False'.
5. 'flag' = 'False'.
6. 'endpoint' remains 0 .

- For $\mathrm{i}=7$ :

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=3$, 'cj' $=$ 'endpoint' $=0$, and 'ck' $=7$.
2. ' $\mathrm{ck}-\mathrm{ci}^{\prime}=7-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=7-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3]){ }^{*}(y s[7]-y s[3])-(y s[0]-y s[3]){ }^{*}(x s[7]-x s[3])=(12.79-4.46) *(4.41-$ $0.53)-(0.6-0.53) *(1.74-4.46)=8.33 * 3.88-0.07 *-2.72=32.3194-0.1904=32.129$.
4. 'counter' $=32.129$ is greater than 0 , so return 'False'.
5. 'flag' = 'False'.
6. 'endpoint' remains 0 .

- For i = 8:

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=3,{ }^{\prime} \mathrm{cj}^{\prime}=$ 'endpoint' $=0$, and 'ck' $=8$.
2. 'ck $-\mathrm{ci}^{\prime}=8-3$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}{ }^{\mathrm{c}}=8-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[3]){ }^{*}(y s[8]-y s[3])-(y s[0]-y s[3]) *(x s[8]-x s[3])=(12.79-4.46) *(11.79-$
$0.53)-(0.6-0.53) *(8.44-4.46)=8.33^{*} 11.26-0.07{ }^{*} 3.98=93.7868-0.2786=93.5082$.
4. 'counter' $=93.5082$ is greater than 0 , so return 'False'.
5. 'flag' ='False'.
6. 'endpoint' remains 0 .
7.2. 'in_hull[endpoint]' $=$ in_hull $[0]=0$ is not greater than 0 , so continue to Step 7.3 .
7.3.1. Set 'in_hull[endpoint]' to 1 : in_hull[0] = 1 .
7.3.2. Update 'last_point' with the value of 'endpoint': 'last_point' $=0$.
7.3.3. Reset 'endpoint' to 0 : 'endpoint' $=0$.
7.3.4. Go back to Step 7.1.
7.1. For every point (by its index 'i'):

- For $\mathrm{i}=0$ :

1. Call 'counter_clockwise' with 'ci' $=$ 'last_point' $=0,{ }^{\prime} \mathrm{cj}^{\prime}=$ 'endpoint' $=0$, and ' ${ }^{\prime} \mathrm{ck}^{\prime}=0$.
2. 'ck-ci' $=0-0$ is equal to 0 , so return 'False'.
3. 'flag' = 'False'.
4. 'endpoint' remains 0 .

- For $\mathrm{i}=1$ :

1. Call 'counter_clockwise' with 'ci' = 'last_point' $=0,{ }^{\prime}{ }^{\prime}{ }^{\text {c }}=$ 'endpoint' $=0$, and 'ck' $=1$.
2. 'ck $-\mathrm{ci}^{\prime}=1-0$ is not equal to 0 , and ' $\mathrm{ck}^{\prime}-\mathrm{cj} \mathrm{C}^{\prime}=1-0$ is equal to 0 , so return 'False'.
3. 'flag' = 'False'.
4. 'endpoint' remains 0 .

- For $\mathrm{i}=2$ :

1. Call 'counter_clockwise' with 'ci' = 'last_point' $=0,{ }^{\prime}{ }^{c j}{ }^{\prime}=$ 'endpoint' $=0$, and 'ck' $=2$.
2. 'ck-ci' $=2-0$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}{ }^{〔}=2-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[0])^{*}(y s[2]-y s[0])-(y s[0]-y s[0])^{*}(x s[2]-x s[0])=(12.79-12.79) *(10.11-$
$0.6)-(0.6-0.6) *(5.5-12.79)=0$ * $9.51-0 *-7.29=0-0=0$.
4. 'counter' $=0$ is equal to 0 , so return 'True'.
5. 'flag' = 'True'.
6. Set 'endpoint' to i: 'endpoint' $=2$.

- For $\mathrm{i}=3$ to $\mathrm{i}=8$, 'flag' will be 'False' because 'endpoint' is not the same as 'last_point' and 'counter' will be greater than 0 for all these points.
7.2. 'in_hull[endpoint] $=$ in_hull[2] $=0$ is not greater than 0 , so continue to Step 7.3 .
7.3.1. Set 'in_hull[endpoint]' to 1 : in_hull[2] = 1 .
7.3.2. Update 'last_point' with the value of 'endpoint': 'last_point' $=2$.
7.3.3. Reset 'endpoint' to 0 : 'endpoint' $=0$.
7.3.4. Go back to Step 7.1.
7.1. For every point (by its index 'i'):
- For $\mathrm{i}=0$ to $\mathrm{i}=2$, 'flag' will be 'False' because either 'ck - ci' or 'ck - cj' will be equal to 0 .
- For $\mathrm{i}=3$ :


2. 'ck $-\mathrm{ci}^{\prime}=3-2$ is not equal to 0 , and ' $\mathrm{ck}-\mathrm{cj}^{\prime}=3-0$ is not equal to 0 , so continue.
3. Compute 'counter' $=(x s[0]-x s[2]){ }^{*}(y s[3]-y s[2])-(y s[0]-y s[2]) *(x s[3]-x s[2])=(12.79-5.5) *(0.53-$
10.11) - $(0.6-10.11)^{*}(4.46-5.5)=7.29 *-9.58-9.51^{*}-1.04=-69.7938-9.8904=-79.6842$.
4. 'counter' $=-79.6842$ is less than 0 , so return 'True'.
5. 'flag' = 'True'.
6. Set 'endpoint' to i: 'endpoint' $=3$.

- For $\mathrm{i}=4$ to $\mathrm{i}=8$, 'flag' will be 'False' because 'counter' will be greater than 0 for all these points.
7.2. 'in_hull[endpoint]' $=$ in_hull[ 3$]=1$ is greater than 0 , so exit the continuous loop and go to Step 8 .

7. Step 8, print the array 'in_hull': $[1,0,1,1,0,0,0,0,0]$.

Table 39: The prompt with Python code of clrs mini numeric/jarvis march and the response of gpt-4. The correct answer shall be $[1,1,1,1,1,1,1,0,1]$, and the first mistakes are marked.

## Prompt

Execute the program step by step. Do not jump steps. Do not stop before completion.
Initial: Set the input array A: $[2,3,2,9]$.
Set the length of the array $\mathrm{n}: 4$.

```
def bubbleSort(A, n):
    for i in range(n-1):
        for j in range(0, n-i-1):
            if A[j] > A[j + 1]:
                A[j],A[j + 1] = A[j + 1], A[j]
                print(A)
    return A
```

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $i=0, A[0]=2$.
2. $j=0, A[0]>A[1]$ is False, no swap.
3. $j=1, A[1]>A[2]$ is True, $\operatorname{swap} A[1]$ and $A[2], A=[2,2,3,9]$.
4. $j=2, A[2]>A[3]$ is False, no swap.
5. $\mathrm{i}=1, \mathrm{~A}[1]=2$.
6. $j=0, A[0]>A[1]$ is False, no swap.
7. $j=1, A[1]>A[2]$ is False, no swap.
8. $i=2, A[2]=3$.
9. $j=0, A[0]>A[1]$ is False, no swap.
10. $i=3$, the loop ends.

11 . The sorted array is $[2,2,3,9]$.
Table 40: The prompt with Python code of bubble sort and the response of gpt-4.

## Prompt

Execute the program step by step. Do not jump steps. Do not stop before completion. When reading or updating an array at some index, use concrete values rather than just variables.

Initial: Given a pattern string pat of length M and a text string txt of length N .
pat: $\operatorname{pat}[0]=A, \operatorname{pat}[1]=A, \operatorname{pat}[2]=B, M=3$.
$\operatorname{txt}: \operatorname{txt}[0]=\mathrm{C}, \operatorname{txt}[1]=\mathrm{A}, \operatorname{txt}[2]=\mathrm{A}, \operatorname{txt}[3]=\mathrm{B}, \mathrm{N}=4$.
Create an array $\operatorname{lps}[]$ of length $M$ with the value of $0: \operatorname{lps}[0]=0, \operatorname{lps}[1]=0, \operatorname{lps}[2]=0$.
def KMPSearch(pat, txt):

$$
\begin{aligned}
& M=\operatorname{len}(p a t) \\
& N=\operatorname{len}(\mathrm{txt}) \\
& \mathrm{Ips}=[0]^{*} M
\end{aligned}
$$

```
    i=1
```

    while i < M :
        if pat[i] == pat[length]:
            length \(+=1\)
            \(\operatorname{lps}[i]=\) length
            \(i+=1\)
        else:
            if length ! \(=0\) :
                    length_prev = length -1
                    length \(=\mid \mathrm{lps}\) [length_prev]
            else:
                    \(\operatorname{lps}[i]=0\)
                    i \(+=1\)
    res \(=[]\)
    while ( \(N-i\) ) >=( \(M-j\) ):
        if pat[j] \(==\) txt[i]:
                i += 1
                \(j+=1\)
        if \(\mathrm{j}=\mathrm{M}\) :
                found_index \(=\mathrm{i}-\mathrm{j}\)
                \(\mathrm{j}=\operatorname{lps}[\mathrm{j}-1]\)
            elif i < N and pat[j] != txt[i]:
                if j ! \(=0\) :
                    \(\mathrm{j}=\operatorname{lps}[\mathrm{j}-1]\)
                else:
                    \(i+=1\)
    return res
    The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

2. Initialize $M=3, N=4, \operatorname{lps}[0]=0, \operatorname{lps}[1]=0, \operatorname{lps}[2]=0$, length $=0$, and $i=1$.
3. Enter the while loop with the condition $\mathrm{i}<\mathrm{M}(1<3)$.
4. Check if pat[i] == pat[length] (pat[1] == pat[0], $A=A$ ). Since it's true, increment length by 1 (length $=1$ ), set $\operatorname{lps}[i]=$ length $(\operatorname{lps}[1]=1)$, and increment i by $1(\mathrm{i}=2)$.
5. Continue the while loop with the condition $\mathrm{i}<\mathrm{M}(2<3)$.
6. Check if pat[i] == pat[length] (pat[2] $==$ pat[1], $B=A$ ). Since it's false, check if length $!=0(1!=0)$. Since it's true, set length_prev = length -1 (length_prev = 0 ), set length $=\operatorname{lps}[$ length_prev] (length $=l p s[0]$, length $=0)$.
7. Continue the while loop with the condition $\mathrm{i}<\mathrm{M}(2<3)$.
8. Check if pat[i] == pat[length] (pat[2] ==pat[0], B = A). Since it's false, check if length $!=0(0!=0)$. Since it's false, set $\operatorname{lps}[i]=0(\operatorname{lps}[2]=0)$ and increment $i$ by $1(i=3)$.
9. Exit the while loop since the condition $\mathrm{i}<\mathrm{M}(3<3)$ is false.
10. Print $\operatorname{lps}[]: \operatorname{lps}[0]=0, \operatorname{lps}[1]=1, \operatorname{lps}[2]=0$.
11. Initialize $i=0, j=0$, and res $=[]$.
12. Enter the while loop with the condition $(N-i)>=(M-j)(4-0>=3-0)$.
13. Check if pat[j] $==\operatorname{txt}[i]$ (pat[ $[0]==\operatorname{txt}[0], A==C)$. Since it's false, check if $j!=0(0!=0)$. Since it's false, increment $i$ by $1(i=1)$.
14. Continue the while loop with the condition $(N-i)>=(M-j)(4-1>=3-0)$.
15. Check if pat[ $[\mathrm{j}==\operatorname{txt[i]}(\operatorname{pat}[0]==\operatorname{txt}[1], A==A)$. Since it's true, increment i by $1(\mathrm{i}=2)$ and increment j by $1(\mathrm{j}=$ 1).
16. Continue the while loop with the condition $(N-i)>=(M-j)(4-2>=3-1)$.
17. Check if pat[j] ==txt[i] (pat[1] ==txt[2],A==A). Since it's true, increment $i$ by $1(i=3)$ and increment $j$ by $1(j=$ 2).
18. Continue the while loop with the condition $(N-i)>=(M-j)(4-3>=3-2)$.
19. Check if pat[j] ==txt[i] (pat[2] ==txt[3],B==B). Since it's true, increment i by $1(i=4)$ and increment $j$ by $1(j=$ $3)$.
20. Check if $j==M(3==3)$. Since it's true, set found_index $=i-j$ (found_index $=4-3$, found_index $=1)$, append found_index to res (res = [1]), and set $j=\operatorname{lps}[j-1](j=\overline{l p s}[2], j=0)$.
21. Exit the while loop since the condition $(N-i)>=(M-j)(4-4>=3-0)$ is false.
22. Return res, which is [1].

Table 41: The prompt with Python code of kmp matcher and the response of gpt-4.

## Prompt

Execute the program step by step. Do not jump steps. Do not stop before completion.
Initial: Set the deadlines array d : $\mathrm{d}[0]=1, \mathrm{~d}[1]=2, \mathrm{~d}[2]=4, \mathrm{~d}[3]=3, \mathrm{~d}[4]=4$.
Set the deadlines array W : $\mathrm{W}[0]=4, \mathrm{~W}[1]=7, W[2]=48, \mathrm{~W}[3]=69, W[4]=77$.
Set the length of the arrays n : 5 .
Set the maximum time slots t: 4 .
Initialize an array called 'result': [False, False, False, False, False].
Initialize an array called 'job': $[-1,-1,-1,-1,-1]$.
def printJobScheduling(d, t):
for i in range( n ):
for j in range $(\min (\mathrm{t}, \mathrm{d}[\mathrm{i}]),-1,-1)$ :
if result[j] is False:
result[j] = True
job[j] = i
print(job)
break
return job

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. etc.):

1. $i=0$.
2. $\mathrm{j}=1($ since $\min (\mathrm{t}, \mathrm{d}[0])=\min (4,1)=1)$.
3. result[1] is False, so set result[1] to True and job[1] to 0 . Print job: $[-1,0,-1,-1,-1]$.
4. $i=1$.
5. $\mathrm{j}=2($ since $\min (\mathrm{t}, \mathrm{d}[1])=\min (4,2)=2)$.
6. result[2] is False, so set result[2] to True and job[2] to 1. Print job: $[-1,0,1,-1,-1]$.
7. $i=2$.
8. $\mathrm{j}=4($ since $\min (\mathrm{t}, \mathrm{d}[2])=\min (4,4)=4)$.
9. $j=3$ (since result[4] is not in the array, decrement $j$ ).
10. result[3] is False, so set result[3] to True and job[3] to 2. Print job: $[-1,0,1,2,-1]$.
11. $\mathrm{i}=3$.
12. $j=3$ (since $\min (t, d[3])=\min (4,3)=3)$.
13. result[3] is True, so decrement $j$ to 2.
14. result[2] is True, so decrement $j$ to 1.
15. result[1] is True, so decrement $j$ to 0 .
16. result[0] is False, so set result[0] to True and job[0] to 3. Print job: $[3,0,1,2,-1]$.
17. $\mathrm{i}=4$.
18. $j=4$ (since $\min (t, d[4])=\min (4,4)=4)$.
19. $j=3$ (since result[4] is not in the array, decrement $j$ ).
20. result[3] is True, so decrement $j$ to 2.
21. result[2] is True, so decrement $j$ to 1.
22. result[1] is True, so decrement $j$ to 0 .
23. result[0] is True, so no free slot is found for job 4.
24. The loop is finished, so return the final job sequence: $[3,0,1,2,-1]$.

Table 42: The prompt with Python code of task scheduling and the response of gpt-4. The correct answer shall be $[4,0,1,3,2]$, and the first mistake is at line 9.

```
Prompt
Execute the following program.
Initial: Set the array p of length N-1 = 4: p[0] = 0.02, p[1] = 0.21, p[2] = 0.23, p[3] = 0.07 and q of length N = 5:
q[0] = 0.13, q[1] = 0.16, q[2] = 0.11, q[3] = 0.06, q[4] = 0.01 respectively.
Set the matrix e and w of size 5 x 5 with all elements initialized to 0.
Set maxint: }66666666
def optimal_bst(p, q, N):
    # p and q are both lists with length N.
    # N = len(p)
    e = np.zeros((N,N))
    w = np.zeros((N,N))
    for i in range(N):
        e[i, i] = q[i]
        w[i, i] = q[i]
    for l in range(1,N):
        upper_i = N - I
        for i in range(upper_i):
            j=i+l
            e[i, j] = 66666666
            w[i, j] = w[i, j - 1] + p[j - 1] + q[j]
            for r in range(i, j):
                    t = e[i, r] +e[r + 1, j] + w[i, j]
            e[i, j] = min(e[i, j], t)
            print(i, j, r, e[i]j])
    return e[0, N-1]
```

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. etc.):

1. $\mathrm{i}=0,0<=3, \mathrm{e}[0][0]=\mathrm{q}[0]=0.13, \mathrm{w}[0][0]=\mathrm{q}[0]=0.13$.
2. $\mathrm{i}=1,1<=3, \mathrm{e}[1][1]=\mathrm{q}[1]=0.16, \mathrm{w}[1][1]=\mathrm{q}[1]=0.16$.
3. $\mathrm{i}=2,2<=3, \mathrm{e}[2][2]=\mathrm{q}[2]=0.11, \mathrm{w}[2][2]=\mathrm{q}[2]=0.11$.
4. $\mathrm{i}=3,3<=3, \mathrm{e}[3][3]=\mathrm{q}[3]=0.06, \mathrm{w}[3][3]=\mathrm{q}[3]=0.06$.
5. $I=1, i=0, j=1, w[0][1]=w[0][0]+p[0]+q[1]=0.13+0.02+0.16=0.31$.
6. $r=0, e[0][1]=\min (66666666, e[0][0]+e[1][1]+w[0][1])=\min (66666666,0.13+0.16+0.31)=0.60$.
7. $I=1, i=1, j=2, w[1][2]=w[1][1]+p[1]+q[2]=0.16+0.21+0.11=0.48$.
8. $r=1, e[1][2]=\min (66666666, e[1][1]+e[2][2]+w[1][2])=\min (66666666,0.16+0.11+0.48)=0.75$.
9. $I=1, i=2, j=3, w[2][3]=w[2][2]+p[2]+q[3]=0.11+0.23+0.06=0.40$.
10. $r=2, e[2][3]=\min (66666666, e[2][2]+e[3][3]+w[2][3])=\min (66666666,0.11+0.06+0.40)=0.57$.
11. $I=2, i=0, j=2, w[0][2]=w[0][1]+p[1]+q[2]=0.31+0.21+0.11=0.63$.
12. $r=0, e[0][2]=\min (66666666, e[0][0]+e[1][2]+w[0][2])=\min (66666666,0.13+0.75+0.63)=1.51$.
13. $r=1, \mathrm{e}[0][2]=\min (1.51, \mathrm{e}[0][1]+\mathrm{e}[2][2]+\mathrm{w}[0][2])=\min (1.51,0.60+0.11+0.63)=1.34$.
14. $I=2, i=1, j=3, w[1][3]=w[1][2]+p[2]+q[3]=0.48+0.23+0.06=0.77$.
15. $r=1, e[1][3]=\min (66666666, e[1][1]+e[2][3]+w[1][3])=\min (66666666,0.16+0.57+0.77)=1.50$.
16. $r=2, e[1][3]=\min (1.50, e[1][2]+e[3][3]+w[1][3])=\min (1.50,0.75+0.06+0.77)=1.58$.
17. $I=3, i=0, j=3, w[0][3]=w[0][2]+p[2]+q[3]=0.63+0.23+0.06=0.92$.
18. $r=0, e[0][3]=\min (66666666, e[0][0]+e[1][3]+w[0][3])=\min (66666666,0.13+1.58+0.92)=2.63$.
19. $r=1, \mathrm{e}[0][3]=\min (2.63, \mathrm{e}[0][1]+\mathrm{e}[2][3]+\mathrm{w}[0][3])=\min (2.63,0.60+0.57+0.92)=2.09$.
20. $r=2, \mathrm{e}[0][3]=\min (2.09, \mathrm{e}[0][2]+\mathrm{e}[3][3]+\mathrm{w}[0][3])=\min (2.09,1.34+0.06+0.92)=2.32$.

The final result is $\mathrm{e}[0][3]=2.09$.
Table 43: The prompt with Python code of optimal binary search tree and the response of gpt-4. The correct answer shall be 2.4, and line 12 and 16 are wrong.

## Prompt

Execute the program step by step. Do not jump steps. Do not stop before completion. When updating an array, use concrete values rather than variables.
Initial: Set the square matrix A of size $4 \times 4$ :
$A[0,0]=0, A[0,1]=0, A[0,2]=0, A[0,3]=1$
$A[1,0]=1, A[1,1]=0, A[1,2]=0, A[1,3]=0$
$A[2,0]=0, A[2,1]=0, A[2,2]=0, A[2,3]=0$
$A[3,0]=1, A[3,1]=0, A[3,2]=1, A[3,3]=0$.
Set color: color[0] = 0, color[1] $=0$, color[2] $=0$, color[3] $=0$.
Set topo: topo[0] = 0, topo[1] = 1, topo[2] = 2, topo[3] = 3 .
Set s_prev: s_prev[0] $=0, \mathrm{~s} \_$prev[1] $=1$, $s \_$prev[2] $=2$, s_prev[3] $=3$.
Set topo_head: 0 .
Set s: 0 .
def dfs(A):
$\mathrm{N}=$ A.shape[0]
color $=n$ n.zeros $(\mathrm{N}$, dtype $=\mathrm{np} . i n t 32)$
topo $=$ np. .arange( N )
s_prev = np.arange(N)
topo_head $=0$
for $s$ in range( N ):
if color[s] $==0$ :
s_last = s
$u=s$
while True:
if color[u] $==0$ : color[u] = 1
for $v$ in range $(N)$ :
if $\mathrm{A}[\mathrm{u}, \mathrm{v}]!=0$ :
if color[v] == 0 :
color[v] = 1
s_prev[v] = s_last
s_last $=\mathrm{v}$
break
if s_last == u:
color[u] = 2
if color[topo_head] $==2$ :
topo[u] = topo_head
topo_head $=u$
if s_prev[u] == u: break
pr $=$ s_prev[s_last]
s_prev[s_last] = s_last
s_last = pr
$\mathrm{u}=\mathrm{s}$ last
return topo

The computation procedure is as follows, with each line numbered sequentially (e.g., 1. 2. 3. 4. 5. 6. 7. 8. 9. etc.):

1. $s=0,0<4$. Since color[ 0$]==0$, set $s \_$last $=0, u=0$.
```
2. color[0] \(=1\).
3. For \(v=0, A[0,0]=0\), go to next \(v\).
4. For \(v=1, A[0,1]=0\), go to next \(v\).
5. For \(v=2, A[0,2]=0\), go to next \(v\).
6. For \(v=3, A[0,3]=1\), color \([3]=1\), s_prev[3] \(=0\), s_last \(=3\).
7. \(\operatorname{color}[3]=2\), color \([0]=2\), topo[3] \(=0\), topo_head \(=3\), s_prev[3] \(=3\).
8. \(s=1,1<4\). Since color[1] \(==0\), set \(s \_\)last \(=1, u=1\).
9. color[1] = 1 .
10. For \(v=0, A[1,0]=1\), color \([0]=2\), go to next \(v\).
11. For \(v=1, A[1,1]=0\), go to next \(v\).
12. For \(v=2, A[1,2]=0\), go to next \(v\).
13. For \(v=3, A[1,3]=0\).
14. \(\operatorname{color}[1]=2\), color[3] \(=2\), topo[1] \(=3\), topo_head \(=1\), s_prev[1] = 1 .
15. \(s=2,2<4\). Since color[2] \(==0\), set s_last \(=2, u=2\).
16. \(\operatorname{color}[2]=1\).
17. For \(v=0, A[2,0]=0\), go to next \(v\).
18. For \(v=1, A[2,1]=0\), go to next \(v\).
19. For \(v=2, A[2,2]=0\), go to next \(v\).
20. For \(v=3, A[2,3]=0\).
21. color[2] = 2, color[1] = 2, topo[2] = 1, topo_head = 2, s_prev[2] = 2 .
22. \(s=3,3<4\). Since color \([3]==2\).
23. \(s=4,4>=4\), stop.
The final topo array is \([3,1,2,0]\).
```

Table 44: The prompt with Python code of topological sort and the response of gpt-4. The correct answer shall be $[0,0,2,3]$, and the first mistake is at line 7.


[^0]:    * Corresponding Authors

[^1]:    - Bubble Sort: the number list $A$.

