Know When to Fuse: Investigating Non-English Hybrid Retrieval in the Legal Domain

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Abstract

Hybrid search has emerged as an effective strategy to offset the limitations of different matching paradigms, especially in out-of-domain contexts where notable improvements in retrieval quality have been observed. However, existing research predominantly focuses on a limited set of retrieval methods, evaluated in pairs on domain-general datasets exclusively in English. In this work, we study the efficacy of hybrid search across a variety of prominent retrieval models within the unexplored field of law in the French language, assessing both zero-shot and in-domain scenarios. Our findings reveal that in a zero-shot context, fusing different domaingeneral models consistently enhances performance compared to using a standalone model, regardless of the fusion method. Surprisingly, when models are trained in-domain, we find that fusion generally diminishes performance relative to using the best single system, unless fusing scores with carefully tuned weights. These novel insights, among others, expand the applicability of prior findings across a new field and language, and contribute to a deeper understanding of hybrid search in non-English specialized domains.¹

1 Introduction

Information retrieval is typically addressed through one of two fundamental matching paradigms: (i) *lexical matching*, which relies on an exact match of terms between queries and documents; and (ii) *semantic matching*, which measures complex relationships between words to capture underlying semantics. Lexical matching is simple, efficient, and generally effective across various domains (Thakur et al., 2021). However, it suffers from the vocabulary gap issue (Berger et al., 2000), where relevant information might not explicitly include query



Figure 1: A high-level illustration of the hybrid search workflow based on various sparse and dense retrievers.

terms yet still fulfills the actual informational needs. Semantic models remedy vocabulary mismatches by learning to model semantic similarity, resulting in significant in-domain performance gains (Qu et al., 2021; Xiong et al., 2021; Hofstätter et al., 2021). Nevertheless, these models tend to exhibit limited generalization across unseen topics (Thakur et al., 2021), which is particularly problematic in highly specialized domains, like law, where highquality labeled data is both scarce and costly.

Recent works suggest that combining these two paradigms can enhance retrieval quality (Kuzi et al., 2020; Wang et al., 2021; Ma et al., 2021), particularly in out-of-distribution settings (Chen et al., 2022; Bruch et al., 2024), as they tend to mitigate each other's limitations. However, these efforts have mostly been limited to combining no more than two systems – typically pairing BM25 (Robertson et al., 1994) with single-vector dense bi-encoders (Reimers and Gurevych, 2019) – while constraining evaluation to English datasets only.

Our work aims to extend this scope by investigating the potential synergies among a broader range of retrieval models, encompassing both sparse and dense methods, specifically within the uncharted *legal* domain in the *French* language, as illustrated

¹Our source code and models are available at https: //github.com/maastrichtlawtech/fusion.

in Figure 1. Our contributions are threefold:

- First, we investigate the efficacy of combining diverse domain-general retrieval models for legal retrieval, assuming *no* domain-specific labeled data is available a highly usual scenario in specialized domains like law.
- Second, we explore the extent to which specialized retrievers and their fusion can impact in-domain performance, assuming *limited* domain-specific training data is available.
- Finally, we release all our learned retrievers, including the first French SPLADE and Col-BERT models for general and legal domains.

2 Methodology

Assuming that different matching paradigms may be complementary in how they model relevance (Chen et al., 2022; Bruch et al., 2024), we aim to explore the potential of combining various systems to enhance performance on French legal retrieval. In this section, we outline the retrieval models (§2.1), fusion techniques (§2.2), and experimental setup (§2.3) employed in our study, with additional comprehensive details available in Appendix A.

2.1 Retrieval Models

We select several prominent retrieval methods representing diverse matching paradigms, all demonstrating high effectiveness in prior studies. Specifically, we explore the unsupervised BM25 weighting scheme (Robertson et al., 1994), our own singlevector dense (Lee et al., 2019; Chang et al., 2020; Karpukhin et al., 2020), multi-vector dense (Khattab and Zaharia, 2020; Santhanam et al., 2022b), and single-vector sparse (Formal et al., 2021a,b) bi-encoder models - respectively dubbed DPR_{FR}, ColBERT_{FR}, and SPLADE_{FR} – and a cross-attention model (Nogueira and Cho, 2019; Han et al., 2020; Gao et al., 2021a) termed monoBERT_{FR}. Following a preliminary comparative analysis of various pretrained French language models in Appendix B.1, we choose CamemBERT_{BASE} (Martin et al., 2020) as the backbone encoder for all our supervised neural retrievers. We refer readers to Appendix A.1 for detailed explanations of each method's relevance matching and optimization processes.

2.2 Fusion Techniques

To leverage existing retrieval methods without modifications, our study explores *late* fusion techniques, which aggregate results post-prediction – in contrast to early fusion methods that merge latent representations of distinct retrievers within the feature space prior to making predictions. In this context, the relevance of a candidate can be assessed using two main measures: its position in the ranked list or its predicted score. This distinction underpins the two primary late fusion approaches explored in this study: *score-based* and *rank-based* fusion. Specifically, we investigate *normalized score fusion* (NSF; Lee, 1995) with various scaling techniques, *Borda count fusion* (BCF; Ho et al., 1994), and *reciprocal rank fusion* (RRF; Cormack et al., 2009). See Appendix A.2 for detailed definitions of each method.

2.3 Experimental Setup

Datasets. We exploit two French text ranking datasets: the domain-general mMARCO-fr (Bonifacio et al., 2021) and the domain-specific LLeQA (Louis et al., 2024). The former is a translated version of MS MARCO (Nguyen et al., 2018) in 13 languages, including French. It comprises a corpus of 8.8M passages, 539K training queries, and 6980 development queries. LLeQA targets longform question answering and information retrieval within the legal domain. It consists of 1,868 Frenchnative questions on various legal topics, distributed across training (1472), development (201), and test (195) sets. Each question is expertly annotated with references to relevant legal provisions drawn from a corpus of 27,942 Belgian law articles.

Evaluation metrics. To measure effectiveness, we use official metrics for each dataset: mean reciprocal rank at cutoff 10 (MRR@10) for mMARCO, and average r-precision (RP) for LLeQA. Both metrics are rank-aware, meaning they are sensitive to variations in the ordering of retrieved results. Additionally, we report the rank-unaware recall measure at various cutoffs (R@k), which is particularly useful for assessing performance of first-stage retrievers. See Appendix A.3 for details.

Baselines. We evaluate our learned retrievers and their hybrid configurations against leading opensource multilingual retrieval models, including BM25 (Robertson et al., 1994), mE5 (Wang et al., 2024) in its small, base, and large variants, and BGE-M3 (Chen et al., 2024) in its dense version.

2.4 Efficiency

To evaluate the practicality of each system for realworld deployment, we assess their computational and memory efficiency during inference.

	Medal	mMAR	CO-fr	Model	Size	#Sa	mples	Batc	h Size	Hardv	vare
	Widdel	MRR@10	R@500	#Params	RAM	PF	F	PF	F	Pre-Finetune	Finetune
Baselines											
1	BM25 $(k1=0.9, b=0.4)$	0.143	0.681	-	-	-	-	-	-	-	-
2	mE5 _{small}	0.297	0.908	117.7M	0.5GB	1B	1.6M	32k	512	32×V100	8×V100
3	$mE5_{BASE}$	0.303	0.914	278.0M	1.1GB	1B	1.6M	32k	512	64×V100	8×V100
4	$mE5_{Large}$	<u>0.311</u>	0.909	559.9M	2.2GB	1B	1.6M	32k	512	Unk.	8×V100
5	$BGE\text{-}M3_{\text{dense}}$	0.270	0.891	567.8M	2.3GB	1.2B	1.6M	67k	1.2k	96×A800	$24 \times A800$
Lea	rned models (ours)										
6	DPR _{FR-BASE}	0.285	0.891	110.6M	0.4GB	-	0.5M	-	152	-	$1 \times V100$
7	SPLADE _{FR-BASE}	0.247	0.860	110.6M	0.4GB	-	0.5M	-	128	-	1×H100
8	ColBERT _{FR-BASE}	0.295 [†]	0.884^{\dagger}	110.6M	0.4GB	-	0.5M	-	128	-	1×H100
9	$monoBERT_{FR-BASE}$	0.334*	0.965*	110.6M	0.4GB	-	0.5M	-	128		1×H100
† Eva	aluated using the PLAID retriev	al engine (Santhar	am et al., 2022	a). * Evaluate	d by re-rankii	ng 1k candi	dates includi	ng gold ar	nd hard neg	ative passages.	

Table 1: Retrieval results on mMARCO-fr small dev set (in-domain). We report each model's training resources.

Index size. We start by calculating the storage footprint of the indexed LLeQA articles, precomputed offline and loaded at inference, noting that the indexing method varies with the retrieval approach. Sparse methods like BM25 and SPLADE use inverted indexes, which store each vocabulary term along lists of articles containing the term and its frequency within those articles. Single-vector dense models, such as DPR_{FR}, mE5, and BGE-M3, rely on flat indexes for brute-force search, sequentially storing vectors on $d \times b \times |\mathcal{C}|$ bits given d-dimensional representations of articles from corpus C encoded in b bits (with b=32 in our study).² Meanwhile, ColBERT uses an advanced centroid-based indexing to store late-interaction token embeddings, with a footprint comparable to dense flat indexes (Santhanam et al., 2022b).

Retrieval latency. We then measure the retrieval latency per query in seconds. We use a query batch size of one to simulate streaming queries and compute the average latency across all queries in the LLeQA dev set. Measurements are conducted on a single NVIDIA H100 for GPU search and an AMD EPYC 7763 for CPU search.

Inference FLOPs. Finally, we estimate the number of floating point operations (FLOPs) per query as a hardware-agnostic measure of compute usage. Details of our estimation methodology across the different systems are provided in Appendix A.4.

3 Zero-Shot Evaluation

In this section, we investigate the out-of-domain generalization capabilities of modern retrieval mod-

els trained on a budget and explore the efficacy of their fusion in the specialized domain of law. Specifically, we explore the following question: Assuming a lack of domain-specific labeled data and limited computational resources, how effectively can hybrid combinations of domain-general retrieval models perform within the legal domain? To address this, we train the supervised retrieval models presented in Section 2 on the French segment of the domain-general mMARCO dataset. We denote the resulting models with the FR-BASE subscript throughout the rest of the paper.

Main results. When evaluated on mMARCO-fr, our learned French retrievers exhibit competitive, and at times superior, in-domain performance compared to leading multilingual retrieval models. This is particularly notable given their relatively smaller size and the constrained resources used during training, as shown in Table 1. For instance, $DPR_{FR-BASE}$ surpasses BGE-M3_{DENSE} with only one-fifth of its parameters, 2400× fewer training samples, and significantly less training compute. Additionally, our cross-encoder consistently outperforms all other retrieval methods, corroborating prior findings on the efficacy of cross-attention (Hofstätter et al., 2020). However, results in Table 2 reveal that, when evaluated in the legal domain, our domain-general French retrievers generally underperform against the multilingual baselines, except for our crossencoder which remains competitive at smaller cutoffs. This discrepancy is largely due to the baselines' extensive (pre-)finetuning across diverse data with large batch sizes – which proved beneficial for enhanced contrastive learning (Qu et al., 2021). Surprisingly, BM25 outperforms all neural models in this specialized context, reaffirming its robustness when dealing with out-of-distribution data.

²While ANNS indexes such as HNSW (Malkov et al., 2014) enable more efficient retrieval, they introduce significant overhead which makes flat indexes generally preferable for smaller datasets like LLeQA (Milvus, 2022; Redis, 2024).

Model			LLeQA		Index St	orage	Latenc	:y (s/q)	FI OD:
	Widdel		R@10	R@500	Disk*	Ratio [*]	GPU	CPU	FLOPS
Base	lines								
1	BM25 $(k1=2.5, b=0.2)$	0.163	0.367	0.672	6.6MB	$\times 0.2$	-	0.142	1.7e+6
2	mE5 _{small}	0.081	0.174	0.611	40.9MB	$\times 1.5$	0.013	0.028	6.6e+8
3	$mE5_{BASE}$	0.074	0.157	0.653	81.9MB	$\times 2.9$	0.014	0.065	2.6e+9
4	$mE5_{LARGE}$	0.074	0.194	0.695	109.1MB	$\times 3.9$	0.022	0.121	9.2e+9
5	$BGE-M3_{dense}$	0.090	0.325	0.734	109.1MB	$\times 3.9$	0.023	0.113	9.2e+9
Lear	rned models (ours)								
6	DPR _{FR-BASE}	0.046	0.146	0.590	81.9MB	$\times 2.9$	0.013	0.057	2.6e+9
7	SPLADE _{fr-base}	0.045	0.107	0.596	30.2MB	$\times 1.1$	0.013	0.609	2.6e+9
8	ColBERT _{FR-BASE}	0.047^{\dagger}	0.148^{\dagger}	0.517^{\dagger}	185.8MB [†]	$\times 6.7$	0.031 [†]	0.142^{\dagger}	2.6e+11
9	$monoBERT_{FR-BASE}$	0.102	0.290	0.536	-	-	4.472*	184.7^{\star}	2.2e+13*
Hyb	rid combinations								
10	$NSF_{z-score}(1,7)$	0.130	0.372	0.755	36.8MB	$\times 1.3$	-	-	2.6e+9
11	$NSF_{MIN-MAX}(1, 8)$	0.134	0.397	0.746	192.4MB	$\times 6.9$	-	-	2.6e+11
12	$NSF_{z-score}(1, 6, 7)$	0.092	0.354	0.742	118.7MB	$\times 4.3$	-	-	5.2e+9
13	$NSF_{z-score}(1, 7, 8)$	0.109	<u>0.399</u>	0.753	222.6MB	$\times 8.0$	-	-	5.2e+9
14	$NSF_{z-score}(1, 6, 8)$	<u>0.139</u>	0.407	0.750	274.3MB	$\times 9.8$	-	-	2.6e+11
15	$NSF_{z-score}(1, 6, 7, 8)$	0.125	0.388	0.736	304.5MB	$\times 10.9$	-	-	2.7e+11
+ Ecti	moted with 22 hit precision for d	ansa vaatars	Potio of inc	lov size to plai	n toxt size				

Table 2: Retrieval results on LLeQA test set (zero-shot). We report performance of the best hybrid configurations obtained after extensive evaluation on LLeQA dev set (see Table 3).

Besides, BM25 is notably efficient at inference, with an index up to $30 \times$ smaller and significantly fewer FLOPs than neural retrievers. In contrast, the full interaction mechanism of $monoBERT_{FR-BASE}$ incurs substantial computational costs, resulting in latencies up to $350 \times$ and $2350 \times$ higher on GPU and CPU, respectively, than the other learned French models - while assessed to re-rank 1,000 candidates only rather than the whole corpus. ColBERT_{FR-BASE}, with its token-to-token interaction, achieves reasonable latencies on both GPU and CPU due to the low-level optimization of PLAID, but results in a larger index. Meanwhile, SPLADE_{FR-BASE} stands out among neural methods by using an inverted index nearly $3 \times$ smaller than that of its single-vector dense counterpart.

Finally, we observe that fusing BM25 with one or more of our learned domain-general French models consistently and significantly outperforms all individual retrievers in the zero-shot setting (except on RP where BM25 excels) yet at the expense of increased memory - but comparable latencies when using parallelization. This fusion markedly enhances recall at large cutoffs compared to standalone BM25. On recall@10, most fusions improve upon BM25; notably, the BM25+DPR_{FR-BASE}+ColBERT_{FR-BASE} fusion shows a 4% enhancement and surpasses both DPR_{FR-BASE} and ColBERT_{FR-BASE} by around 26%. Surprisingly, the BM25+SPLADE_{FR-BASE} fusion is the most effective on R@500 while standing out for its efficiency due to both methods' use of inverted indexes.

How do score distributions vary across models? Figure 2 depicts the score distributions of end-toend retrievers, normalized using both traditional techniques and our proposed percentile normalization. We find that traditional scaling methods lead to misaligned distributions among retrievers, particularly under min-max scaling. Such misalignment impacts score fusion as identical scores may convey different levels of relevance across systems. For example, a min-max normalized score of 0.35 approximates the median for DPR_{FR-BASE}, but corresponds to the 95th percentile for BM25. When these scores are equally combined, the higher relevance indicated by BM25's score is therefore negated. To address this, we explore a new scaling approach that maps scores to their respective percentiles within each system's overall score distribution, estimated using around 5.6 million data points per system. This way, a score of 0.35 is adjusted to 0.5 for DPR_{FR-BASE} and 0.95 for BM25, leading to a relatively higher fused score that favors high relevance signals. This method requires pre-computing each retriever's score distribution, ideally with a volume matching the corpus size to avoid score collisions. Despite its intuitive appeal, our empirical findings reveal that this percentile-based scaling does not surpass traditional methods, as shown in Table 3.

How complementary are distinct retrievers? We select the two systems that showed the best hybrid sparse-dense performance in Table 3, namely BM25+ColBERT_{FR-BASE}, and analyze their min-max scaled scores across 18.6K query-article pairs from



Figure 2: Score distributions of domain-general end-to-end retrievers, normalized using min-max, z-score, and percentile scaling. The distributions are derived from ranking all 27,942 articles in LLeQA's knowledge corpus against the 201 development set queries, resulting in approximately 5.6 million scores per system.



Figure 3: Illustration of the complementary relationship between a sparse (BM25) and a dense (ColBERT_{FR-BASE}) system on out-of-distribution data. Scores have been min-max normalized and categorized into four distinct regions based on each system's global distribution, depicted in Figure 2.

LLeQA, balanced between positive and negative instances. We examine four scenarios: (A) BM25 scores high (above the third quartile of its distribution, depicted in Figure 2) while ColBERT_{FR-BASE} scores low (below the first quartile of its distribution); (B) BM25 scores low while ColBERT_{FR-BASE} scores high; (C) both systems score high; (D) both systems score low. Our findings, shown in Figure 3, reveal that when one system scores high while the other does not, the higher-scoring system generally provides the correct signal, effectively compensating for the other's error. Conversely, when both systems concur on the relevance assessment, whether high or low, they are predominantly correct.

Does fusion always help for OOD data? We conduct an exhaustive evaluation across all possible combinations of our learned retrievers (excluding the monoBERT_{FR-BASE} re-ranker due to its high inefficiency for end-to-end retrieval) and BM25, using the fusion methods presented in Section 2.

For NSF, we test both conventional min-max and z-score scaling, as well as our proposed percentile normalization, with either equal or tuned weights. This results in a total of 88 different configurations, whose results are presented in Table 3. Of these, we find that 72 (i.e., 82%) improve performance compared to using the retrievers from the respective combinations individually. Remarkably, nine combinations outperform the extensively trained BGE-M3_{DENSE} model, which demonstrates the best individual performance by far on LLeQA dev set. Overall, our findings indicate that fusion almost always enhances performance on out-of-distribution data, regardless of the fusion technique or normalization approach used - though tuned NSF with z-score scaling seems to deliver optimal results.

4 In-Domain Evaluation

We now investigate the performance enhancement given by specialized retrievers trained in the le-

	Method		DDF	NSF	MIN-MAX	NSF	Z-SCORE	NSF	ERCENTILE
			КЛГ	Equal	Tuned	Equal	Tuned	Equal	Tuned
	BM25	0.232	0.232	0.232	0.232	0.232	0.232	0.232	0.232
gle	DPR _{FR-BASE}	0.184	0.184	0.184	0.184	0.184	0.184	0.184	0.184
Sing	SPLADE _{FR-BASE}	0.180	0.180	0.180	0.180	0.180	0.180	0.180	0.180
þ	ColBERT _{FR-BASE}	0.232	0.232	0.232	0.232	0.232	0.232	0.232	0.232
rse	BM25 + SPLADE _{FR-BASE}	0.262	0.279	0.295	0.295	0.286	0.300^{\dagger}	0.282	0.286
Spa / dei	$DPR_{FR-BASE} + ColBERT_{FR-BASE}$	0.219	0.230	0.229	0.243	0.227	0.243	0.206	0.228
rse ns	BM25 + DPR _{FR-BASE}	0.233	0.262	0.268	0.276	0.265	0.286	0.257	0.257
-spa	$BM25 + ColBERT_{FR-BASE}$	0.249	0.269	0.293	0.303^{\dagger}	0.262	0.294	0.261	0.266
se+ 2 sy	$SPLADE_{FR-BASE} + DPR_{FR-BASE}$	0.188	0.203	0.196	0.217	0.197	0.218	0.195	0.210
Den w.	$SPLADE_{FR-BASE} + ColBERT_{FR-BASE}$	0.238	0.220	0.225	0.249	0.229	0.243	0.229	0.234
rse ns	$BM25 + SPLADE_{FR-BASE} + DPR_{FR-BASE}$	0.228	0.267	0.297	0.301^{\dagger}	0.296	0.310^{\dagger}	0.263	0.287
-spa 'ster	$BM25 + SPLADE_{FR-BASE} + ColBERT_{FR-BASE}$	0.260	0.281	0.308†	0.308^{\dagger}	0.300^{\dagger}	0.314^{\dagger}	0.266	0.282
se+ 3 sy	$BM25 + DPR_{FR-BASE} + ColBERT_{FR-BASE}$	0.238	0.289	0.302^{\dagger}	0.308^{\dagger}	0.287	0.314^{\dagger}	0.257	0.263
Der w.	$SPLADE_{FR-BASE} + DPR_{FR-BASE} + ColBERT_{FR-BASE}$	0.226	0.232	0.229	0.250	0.229	0.249	0.212	0.233
All	$BM25 + SPLADE_{{\scriptscriptstyle FR}\text{-}{\scriptscriptstyle BASE}} + DPR_{{\scriptscriptstyle FR}\text{-}{\scriptscriptstyle BASE}} + ColBERT_{{\scriptscriptstyle FR}\text{-}{\scriptscriptstyle BASE}}$	0.254	0.275	0.307^{\dagger}	0.315^{\dagger}	0.300^{\dagger}	0.323^{\dagger}	0.260	0.277

Table 3: Out-of-domain recall@10 results on LLeQA dev set. We report performance of normalized score fusion using both equal and tuned weights between systems. Hybrid combinations that improve over each of their constituent systems are highlighted in green, while those that underperform compared to one or more of their systems are marked in red. \dagger indicates competitive performance with state-of-the-art BGE-M3_{DENSE} (30.6% R@10).

gal domain and assess the effectiveness of fusion techniques in this in-domain context. Specifically, we explore the following question: Assuming a limited amount of domain-specific labeled data, to what extent can specialized retrievers and their fusion enhance performance within the legal domain? To address this question, we fine-tune our domain-general neural retrievers, initially trained on mMARCO-fr, on the 1.5K training questions from LLeQA. We denote the resulting models with the FR-LEX subscript in the remainder of the paper.

Main results. Table 4 presents the in-domain performance of our specialized retrieval models. In line with previous findings (Karpukhin et al., 2020; Khattab and Zaharia, 2020; Formal et al., 2021b; Nogueira et al., 2019), we note substantial improvements across all models compared to the zero-shot setting, with each now significantly outperforming the robust BM25 baseline. Interestingly, our singlevector dense retriever, DPR_{FR-LEX}, surpasses all the other approaches, including the more computationally demanding monoBERT_{FR-LEX} cross-encoder on smaller recall cutoffs. These results underscore the effectiveness of neural methods when trained indomain, even with relatively limited sample sizes.

Is task-adaptive pre-finetuning beneficial? Here, we study the hypothesis that performing an intermediary finetuning step on a task-related dataset before finetuning on the target dataset can help enhance downstream performance (Dai and Callan, 2019; Li et al., 2020), especially when training samples in the target domain are scarce (Zhang et al., 2020). We therefore compare two learning strategies: the first directly finetunes the pretrained CamemBERT backbone on the specialized LLeQA dataset, while the second (which we adopted as our default approach) incorporates a pre-finetuning step on the domain-general mMARCO-fr dataset. We find this intermediary phase to consistently improve in-domain performance at higher recall cutoffs across all bi-encoder models, as shown in Table 5. However, at lower recall cutoffs, pre-finetuning benefits dense bi-encoders only, with SPLADE_{FR-LEX} experiencing diminished performance. This strategy does not appear to yield improvements for the monoBERT_{FR-LEX} cross-encoder.

Does fusion still help with specialized retrievers? Table 6 highlights the in-domain performance of hybrid combinations previously assessed in a zeroshot setting. We now observe a very distinct pattern: around 70% of these combinations lead to deteriorated performance compared to using one of their constituent systems only. Among the 27 (out of 88) configurations that do show improvement, 23 leverage NSF with weights tuned in-domain, while only four combinations (i.e., 5% in total) achieve superior performance without prior tuning. Furthermore, the performance gap between individual systems and their hybrid combinations is considerably narrower within this in-domain context. While a two-system hybrid fusion can yield up to a 7.1%

	Model	R@1k	R@500	R@100	R@10	RP
Dev	BM25	0.634	0.577	0.457	0.232	0.122
	$SPLADE_{\rm fr-lex}$	0.925	0.889	0.792	<u>0.535</u>	<u>0.334</u>
	DPR	0.948	0.927	0.855	0.595	0.462
	$ColBERT_{\rm FR-LEX}$	0.892	0.852	0.747	0.434	0.255
	monoBERT _{FR-LEX}	0.967	0.942	<u>0.805</u>	0.430	0.219
	BM25	0.742	0.672	0.537	0.367	0.163
Ļ	$SPLADE_{\tiny FR-LEX}$	0.903	0.857	0.687	0.434	0.102
Tes	DPR	0.937	0.916	0.801	0.558	0.244
	$ColBERT_{\text{fr-lex}}$	0.841	0.800	0.679	0.432	0.125
	monoBERT _{FR-LEX}	0.980	0.939	<u>0.746</u>	<u>0.473</u>	0.143

Model	Recall at	Δ Avg.	
	@1000	@500	
DPR _{FR-LEX}	0.925 / 0.933	0.888 / 0.905	+1.3%
SPLADE _{FR-LEX}	0.863 / 0.878	0.817 / 0.821	+1.0%
ColBERT _{FR-LEX}	0.806 / 0.835	0.777 / 0.806	+2.9%
$monoBERT_{FR-LEX}$	0.967 / 0.967	0.928 / 0.927	-0.1%
	@50	@10	
DPR _{FR-LEX}	0.685 / 0.706	0.526 / 0.541	+1.8%
SPLADE _{FR-LEX}	0.617 / 0.596	0.402 / 0.403	-1.0%
ColBERT _{FR-LEX}	0.593 / 0.599	0.388 / 0.416	+1.7%
$monoBERT_{FR-LEX}$	0.632 / 0.629	0.353 / 0.335	-1.2%

Table 4: In-domain performance on LLeQA dev and test sets. We train each model five times with different seeds and report the best based on the dev set results.

Table 5: In-domain recall@k performances on LLeQA test set without / with pre-finetuning on mMARCO-fr. We report the means across 5 runs with different seeds.



Figure 4: Effect of weight tuning in normalized score fusion between BM25 and DPR_{FR-{LEX,BASE}} on LLeQA dev set.

R@10 improvement over the best single system in zero-shot scenarios, this enhancement does not exceed 1.4% once the models are trained in-domain. Appendix C.1 further discusses that degradation.

How does α in paired NSF affect performance? Finally, we evaluate the impact of weight tuning on the in-domain performance of NSF in a paired configuration, where one system is assigned a weight α and the other $1 - \alpha$. We select the best performing two-system combination from Table 6, i.e., BM25+DPR_{FR-LEX}. For comparison, we also report performance of this combination in a zero-shot context and that of RRF in both scenarios, as depicted in Figure 4. We find that integrating BM25 offers minimal benefits once DPR_{FR} is domain-tuned, with equal weighting between both systems consistently leading to worse performance. This finding contrasts starkly with the out-of-distribution setting, where combining both systems consistently improves performance compared to using one of them alone, regardless of the α weight assigned.

5 Related Work

Statute law retrieval. Returning the relevant legislation to a short legal question is notably challenging due to the linguistic disparity between the specialized jargon of legal statutes (Charrow and Crandall, 1978) and the plain language typically used by laypeople. Research on statute retrieval has traditionally focused on text-level similarity between queries and candidate documents, with earlier methods employing lexical approaches such as TF-IDF (Kim and Goebel, 2017; Dang et al., 2019) or BM25 (Wehnert et al., 2019; Gain et al., 2021). With advancements in representation learning techniques (Vaswani et al., 2017; Devlin et al., 2019), attention has shifted towards dense retrieval to enhance semantic matching capabilities. For instance, Louis and Spanakis (2022) demonstrate that supervised single-vector dense bi-encoders significantly outperform TF-IDF weighting schemes. Su et al. (2024) explore various dense bi-encoder models trained on different domains and reached similar conclusions. Santosh et al. (2024) further push performance of dense bi-encoders by introducing a dynamic negative sampling strategy tailored to law. In parallel, some studies have begun incorporating legal knowledge into the retrieval process. For example, Louis et al. (2023) propose a graphaugmented dense retriever that uses the topological

Method		DDE	NSF _{MIN-MAX}		NSF _{z-score}		NSF _{percentile}	
		ККГ	Equal	Tuned	Equal	Tuned	Equal	Tuned
BM25	0.232	0.232	0.232	0.232	0.232	0.232	0.232	0.232
DPR _{FR-LEX}	0.595	0.595	0.595	0.595	0.595	0.595	0.595	0.595
SPLADE _{FR-LEX}	0.535	0.535	0.535	0.535	0.535	0.535	0.535	0.535
ColBERT _{FR-LEX}	0.434	0.434	0.434	0.434	0.434	0.434	0.434	0.434
$BM25 + SPLADE_{FR-LEX}$	0.385	0.457	0.417	0.570	0.350	0.561	0.369	0.450
$DPR_{FR-Lex} + ColBERT_{FR-Lex}$	0.546	0.541	0.577	0.609^{\dagger}	0.592	0.608^{\dagger}	0.464	0.555
$BM25 + DPR_{FR-LEX}$	0.391	0.485	0.398	0.619 [†]	0.326	0.618^{\dagger}	0.351	0.452
$BM25 + ColBERT_{FR-LEX}$	0.363	0.412	0.360	0.470	0.288	0.473	0.383	0.437
$SPLADE_{FR-Lex} + DPR_{FR-Lex}$	0.573	0.586	0.582	0.613^{\dagger}	0.586	0.612^{\dagger}	0.587	0.604
$SPLADE_{FR-LEX} + ColBERT_{FR-LEX}$	0.514	0.509	0.537	0.557	0.543	0.553	0.464	0.519
$BM25 + SPLADE_{FR-LEX} + DPR_{FR-LEX}$	0.431	0.606^{\dagger}	0.533	0.629^{\dagger}	0.447	0.625^{\dagger}	0.395	0.472
$BM25 + SPLADE_{FR-LEX} + ColBERT_{FR-LEX}$	0.427	0.535	0.505	0.575	0.402	0.578	0.412	0.475
$BM25 + DPR_{FR-Lex} + ColBERT_{FR-Lex}$	0.429	0.564	0.481	0.624^{\dagger}	0.372	0.623^{\dagger}	0.402	0.468
$SPLADE_{FR-LEX} + DPR_{FR-LEX} + ColBERT_{FR-LEX}$	0.548	0.579	0.579	0.617^{\dagger}	0.587	0.620^{\dagger}	0.480	0.560
$BM25 + SPLADE_{\text{FR-LEX}} + DPR_{\text{FR-LEX}} + ColBERT_{\text{FR-LEX}}$	0.457	0.603 [†]	0.561	0.628^{\dagger}	0.485	0.627^{\dagger}	0.418	0.477

Table 6: In-domain recall@10 results on LLeQA dev set. The red region highlights hybrid combinations that perform worse than one or more of their systems, while the green region emphasizes combinations that outperform each of their constituent systems. † indicates improved performance over DPR_{FR-LEX} alone.

structure of legislation to enrich article content information. Meanwhile, Qin et al. (2024) develop a generative model that learns to represent legal documents as hierarchical semantic IDs before associating queries with their relevant document IDs. Despite this progress, no studies have explored the potential of combining diverse retrieval approaches in the legal domain, especially in zero-shot settings using domain-general models, which may individually struggle due to the specialized nature of law.

French language representation. Existing research in NLP predominantly focuses on Englishcentric directions (ARR, 2024). In French, efforts have been made in developing monolingual pretrained language models in various configurations: encoder-only (Martin et al., 2020; Le et al., 2020; Antoun et al., 2023), seq2seq (Eddine et al., 2021), and decoder-only (Louis, 2020; Simoulin and Crabbé, 2021; Müller and Laurent, 2022; Launay et al., 2022). Despite these advancements, specialized models for French remain scarce, largely due to the limited availability of high-quality labeled data. This scarcity is particularly pronounced in the field of retrieval, with few exceptions (Arbarétier, 2023). As a result, practitioners typically rely on larger multilingual models (Wang et al., 2024; Chen et al., 2024) that distribute tokens and parameters across various languages, often leading to sub-optimal downstream performance due to the curse of multilinguality (Conneau et al., 2020).

6 Conclusion

Our work explores the potential of combining distinct retrieval methods in a non-English specialized domain, specifically French statute laws. Our findings reveal that supervised domain-general monolingual models, trained with limited resources, can rival leading multilingual retrieval models, though are more vulnerable to out-of-distribution data. However, combining these monolingual models almost consistently enhances their zero-shot performance, regardless of the fusion technique employed, with certain combinations achieving stateof-the-art results in the legal domain. We show the complementary nature of these models and find they can effectively compensate for each other's mistakes, explaining the performance boost. Moreover, we confirm that in-domain training significantly enhances the effectiveness of neural retrieval models, while pre-finetuning can help with dense bi-encoders. Finally, our results indicate that fusion generally does not benefit specialized retrievers and only improves performance when scores are fused with carefully tuned weights, as equal weighting consistently leads to reduced performance. Overall, these insights suggest that for specialized domains, finetuning a single bi-encoder generally yields optimal results when (even limited) highquality domain-specific data is available, whereas fusion should be preferred when such data is not accessible and domain-general retrievers are used.

Limitations

We identify three core limitations in our research.

Firstly, our analysis specifically targets two underexplored areas – the legal domain and the French language – and is therefore confined to the only dataset available in this niche (LLeQA; Louis et al., 2024). This raises questions about the generalizability of our findings across broader French legal resources, such laws from different Frenchspeaking jurisdictions (e.g., France, Switzerland, or Canada) or across legal topics beyond those covered in LLeQA.

Secondly, our study focuses solely on end-toend retrievers – i.e., systems that identify and fetch all potentially relevant items from an entire knowledge corpus – as opposed to ranking methods that take the output of retrievers and sort it. Specifically, we deliberately omit the monoBERT_{FR} ranker due to its prohibitive inference costs for end-to-end retrieval – a brute-force search across all 28K articles in LLeQA requires about two minutes per query on GPU, a latency $9500 \times$ higher than that of single-vector retrieval, making it impractical for real-world retrieval. We let the exploration of fusion with re-rankers for future work.

Lastly, although beyond the scope of our work, it remains an open question whether the present findings are applicable to other non-English languages within different highly specialized domains.

Ethical Considerations

The scope of this work is to drive research forward in legal information retrieval by uncovering novel insights on fusion strategies. We believe this is an important application field where more research could improve legal aid services and access to justice for all. We do not foresee major situations where our methodology and findings would lead to harm (Tsarapatsanis and Aletras, 2021). Nevertheless, we emphasize that the premature deployment of prominent retrieval models not tailored for the legal domain poses a tangible risk to laypersons, who may uncritically rely on the provided information when faced with a legal issue and inadvertently worsen their personal situations.

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A Methodology Details

Formally speaking, a statutory article retrieval system takes as input a question q along with a corpus of law articles C, and returns a ranked list $\mathcal{R}_q \subset C$ of the supposedly relevant articles, sorted by decreasing order of relevance.

A.1 Retrieval Models

BM25 (Robertson et al., 1994) is an unsupervised probabilistic weighting scheme that estimates relevance based on term-matching between highdimensional sparse vectors using statistical properties such as term frequencies, document frequencies, and document lengths. Specifically, it calculates a relevance score $s(q, a) : \mathcal{V}^{|q|} \times \mathcal{V}^{|a|} \to \mathbb{R}_+$ between query q and article a as a sum of contributions of each query term t from vocabulary \mathcal{V} appearing in the article, i.e.,

$$s_{\text{BM25}}(q, a) = \sum_{t \in q} \log\left(\frac{|\mathcal{C}| - \mathrm{df}(t) + 0.5}{\mathrm{df}(t) + 0.5}\right) \cdot \frac{\mathrm{tf}(t, a) \cdot (k_1 + 1)}{\mathrm{tf}(t, a) + k_1 \cdot \left(1 - b + b \cdot \frac{|a|}{avgal}\right)},$$
(1)

where the term frequency $\mathrm{tf}(t, a) : \mathcal{V}^1 \times \mathcal{V}^{|a|} \to \mathbb{Z}_+$ is the number of occurrences of term t in article a, the document frequency $\mathrm{df}(t) : \mathcal{V}^1 \to \mathbb{Z}_+$ is the number of articles within the corpus \mathcal{C} that contain term $t, k_1 \in \mathbb{R}_+$ and $b \in [0, 1]$ are constant parameters, and avgal is the average article length.

BM25 remains widely used due to its balance between simplicity and robustness, often competing with modern retrieval methods (Thakur et al., 2021) while being extremely efficient and requiring no training. However, its reliance on exact-term matching restricts its ability to understand semantics, capture contextual relationships, and handle synonyms or rare terms.

DPR_{FR-{BASE,LEX}} are based on the widely-adopted siamese bi-encoder architecture (Gillick et al., 2018), which consists of a learnable text embedding function $E(i; \mathbf{\Omega}) : \mathcal{V}^n \mapsto \mathbb{R}^{n \times d}$ that maps an input text sequence i of n terms from vocabulary \mathcal{V} to d-dimensional real-valued term vectors, i.e.,

$$E(i; \mathbf{\Omega}) = \mathbf{H}_i = \left[\mathbf{h}_{i, \text{CLS}}, \mathbf{h}_{i, 1}, \cdots, \mathbf{h}_{i, n}\right], \quad (2)$$

and calculates a relevance score between query qand article a by operating on their independently computed bags of contextualized term embeddings $\mathbf{H}_i \in \mathbb{R}^{n \times d}$. Our single-vector dense representation models obtain this score by performing

$$s_{\text{SINGLE}}(q, a) = \mathbf{h}_q^* \cdot \mathbf{h}_a^*, \tag{3}$$

where $\mathbf{h}_i^* \in \mathbb{R}^d$ is the global representation of sequence *i*, derived by mean pooling across the sequence term embeddings, i.e.,

$$\mathbf{h}_{i}^{*} = \operatorname{AvgP}(\mathbf{H}_{i}) = \frac{1}{|i|} \mathbf{H}_{i}^{\mathsf{T}} \mathbf{1}_{|i|}.$$
 (4)

The models are trained via optimization of the contrastive NT-Xent loss (Chen et al., 2020; Gao et al., 2021b), which aims to learn a high-quality embedding function so that relevant query-article pairs



Figure 5: High-level illustration of the four prominent neural retrieval architectures explored in this study.

achieve higher similarity than irrelevant ones. Let $\mathcal{B} = \{(q_i, a_i^+, a_{\mathrm{H},i}^-)\}_{i=1}^N$ be a batch of N training instances, each comprising a query q_i associated with a positive article a_i^+ and a hard negative article $a_{\mathrm{H},i}^-$. By considering the articles paired with all other queries within the same batch, we can enrich each training triple with an additional set of 2(N-1) in-batch negatives $\mathcal{A}_{\mathrm{IB},i}^- = \{a_j^+, a_{\mathrm{H},j}^-\}_{j \neq i}^N$. Given these augmented training samples, we contrastively optimize the negative log-likelihood of each positive article such that

$$\mathcal{L}_{\text{NT-XENT}} = -\log \frac{e^{s(q_i, a_i^+)/\tau}}{\sum_{a \in \{a_i^+, a_{\text{H}, i}^-\} \cup \mathcal{A}_{\text{IB}, i}^-} e^{s(q_i, a)/\tau}},$$
(5)

where $\tau \in \mathbb{R}_+$ is a temperature hyper-parameter that controls the concentration level of the distribution (Hinton et al., 2015). We enforce $\|\mathbf{h}_i^*\| = 1$ via a ℓ_2 -normalization layer such that Equation (3) computes the cosine similarity.

Single-vector dense models proved to effectively model language nuances and contextual information (Karpukhin et al., 2020). Furthermore, the independent encoding enables offline precomputation of article embeddings, resulting in low latency query-time retrieval. However, its effectiveness can be limited by the quality and diversity of its training data, potentially leading to sub-optimal performance with out-of-distribution content (Thakur et al., 2021).

SPLADE_{FR-{BASE,LEX}} follow SPLADE-max (Formal et al., 2021a), which uses the same singlevector scoring mechanism as its dense representation counterpart, outlined in Equation (3), but operates on different global sequence representations derived as follows:

$$\mathbf{h}_{i}^{*} = \mathrm{MaxP}\left(\mathrm{sat}\left(\mathrm{transf}(\mathbf{H}_{i})\mathbf{W}_{\mathrm{MLM}}^{\mathsf{T}} + \mathbf{b}_{\mathrm{MLM}}\right)\right)\right),$$
(6)

where $transf(\cdot; \gamma) : \mathbb{R}^{n \times d} \to \mathbb{R}^{n \times d}$ first transforms the contextualized term embeddings using

$$transf(\cdot; \boldsymbol{\gamma}) = LayerNorm(GELU(Linear(\cdot))),$$
(7)

preparing them for subsequent projection onto the vocabulary space via the MLM classification head $\mathbf{W}_{MLM} \in \mathbb{R}^{|\mathcal{V}| \times d}$, with bias $\mathbf{b}_{MLM} \in \mathbb{R}^{|\mathcal{V}|}$. The function $\operatorname{sat}(\cdot) : \mathbb{R}^{n \times |\mathcal{V}|} \to \mathbb{R}^{n \times |\mathcal{V}|}$ then applies ReLU to ensure positive token activations, before performing log-saturation to maintain sparsity and prevent some tokens from dominating:

$$\operatorname{sat}(\cdot) = \log\left(1 + \operatorname{ReLU}(\cdot)\right). \tag{8}$$

Finally, a max pooling operation $\operatorname{MaxP}(\cdot)$: $\mathbb{R}^{n \times |\mathcal{V}|} \to \mathbb{R}^{|\mathcal{V}|}$ is applied to distill the global sequence representation. The model is trained by jointly optimizing the contrastive NT-Xent objective, presented in Equation (5), and the FLOPS regularization loss (Paria et al., 2020), which aims to impose sparsity on the produced embeddings while encouraging an even distribution of the non-zero elements across all the dimensions to ensure maximal speedup. This is achieved by minimizing a smooth relaxation of the average number of floating-point operations necessary to compute the dot product between two embeddings (as outlined in Equation (3)), defined as follows:

$$\ell_{\text{FLOPS}} = \sum_{j=1}^{|\mathcal{V}|} \bar{p}_j^2 = \sum_{j=1}^{|\mathcal{V}|} \left(\frac{1}{|\mathcal{B}|} \sum_{i=1}^{|\mathcal{B}|} \mathbf{h}_{ij}^* \right)^2 \quad (9)$$

where $\bar{p}_j \approx |\mathcal{B}|^{-1} \sum_{i=1}^{|\mathcal{B}|} \mathbb{1}[\mathbf{h}_{ij}^* \neq 0]$ is the empirical estimation of the activation probability for token $t_j \in \mathcal{V}$ over a batch \mathcal{B} . The overall loss is given by

$$\mathcal{L}_{\text{SPLADE}} = \mathcal{L}_{\text{NT-XENT}} + \lambda_q \ell_{\text{FLOPS}}^q + \lambda_a \ell_{\text{FLOPS}}^a, (10)$$

where λ_i controls the strength of the regularization, with higher values typically encouraging the model to learn sparser representations, therefore enhancing efficiency yet often at the expense of effectiveness. By applying separate regularization weights for queries and articles, greater emphasis can be placed on sparsity for queries, which is critical for fast inference with inverted indexes.

As its representations are grounded in the encoder's vocabulary, SPLADE enhances interpretability and facilitates explanations of observed rankings. It also exhibits strong generalization capabilities on out-of-distribution data and the sparsity of its vectors enables the use of inverted indexes for fast inference. Nevertheless, learning sparse representations in high-dimensional spaces poses specific challenges: factors such as the tokenization type or the initial distribution of MLM weights can lead to model divergence (Formal, 2023).

ColBERT_{FR-{BASE,LEX}} use the fine-granular late interaction scoring mechanism of ColBERT (Khattab and Zaharia, 2020), which calculates the similarity across all pairs of query and article token embeddings, applies max-pooling across the resulting scores for each query term, and then sum the maximum values across query terms to derive the overall relevance estimate, i.e.,

$$s_{\text{MULTI}}(q,a) = \sum_{i=1}^{|q|} \max_{j=1}^{|a|} \mathbf{h}_{q,i} \cdot \mathbf{h}_{a,j}.$$
 (11)

We train the model by jointly optimizing two contrastive objectives, namely the pairwise softmax cross-entropy loss used in ColBERTv1, defined as

$$\mathcal{L}_{\text{PAIRSM-CE}} = -\log \frac{e^{s(q_i, a_i^+)}}{e^{a(q_i, a_i^+)} + e^{s(q_i, a_{\text{H}, i}^-)}}, \quad (12)$$

and the NT-Xent loss, added as an enhancement for optimizing ColBERTv2 (Santhanam et al., 2022b). ColBERT's fine-grained late interaction between term embeddings demonstrates greater effectiveness and robustness to out-of-distribution data compared to single-vector dense bi-encoders (Thakur et al., 2021), while enabling result interpretability. However, its computational complexity requires sophisticated engineering schemes and low-level optimizations for efficient large-scale deployment (Santhanam et al., 2022a).

monoBERT_{FR-{BASE,LEX}} exploit the encoder-only cross-attention model structure (Nogueira and Cho, 2019), which uses a text embedding model similar to the one defined in Equation (2) to perform

all-to-all interactions across terms from concatenated query-article pairs, before deriving a relevance score through binary classification on the pair representation, i.e.,

$$s_{\text{MONO}}(q, a) = \sigma \left(\text{transf} \left(\mathbf{h}_{[q;a]}^* \right) \mathbf{W}_{\text{out}}^\mathsf{T} + \mathbf{b}_{\text{out}} \right),$$
(13)

where $\mathbf{h}_{[q;a]}^* \in \mathbb{R}^d$ is obtained through a first token pooling operation $\operatorname{FirstP}(\cdot) : \mathbb{R}^{n \times d} \to \mathbb{R}^d$, which extracts the special CLS token representation of the concatenated sequence:

$$\mathbf{h}_{[q;a]}^* = \mathrm{FirstP}\big(\mathbf{H}_{[q;a]}\big) = \mathbf{h}_{[q;a],\mathrm{CLS}}.$$
 (14)

The CLS token embedding is then transformed with $transf(\cdot; \theta) : \mathbb{R}^d \to \mathbb{R}^d$ such that

$$\operatorname{transf}(\cdot;\boldsymbol{\theta}) = \operatorname{tanh}(\operatorname{Linear}(\cdot)), \quad (15)$$

before being projected to a real-valued score via a linear layer $\mathbf{W}_{out} \in \mathbb{R}^{1 \times d}$ with bias $\mathbf{b}_{out} \in \mathbb{R}^d$. Finally, the sigmoid function σ bounds the resulting score to the interval [0, 1]. The model is optimized via the binary cross-entropy training objective

$$\mathcal{L}_{\text{BCE}} = -y_i \cdot \log \left(s(q_i, a_i) \right) - \left(1 - y_i \right) \cdot \log \left(1 - s(q_i, a_i) \right),$$
(16)

where y_i is the ground-truth relevance label for query-article pair (q_i, a_i) .

The rich interaction mechanism of such a model allows to capture complex relationships and often achieve state-of-the-art performance in retrieval tasks (Hofstätter et al., 2020). However, its high computational complexity makes it impractical for large-scale or real-time retrieval scenarios, limiting its use to re-ranking small candidate sets only.

A.2 Late Fusion Techniques

A late fusion function $f(q, a, \mathcal{M}) : \mathcal{V}^{|q|} \times \mathcal{V}^{|a|} \times \mathcal{M} \to \mathbb{R}_+$ computes a relevance score between query q and article a by combining the ranked lists of articles $\mathcal{R}_m \subset \mathcal{C}$ returned separately by a set of retrieval models \mathcal{M} .

Borda count fusion (BCF) uses a straightforward approach – originally developed as a voting mechanism (de Borda, 1781) – which combines the ranks from different systems linearly (Ho et al., 1994) such that

$$f_{\text{BCF}}(q, a, \mathcal{M}) = \sum_{m \in \mathcal{M}} |\mathcal{R}_m| - \pi_m(q, a) + 1,$$
(17)

where $\pi_m(q, a) \in [1, |\mathcal{R}_m|]$ denotes the rank of article *a* in the list of results returned by model *m* for query *q*, i.e.,

$$\pi_m(q, a) = 1 + \sum_{a_i \in \mathcal{C}} \mathbb{1}[s_m(q, a_i) > s_m(q, a)].$$
(18)

Reciprocal rank fusion (RRF) refines the previous approach by introducing a non-linear weighting scheme that gives more emphasis to top-ranked documents (Cormack et al., 2009), i.e.,

$$f_{\text{RRF}}(q, a, \mathcal{M}) = \sum_{m \in \mathcal{M}} \frac{1}{k + \pi_m(q, a)}, \quad (19)$$

where k > 0 is a constant set to 60 by default.

Normalized score fusion (NSF) linearly combines the output relevance scores from distinct retrieval models (Lee, 1995) such that

$$f_{\text{NSF}}(q, a, \mathcal{M}) = \sum_{m \in \mathcal{M}} \alpha_m \hat{s}_m(q, a), \qquad (20)$$

where the scalars α_m , controlling the relative importance of each model m in the fused score, are non-negative and sum to one. These weights can be varied or uniformly distributed, as in CombSUM (Shaw and Fox, 1994). Given that the original model-specific scores can be unbounded, they are generally normalized prior to fusion, using either min-max scaling where

$$\hat{s}_m(q,a) = \frac{s_m(q,a) - \min_{i=1}^{|\mathcal{C}|} s_m(q,a_i)}{\max_{i=1}^{|\mathcal{C}|} s_m(q,a_i) - \min_{i=1}^{|\mathcal{C}|} s_m(q,a_i)}$$
(21)

or z-score scaling such that

$$\hat{s}_m(q,a) = \frac{s_m(q,a) - \mu_m(q)}{\sigma_m(q)},$$
 (22)

where $\mu_m(q)$ is the mean score across all candidate articles in the ranked list for query q returned by model m, and $\sigma_m(q)$ denotes the standard deviation of these scores. Beyond these conventional scaling methods, we also investigate a percentilebased normalization, the rationale and specifics of which are elaborated in Section 3.

A.3 Evaluation Metrics

Let $\operatorname{rel}(q, a) : \mathcal{V}^m \times \mathcal{V}^n \to \{0, 1\}$ be a binary relevance function, indicating whether an article *a* from the corpus C is relevant to a query *q*. Assume that $\mathcal{R}_q = \{(i, a)\}_{i=1}^k$ denotes the ranked list of articles returned by a retrieval system, truncated at the top-*k* results. We define the metrics mentioned in Section 2.3 as follows. **Recall@**k. The metric quantifies the proportion of relevant articles retrieved within the top-k ranked results for query q, compared to the total number of relevant articles in the corpus C, i.e.,

$$\mathbf{R} \mathfrak{G} k(q, \mathcal{R}_q) = \frac{\sum_{(i,a) \in \mathcal{R}_q} \operatorname{rel}(q, a)}{\sum_{a \in \mathcal{C}} \operatorname{rel}(q, a)}.$$
 (23)

Reciprocal rank@k. The metric takes the inverse of the position at which the first relevant article appears within the top-k results for query q, i.e.,

$$\mathbf{RR}@k(q, \mathcal{R}_q) = \max_{(i,a)\in\mathcal{R}_q} \frac{\operatorname{rel}(q, a)}{i}.$$
 (24)

R-precision. The metric computes the ratio of relevant articles within the top-N retrieved results for query q, where N represents the total number of relevant articles for that query, i.e.,

$$\operatorname{RP}(q, \mathcal{R}_q) = \frac{\sum_{(i,a) \in \{\mathcal{R}_q\}_{i=1}^N} \operatorname{rel}(q, a)}{N}.$$
 (25)

For all metrics, we report the average scores over a set of Q queries.

A.4 Counting FLOPs

Below, we detail our methodology to estimate the inference complexity per query in terms of floating point operations (FLOPs). Except for BM25, the main computational cost derives from the Transformer encoder's forward pass, executed once with bi-encoder models to encode the query and repeatedly in cross-encoders to process each query-article pair. We leverage DeepSpeed's profiler to measure the forward pass cost of each neural retriever.³ Queries are assumed to be 15 tokens and articles 157 tokens, as per their respective average lengths in LLeQA.

BM25. In the BM25 scoring formula, outlined in Equation (1), several elements can be precomputed and cached to streamline computations during inference. These include the inverse document frequency (IDF) for each term, the normalized document lengths adjusted by the parameters k1 and b, and the constant (k1+1). For each query term and candidate document, the process involves four primary operations. First, the term frequency (TF), retrieved via a simple lookup, is multiplied by the pre-computed IDF and (k1+1). The result is then added to the stored normalized document

³https://www.deepspeed.ai/tutorials/ flops-profiler/

French PLM Backbone	#Params	Architecture	#L	Pre-training	MRR@10	R@100	R@500
DistilCamemBERT (Delestre and Amar, 2022)	68.1M	BERT	6	MLM+KL+COS	0.268	<u>0.764</u>	<u>0.879</u>
ELECTRA-fr _{BASE} (Schweter, 2020)	110.0M	BERT	12	RTD	0.234	0.690	0.816
CamemBERT _{BASE} (Martin et al., 2020)	110.6M	BERT	12	MLM	0.285	0.778	0.891
CamemBERTa _{BASE} (Antoun et al., 2023)	111.8M	DeBERTa	12	RTD	0.248	0.696	0.822

Table 7: In-domain retrieval performances on mMARCO-fr small dev set (Bonifacio et al., 2021) for single-vector dense representation models trained using various French pretrained autoencoding language models as their text embedding backbone. MLM, RTD, KL, and COS denote the masked language modeling (Devlin et al., 2019), replaced token detection (Clark et al., 2020), Kullback-Leibler divergence (Radford et al., 2018), and negative cosine embedding (Sanh et al., 2019) training objectives, respectively. #L indicates the number of encoder layers.

length. Finally, this sum is used as the denominator in dividing the product of TF, IDF, and (k1+1). These four operations – two multiplications, one addition, and one division – per term-article pair lead to an overall computational cost of $4|\overline{q}||\mathcal{C}|$ FLOPs for searching across the whole corpus.

SPLADE_{FR-BASE}. At indexing time, this model creates a pseudo-TF for each token t in the vocabulary by scaling and rounding the corresponding activation weights in sparse article representations. This enables the construction of a pseudo text collection where each term t is repeated TF(t, a) times for article a. During inference, obtaining the query representation requires a single forward pass. For each non-zero term in that representation, the search process involves three core steps: accessing the inverted list for the term (a negligible lookup operation), multiplying the query term weight by each article term weight from that list, and adding each result to the corresponding article's score accumulator. Consequently, for each term-article pair, the operations include one multiplication and one addition. With $C_{\rm FW}$ representing the cost of the encoder's forward pass, $|\mathbf{h}_{a}^{+}|$ the average number of non-zero terms in the query representation, and $|\mathcal{L}_{IV}|$ the average length of the inverted lists for these terms, the total computational complexity is estimated as $C_{\rm FW} + 2 \overline{|\mathbf{h}_q^+|} \overline{|\mathcal{L}_{\rm IV}|}$ FLOPs.⁴

Single-vector dense bi-encoders. With these models, a brute-force search across all articles from corpus C necessitates |C| inner products between *d*-dimensional article representations – each involving *d* multiplications and *d* – 1 additions. Consequently, the total inference cost amounts to $C_{\text{FW}} + (2d-1)|C|$ operations.

ColBERT_{FR-BASE}. For each candidate article, this model computes Equation (11) with the query and candidate token representations of *d* dimensions. For each query term, this computation requires $2d|\overline{q}||\overline{a}|$ operations for token-level inner products, $|\overline{q}||\overline{a}|$ to identify the row-wise max, and $|\overline{q}|$ for the final average. When performing brute-force search across the entire corpus, the inference complexity is estimated as $C_{\text{FW}} + |\overline{q}|^2 (2d|\overline{a}|+|\overline{a}|+1)|\mathcal{C}|$ FLOPs.

monoBERT_{FR-BASE}. This model requires one forward pass per article to assess, incurring a high computational cost that typically limits their use to re-ranking a set of candidates returned by a cheaper retrieval model. To reflect that practice, we report the number of operations needed to score a fixed set of 1000 articles, resulting in $10^3 C_{\text{FW}}$ FLOPs.

B Implementation Details

B.1 Embedding Backbone

To ensure a fair comparison between the different matching paradigms detailed in Section 2.1, irrespective of the underlying text embedding model's capacity, we choose to exploit the same pretrained autoencoding language model across all our neural retrievers. To explore the efficacy of existing French embedding models for text retrieval, we finetune four prominent pretrained models on mMARCO-fr, including CamemBERT_{BASE} (Martin et al., 2020), ELECTRA-fr_{BASE} (Schweter, 2020), DistilCamemBERT (Delestre and Amar, 2022), and CamemBERTa_{BASE} (Antoun et al., 2023). We limit our investigation to the performance of single-vector dense bi-encoders to minimize environmental impact. Table 7 presents the results on the mMARCO-fr small dev set, revealing that CamemBERT_{BASE} significantly outperforms the other French text encoders. Following these findings, we select this model as the common backbone encoder for all our neural retrievers.

⁴On LLeQA, the FR-BASE model activates an average of 178 tokens per query, and the associated index features inverted lists of 378 elements on average.

Training data (\rightarrow)	mMARCO-fr				LLeQA			
Learned model (\rightarrow)	DPR _{FR-BASE}	$\textbf{SPLADE}_{\text{FR-BASE}}$	$ColBERT_{FR-BASE}$	monoBERT _{FR-BASE}	DPR _{FR-LEX}	$\textbf{SPLADE}_{\text{fr-lex}}$	ColBERT _{FR-LEX}	monoBERT _{fr-lex}
Configuration								
Max query length	128	32	32	-	512	64	64	-
Max article length	128	128	128	256 - q	512	512	512	512 - q
Pooling strategy	mean	max	-	cls	mean	max	-	cls
Similarity function	cos	cos	cos	-	cos	cos	cos	-
Hyperparameters								
Steps	66k	100k	200k	20k	1k	2k	1k	2k
Batch size	152	128	128	128	64	32	64	64
Optimizer	AdamW	AdamW	AdamW	AdamW	AdamW	AdamW	AdamW	AdamW
Weight decay	0.01	0.01	0.0	0.01	0.01	0.01	0.0	0.01
Peak learning rate	2e-5	2e-5	5e-6	2e-5	2e-5	2e-5	5e-6	2e-5
Learning rate decay	linear	linear	linear	constant	constant	constant	constant	constant
Warm-up ratio	0.01	0.04	0.1	0.0	0.0	0.0	0.0	0.0
Gradient clipping	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
Softmax temperature	0.05	0.05	1.0	-	0.05	0.05	1.0	-
Energy								
Hardware	V100	H100	H100	H100	H100	H100	H100	H100
Thermal design power (W)	300	310	310	310	310	310	310	310
Training time (h)	14.1	12.9	18.4	1.5	0.22	0.30	0.18	0.17
Power consumption (kWh)	4.2	4.0	5.7	0.5	0.07	0.09	0.06	0.05
Carbon emission (kgCO2eq)	1.8	1.7	2.5	0.2	0.03	0.04	0.03	0.02

Table 8: Implementation details for our learned domain-general (FR-BASE) and domain-specific (FR-LEX) retrievers.



Figure 6: Distribution of paired relevance scores from our learned specialized retrievers on around 3,000 queryarticle pairs from the LLeQA dev set, evenly balanced between positive and negative instances.

B.2 Optimization

Table 8 provides details on our models' configuration, training hyperparameters, and energy consumption. Training and GPU-based experiments are conducted on a single 80GB NVIDIA H100, while CPU-based evaluations are performed on a server with a 64-core AMD EPYC 7763 CPU at 3.20GHz and 500GB of RAM. We implement, train, tune, and monitor our models using the following Python libraries: pytorch (Paszke et al., 2019), transformers (Wolf et al., 2020), sentence-transformers (Reimers and Gurevych, 2019), colbert-ai (Khattab and Zaharia, 2020), and wandb (Biewald, 2020).

C Additional Results

C.1 Complementarity of Specialized Models

To understand why fusion does not enhance the performance of specialized retrievers, we examine

the complementarity of their relevance signals in Figure 6. We sample approximately 1,500 positive query-article pairs from the LLeQA dev set, along with an equal number of random negatives, and gather the scores assigned by the different models to each pair. Contrary to the zero-shot context, we find that the output scores from the specialized models align closely, as shown by the linear distribution of paired scores in Figure 6. Pairs that receive high relevance scores from one system typically receive similar scores from others, and the same applies to lower scores. We hypothesize that since all retrieval models were trained on a limited number of the exact same domain-specific data with the same primary contrastive learning objective, they converged towards learning similar relevance signals, with some models like DPR_{FR-LEX} developing more nuanced ones. Consequently, fusing models that have learned related signals, but with varying levels of accuracy, generally results in

#	BM25	$DPR_{\text{fr-base}}$	SPLADE _{FR-BASE}	ColBERT _{FR-BASE}
		Min	r-max scaling	
5	.50	0	.50	0
6	0	.25	0	.75
7	.40	.60	0	0
8	.40	0	0	.60
9	0	.70	.30	0
10	0	0	.20	.80
11	.25	.25	.50	0
12	.35	0	.40	.25
13	.35	.25	0	.40
14	0	.10	.20	.70
15	.30	.35	.10	.25
		Z-s	core scaling	
5	.40	0	.60	0
6	0	.25	0	.75
7	.30	.70	0	0
8	.25	0	0	.75
9	0	.80	.20	0
10	0	0	.20	.80
11	.20	.40	.40	0
12	.20	0	.40	.40
13	.20	.30	0	.50
14	0	.40	.10	.50
15	.15	.45	.10	.30
		Perc	entile scaling	
5	.60	0	.40	0
6	0	.05	0	.95
7	.50	.50	0	0
8	.40	0	0	.60
9	0	.85	.15	0
10	0	0	.20	.80
11	.45	.05	.50	0
12	.55	0	.35	.10
13	.50	.40	0	.10
14	0	.05	.70	.25
15	.50	.05	.40	.05

#	BM25	DPR _{FR-LEX}	SPLADE _{FR-LEX}	ColBERT _{FR-LEX}
		Min	-max scaling	
5	.15	0	.85	0
6	0	.85	0	.15
7	.10	.90	0	0
8	.15	0	0	.85
9	0	.70	.30	0
10	0	0	.85	.15
11	.05	.60	.35	0
12	.15	0	.75	.10
13	.10	.80	0	.10
14	0	.60	.25	.15
15	.05	.60	.30	.05
		Z-s	core scaling	
5	.10	0	.90	0
6	0	.65	0	.35
7	.05	.95	0	0
8	.05	0	0	.95
9	0	.70	.30	0
10	0	0	.75	.25
11	.05	.55	.40	0
12	.05	0	.75	.20
13	.05	.80	0	.15
14	0	.60	.25	.15
15	.05	.80	.05	.10
		Perc	entile scaling	
5	.05	0	.95	0
6	0	.95	0	.05
7	.05	.95	0	0
8	.10	0	0	.90
9	0	.85	.15	0
10	0	0	.95	.05
11	.05	.45	.50	0
12	.05	0	.90	.05
13	.05	.75	0	.20
14	0	.85	.10	.05
15	.05	.40	.50	.05

Table 9: Optimally tuned weights for the normalized score fusion results presented in Table 3 (zero-shot).

Table 10: Optimally tuned weights for the normalized score fusion results presented in Table 6 (in-domain).

degraded performance compared to using the best model alone.

C.2 Weight Tuning in NSF

Table 9 an Table 10 present the optimal weights assigned to each retrieval system in zero-shot and in-domain contexts, respectively, when using normalized score fusion (NSF). These weights were meticulously determined through extensive tuning on the LLeQA dev set. Additionally, Figures 7 to 11 illustrate the variation in performance based on the weights assigned to pairs of retrieval systems.



Figure 7: Effect of weight tuning in NSF between BM25 & ColBERT_{FR-{LEX,BASE}} on LLeQA dev set.



Figure 8: Effect of weight tuning in NSF between BM25 & SPLADE_{FR-{LEX,BASE}} on LLeQA dev set.



Figure 9: Effect of weight tuning in NSF between $SPLADE_{FR-\{LEX,BASE\}}$ & $DPR_{FR-\{LEX,BASE\}}$ on LLeQA dev set.



 $Figure \ 10: \ Effect \ of \ weight \ tuning \ in \ NSF \ between \ DPR_{FR-\{LEX,BASE\}} \ \& \ ColBERT_{FR-\{LEX,BASE\}} \ on \ LLeQA \ dev \ set.$



 $Figure \ 11: \ Effect \ of \ weight \ tuning \ in \ NSF \ between \ ColBERT_{FR-\{LEX,BASE\}} \ \& \ SPLADE_{FR-\{LEX,BASE\}} \ on \ LLeQA \ dev \ set.$