

SURGE: On the Potential of Large Language Models as General-Purpose Surrogate Code Executors

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Abstract

Neural surrogate models are powerful and efficient tools in data mining. Meanwhile, large language models (LLMs) have demonstrated remarkable capabilities in code-related tasks, such as generation and understanding. However, an equally important yet underexplored question is whether LLMs can serve as surrogate models for code execution prediction. To systematically investigate it, we introduce SURGE, a comprehensive benchmark with 1160 problems covering 8 key aspects: multi-language programming tasks, competition-level programming problems, repository-level code analysis, high-cost scientific computing, time-complexity-intensive algorithms, buggy code analysis, programs dependent on specific compilers or execution environments, and formal mathematical proof verification. Through extensive analysis of 21 open-source and proprietary LLMs, we examine scaling laws, data efficiency, and predictive accuracy. Our findings reveal important insights about the feasibility of LLMs as efficient surrogates for computational processes. The benchmark and evaluation framework are available at <https://github.com/Imbernoulli/SURGE>.

1 Introduction

Neural surrogate models (Zhang et al., 2024; Sun and Wang, 2019) are powerful tools in data mining and machine learning, which efficiently approximate complex computational processes. Meanwhile, Large language models (LLMs) (Reid et al., 2024; Meta, 2024; Anthropic, 2024b; Hui et al., 2024; Bi et al., 2024) have demonstrated remarkable capabilities in code-related tasks (Lu et al., 2021a; Zheng et al., 2023; Luo et al., 2023; Team, 2024a; Guo et al., 2024), including code understanding (Ahmad et al., 2020; Chakraborty et al., 2020) and code generation (Li et al., 2018a; Parvez et al., 2018). However, an equally important yet underexplored question is whether LLMs can serve as

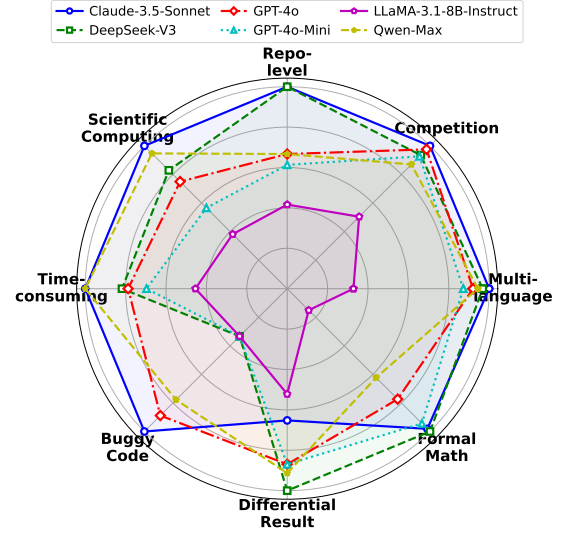


Figure 1: Performance of 6 typical models on SURGE.

general-purpose surrogate code executors, which predict the behavior of a program without actually running it. A recent study (Lyu et al., 2024) acknowledges its importance, however, it focuses on a case study rather than a systematic analysis.

The ability to predict code execution outcomes without execution has tremendous significance. In scientific computing, running simulations often requires substantial computational resources and is time-consuming, making it impractical to test every possible configuration (Lu and Ricciuto, 2019; Hesthaven and Ubbiali, 2018; Benner et al., 2015). In security-sensitive environments, executing untrusted code poses inherent risks, necessitating alternative mechanisms for assessing program behavior without exposing the system to potential vulnerabilities (Nebbione and Calzarossa, 2023; Shirazi et al., 2017; Wang et al., 2024). Additionally, some code requires highly specific execution environments, which may not always be available, making surrogate execution a valuable alternative (Queiroz et al., 2023; Gu et al., 2025). Moreover, accurately

predicting a model’s potential outputs or errors is crucial for improving traditional tasks such as code understanding, code generation, and even math reasoning (Li et al., 2025). Lastly, many works use LLMs as reward models (RMs) in reinforcement learning. For code tasks, accurate execution prediction is key to a reliable RM (Ouyang et al., 2022).

Traditional approaches to surrogate code executing (King, 1976; Cadar and Sen, 2013) struggle to generalize across languages and suffer from scalability issues when applied to complex real-world codebases. Containerized environments (Merkel, 2014) mitigate dependency issues but still require full code execution. Recent efforts to train neural executors (Yan et al., 2020) focus on narrow tasks and lack the generality needed for real-world code. In contrast, LLMs’ capacity to internalize patterns from vast code corpora (Lu et al., 2021b; Chaudhary, 2023) suggests a path toward general-purpose surrogate code execution.

To understand the potential of LLMs as **General-purpose SURrogate** code executors, we introduce **SURGE**. It includes 8 components: (1) fundamental programming tasks in multiple languages, (2) competition programming problems requiring deep logical inference, (3) repository-level codebases that test long-range dependencies, (4) scientific simulations and optimizations where direct execution is high-cost, (5) time-consuming logical algorithms that have high time-complexity, (6) buggy code that examines LLMs’ ability to predict runtime errors, (7) programs whose behavior depends on specific compiler versions or execution environments and (8) math theorem proving in formal language (De Moura et al., 2015; Moura and Ullrich, 2021) which expects compilers to testify.

Through extensive evaluation of 21 open-source and proprietary LLMs on SURGE, we provide the first large-scale study of LLMs’ capabilities as computational surrogates. Additionally, we investigate the impact of various factors, including prompt engineering strategies, programming language characteristics, computational complexity, and execution time requirements, on surrogate performance. Our findings reveal both the promising potential and current limitations of LLMs as general-purpose code execution surrogates. The performance of typical models on SURGE is shown in Figure 1.

Beyond benchmarking, we conduct a scaling law study on whether LLMs’ performance improves with model size and training data. We train models with 4 different sizes on different scales of training

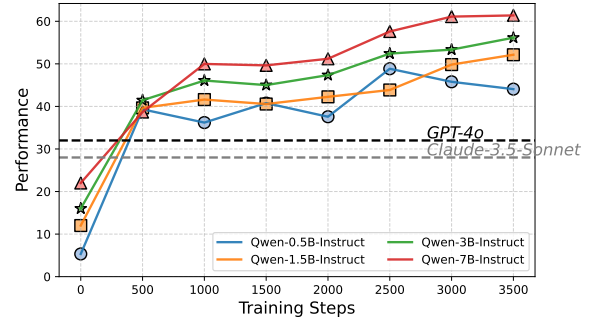


Figure 2: Performance scaling across model sizes and training steps.

data from the formal language subset of SURGE. Our experiments demonstrate that models’ performance consistently improves with both model size and training steps, with larger models showing stronger learning capacity and higher performance ceilings throughout the training process (Figure 2).

In short, our work makes the following key contributions:

- We introduce SURGE, the first holistic benchmark for evaluating LLMs as general-purpose surrogate code executors. It consists of 8 subsets and 1160 problems.
- We evaluate 21 open-source and proprietary LLMs on SURGE and conduct the first large-scale analysis on them.
- We present a scaling law study with models of varying sizes and scales of training data, providing empirical insights on the scaling law of LLMs on these tasks.

2 Related Works

Neural Surrogate Models. Neural surrogate models are neural network-based approximations used to replace computationally expensive simulations in various scientific and engineering domains (Zhang et al., 2024; Sun and Wang, 2019). These models act as domain-specific emulators by learning complex input-output relationships from high-fidelity data (Raissi et al., 2020; Sun et al., 2020; Bessa et al., 2017; Thuerey et al., 2020; Raissi et al., 2019; Willard et al., 2022). Recently, generative models have been incorporated into surrogate modeling. Some equip language models with traditional surrogate models to facilitate iterative optimization (Ma et al., 2024; Lyu et al., 2025), and some use generative models to realize the end-to-end surrogate process (Gruber et al., 2024; Hao et al., 2024; Wimmer and Rekabsaz, 2023; Che

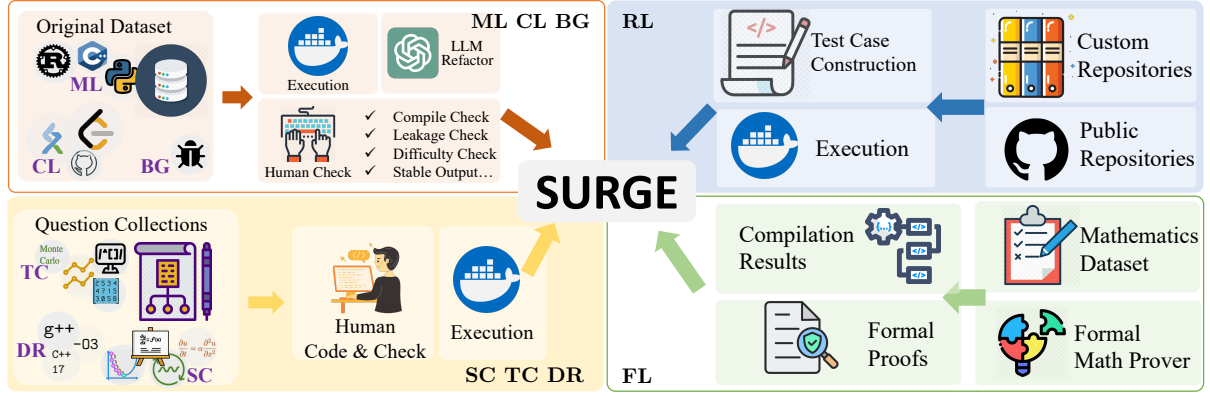


Figure 3: The Construction of SURGE employs 4 methodologies: 1. Iterative Refactor, 2. Repository Sampling, 3. Manual Implementation, and 4. Inference & Verification.

et al., 2024). While these studies primarily focus on natural sciences, time series, and multimodal gaming, the application of surrogate modeling to code execution, where both input and output exist in the modality of language, remains unexplored.

LLMs for Code. LLMs are widely used in code-related tasks (Lu et al., 2021a; Luo et al., 2023; Team, 2024a; Guo et al., 2024), which can be fundamentally categorized into code understanding and code generation. Code understanding tasks include code summarization (Hu et al., 2018; Harer et al., 2019; Ahmad et al., 2020), bug detection (Li et al., 2018b; Russell et al., 2018; Zhou et al., 2019; Chakraborty et al., 2020), duplication detection (Zhang et al., 2019; Yu et al., 2019; Wang et al., 2020), code retrieval (Husain et al., 2020; Lu et al., 2021a), etc. Code generation tasks include code completion (Li et al., 2018a; Parvez et al., 2018), code repair (Chen et al., 2019; Chakraborty et al., 2020; Lutellier et al., 2020), test generation (Watson et al., 2020; Siddiq et al., 2024; Schäfer et al., 2023), etc. However, while the potential execution result of code is important for both code understanding and generation, this aspect remains largely unexplored (Weber et al., 2024).

3 SURGE

SURGE assesses the model’s ability to approximate execution results across multiple dimensions, including multi-lingual diversity, repository-level complexity, computational intensity, error handling, and scenario-dependent variability. Below, we describe each component of SURGE, including motivation and construction methods.

3.1 Dataset Construction

As illustrated in Figure 3, the construction of SURGE involves four distinct methodologies, each applied to specific components of our eight subsets. For **ML**, **CL**, **BG** components, we employ the Iterative Refactor methodology, where we refine the code through an interactive process involving LLM assistance and human verification. The **RL** component is constructed through Repository Sampling, where we extract and construct test cases from both public and custom code repositories. For **SC**, **TC**, **DR** components, we utilize Manual Implementation, carefully handcrafting code based on selected textbook materials and question collections. Finally, the **FL** component is developed using the Inference & Verification approach, leveraging formal mathematical provers to generate proofs and validate them through compiler verification.

To mitigate the risk of data contamination and answer leakage, we implemented a robust two-fold sanitization strategy across the dataset: (1) We applied **automated filtering** scripts to systematically remove comments from all code snippets before presenting them to the models for evaluation. (2) We **manually inspected** all generated or collected code to identify and remove any comments, ‘assert’ statements, or other annotations that could inadvertently provide hints or reveal the expected output.

3.2 Dataset Components

Multi-lingual Code (ML). A fundamental nature of a general-purpose surrogate executor is its ability to handle multiple programming languages, especially computational languages. Our dataset covers 7 such languages, including C, C++, C#,

Subset	Construction Method	Source	Quantity	Metric	Categories
ML	Iterative Refactor	McEval (Chai et al., 2024)	150	Exact Match	Languages
CL	Iterative Refactor	GitHub	150	Exact Match	Difficulties & Languages
RL	Repository Sampling	GitHub & Custom	60	Mixed	-
SC	Manual Implementation	Custom	150	Mixed	Scenarios
TC	Manual Implementation	Custom	150	Mixed	Scenarios, CPU Time
BG	Iterative Refactor	DebugBench (Tian et al., 2024)	150	Jaccard similarity	Error Type & Languages
DR	Manual Implementation	Custom	200	Jaccard similarity	Variable Type
FL	Inference & Verification	Lean-Workbook (Ying et al., 2024)	150	Custom	-

Table 1: Statistics of SURGE, including construction methods, problem sources, quantities, evaluation metrics, and criteria for further classification. In the table, “custom” refers to customized approaches, and “mixed” indicates multiple methods, which are elaborated in detail in the text.

Java, Rust, Python, and Julia. Our dataset is adapted from McEval (Chai et al., 2024). The original dataset does not provide executable code, so we used an LLM to generate executable code by providing it with prompts, ground truth, and test cases in the original dataset. This generated code was then manually processed; specifically, we (1) modified code that failed to compile (e.g., by adding missing headers) and (2) carefully reviewed the code to prevent answer leakage through assert statements or comments.

Competition-level Code (CL). Next, we consider competition-level code, which presents a higher level of coding difficulty. We collect these tasks from 2 public repositories¹², which contain problems from open coding platforms (e.g. LeetCode, Luogu). The dataset includes problems in 3 languages, C++, Java, and JavaScript. Since the original repositories only provide partial solutions, we first use an LLM to generate complete, executable code that prints the expected output. This generated code is then manually verified. During this process, if issues such as package mismatches or syntax errors (e.g., mixing language versions) arose, we manually revised the code to ensure successful compilation and execution. To investigate whether problem difficulty affects the performance of surrogate models, we classify problems into 5 different difficulty levels.

Repository-level Code (RL). In real-world scenarios, most code exists at the repository level, making repository-level code execution prediction equally important for a general-purpose surrogate model. We manually collect computational repositories that fit within the input length constraints of LLMs. These repositories include tasks such as

solving the 24-point problem, Sudoku solving, and converting Python code to LaTeX. These tasks exhibit complex logic but do not rely on sophisticated models or external inputs. To assess the model’s ability to understand multi-file structures, we also manually construct two repositories containing advanced C++ syntax and multiple files.

Scientific Computing (SC). Scientific computing has long been adopting neural surrogate models. We introduced tasks ranging from solving ordinary differential equations (ODEs) to optimization problems and signal processing. These tasks are motivated by and widely used in real-world scientific challenges, including areas where increasing research has been done on solving these computational tasks through building efficient surrogate models (Wu et al., 2023; Zhang et al., 2023). A comprehensive overview of the setup for each task, along with the corresponding algorithms, can be found in Appendix C.4.1.

Time-Consuming Algorithms (TC). Surrogate models were originally motivated by real-world applications where program execution is high-cost and time-consuming. It’s a necessity for LLMs to generalize well to strongly computation-power-dependent and time-consuming tasks. We include examples from linear algebra, sorting, searching, Monte Carlo simulations, and string matching programs, ensuring a broad representation of computationally intense tasks. These tasks cover various complexity classes, including P (e.g., sorting an array), NP (e.g., Hamiltonian Cycle), and NP-Hard (e.g., Traveling Salesman’s Problem). Additionally, we record the CPU execution time for each program under consistent environments individually to support subsequent studies. A detailed description of this subset is provided in Appendix C.5.1.

¹<https://github.com/azl397985856/leetcode>

²<https://gitee.com/shanire/OJCode>

Buggy Code (BG). Real-world code execution often encounters errors, which pose risks in sensitive scenarios. Therefore, code surrogate models should recognize the presence of bugs. This dataset is adapted from DebugBench (Tian et al., 2024), which extracted Java, Python, and C++ code from LeetCode and manually inserted errors from 4 major bug categories and 18 minor types. Since DebugBench only provides code snippets rather than complete executable programs, we first used an LLM to automatically complete the error-free code into fully runnable versions. After verifying their correctness, we replaced relevant parts with buggy code and executed them again to capture the corresponding error outputs. Some errors resulted in infinite loops, causing timeouts, so we set a 30-second execution filter to avoid such cases.

Code with Differential Results under Different Scenarios (DR). Various contextual factors, such as compiler versions, optimization levels, and language standards, often influence code execution. These variations can lead to different outputs for the same code snippet. We focus specifically on C++ and manually collect code snippets from textbooks and online sources (Bryant and O’Hallaron, 2010; Lippman et al., 2012) that exhibit different behaviors under varying compilation settings. We consider multiple compilers (g++, clang++), C++ standards (03, 11, 14, 17), and optimization levels (-O0, -O1, -O2, -O3, -Os). Each snippet is executed across these different settings, and we retain only those that produce varying outputs through different configurations while discarding cases that yield identical results across all settings.

Mathematics Formal Language (FL). Math-Proving Formal Languages are specialized programming languages designed for mathematical proof verification through compilers (De Moura et al., 2015; Moura and Ullrich, 2021; Paulson, 1994; Barras et al., 1997). These compilers can determine whether a proof is correct and identify specific errors. The verification is very time-consuming. In this study, we focus on Lean4 which is the most widely used proof language. To build our dataset, we use Goedel-Prover (Lin et al., 2025) to conduct large-scale reasoning on Lean-Workbook (Ying et al., 2024) and extract an equal proportion of correct and incorrect proofs. This balanced dataset allows us to evaluate the surrogate model’s ability to assess proof validity effectively.

3.3 Evaluation Metrics

We design different evaluation metrics tailored to each subset of SURGE to ensure accurate evaluation.

In **ML** and **CL**, the outputs are simple numerical values or formatted strings, we employ exact string matching to measure correctness.

For **RL**, we employ different evaluation methods for different tasks. For structured C repositories, we use exact character matching to compare outputs. For Sudoku and 24-point problems, we use edit distance to compare results. For other types of repositories, we apply the Ratcliff/Obershelp (Ratcliff and Metzner, 1988) algorithm.

For **SC** and **TC**, various tasks necessitate distinct evaluation methods. Specifically, (1) numerical simulations are evaluated using the average Relative Absolute Error (RAE); (2) position-based tasks, such as binary search, are assessed through exact string matching; and (3) sorting tasks are evaluated by the rank correlation coefficient (Spearman, 1904). Details regarding the evaluation metrics can be found in Appendix C.4.2 and Appendix C.5.2.

For **BG**, we use the Jaccard similarity (Jaccard, 1901) between predicted and ground truth error messages. For **DR**, since the same code can produce different outputs in varying settings, which sometimes include warnings or errors, we again utilize Jaccard similarity.

For **FL**, the results consist of two parts: (1) whether the proof passes or not, and (2) if it fails, we evaluate the accuracy of the error message. The error message consists of a list containing the error locations and descriptions. We compute the score of a prediction as $\frac{1}{N} \sum_{j=1}^N \mathbb{1}[\hat{p}_j \in P] \cdot J(\hat{m}_j, m_j)$, where N is the number of errors in the ground truth, P is the set of predicted error positions, p_j represents the j -th ground truth error position, $\hat{p}_j$ represents the predicted error position corresponding to p_j , $\mathbb{1}[\hat{p}_j \in P]$ is the indicator function which equals to 1 only when there exists $\hat{p}_j \in P$, m_j is the ground truth error message for position p_j , $\hat{m}_j$ is the predicted error message for position $\hat{p}_j$, and J is the Jaccard similarity function.

3.4 Dataset Statistics

Table 1 presents detailed statistics of SURGE, including the construction methods, problem sources, dataset quantities, number of examples in few-shot scenarios, evaluation metrics, and classification criteria for each subset.

Model	ML									CL	RL	SC	TC	BG			DR	FL	Avg.
	CPP	Rust	Python	Julia	Java	Others	CPP	Java	Python										
Zero-shot																			
Claude-3.5-Sonnet	72.73	55.00	88.00	66.67	76.92	75.00	81.58	57.31	61.55	35.27	9.09	12.55	51.40	12.92	17.92	51.59			
DeepSeek-V3	54.55	60.00	76.00	61.11	46.15	72.50	56.58	44.19	59.65	35.31	4.05	3.03	21.50	10.92	32.46	42.53			
GPT-4o	40.91	45.00	60.00	55.56	57.69	55.00	66.45	49.13	53.16	34.44	4.28	7.48	34.59	14.75	21.99	40.03			
Qwen-Max	50.00	45.00	44.00	27.78	26.92	50.00	38.82	37.15	56.98	35.44	2.82	3.20	30.52	14.03	29.89	32.84			
Qwen-2.5-7B-Instruct	13.64	5.00	12.00	5.56	11.54	17.50	27.63	27.98	22.90	29.43	2.21	3.66	9.46	7.24	36.42	15.48			
Qwen-2.5-32B-Instruct	45.45	20.00	48.00	33.33	42.31	20.00	50.66	22.61	32.50	30.99	1.21	2.09	12.16	7.26	7.65	25.08			
Qwen-2.5-Coder-7B-Instruct	45.45	30.00	52.00	44.44	50.00	42.50	75.00	20.86	45.50	28.00	0.86	3.47	13.53	14.23	40.40	33.75			
Qwen-2.5-Coder-32B-Instruct	59.09	55.00	60.00	44.44	69.23	60.00	80.26	48.43	57.18	18.84	1.49	1.95	17.96	13.42	29.19	41.10			
LLaMA-3.1-8B-Instruct	0.00	0.00	4.00	5.56	15.38	5.00	13.16	20.41	4.41	15.46	4.41	4.12	5.98	3.97	0.00	8.49			
LLaMA-3.1-70B-Instruct	54.55	40.00	52.00	33.33	65.38	47.50	78.29	31.60	48.65	30.19	1.59	4.18	14.27	15.73	39.16	37.10			
Zero-shot Chain-of-Thought																			
Claude-3.5-Sonnet	90.91	65.00	96.00	77.78	69.23	92.50	82.24	62.31	63.38	40.70	16.91	20.69	62.23	18.19	33.98	59.47			
DeepSeek-V3	81.82	85.00	88.00	72.22	69.23	85.00	76.32	62.70	57.57	36.71	4.45	7.85	46.26	16.21	35.19	54.97			
GPT-4o	68.18	65.00	92.00	72.22	76.92	77.50	79.61	53.74	48.56	28.36	8.19	9.97	44.29	14.21	27.91	51.11			
Qwen-Max	86.36	75.00	80.00	72.22	76.92	80.00	71.05	50.49	61.78	36.71	2.65	7.73	46.85	16.16	20.74	52.31			
Qwen-2.5-7B-Instruct	40.91	15.00	32.00	33.33	26.92	47.50	52.63	27.51	25.68	28.95	1.12	3.76	14.94	9.41	36.46	26.41			
Qwen-2.5-32B-Instruct	50.00	40.00	40.00	55.56	38.46	57.50	53.29	32.71	43.29	30.59	3.10	6.96	23.86	11.49	7.39	32.95			
Qwen-2.5-Coder-7B-Instruct	68.18	40.00	40.00	38.89	53.85	57.50	46.05	19.70	40.91	30.19	2.29	4.71	12.77	15.04	37.12	33.81			
Qwen-2.5-Coder-32B-Instruct	77.27	65.00	80.00	55.56	73.08	67.50	71.71	54.58	55.69	34.36	2.05	4.74	22.43	17.62	28.55	47.34			
LLaMA-3.1-8B-Instruct	40.91	15.00	24.00	22.22	26.92	30.00	41.45	17.87	32.65	18.22	1.52	4.23	13.38	10.12	0.66	19.94			
LLaMA-3.1-70B-Instruct	59.09	50.00	72.00	61.11	57.69	52.50	58.55	34.44	43.93	29.76	1.71	3.49	15.02	16.86	25.85	38.80			
Few-shot Chain-of-Thought																			
Claude-3.5-Sonnet	86.36	70.00	96.00	72.22	65.38	82.50	82.24	70.65	63.58	41.00	22.04	23.61	44.15	25.70	31.99	58.49			
DeepSeek-V3	90.91	65.00	84.00	77.78	73.08	95.00	80.26	78.64	66.00	38.60	21.98	15.14	40.27	24.38	35.17	59.08			
GPT-4o	68.18	60.00	88.00	77.78	73.08	75.00	75.66	76.86	59.65	37.12	12.91	7.74	29.52	22.08	26.65	52.68			
Qwen-Max	81.82	70.00	88.00	77.78	73.08	80.00	82.24	72.53	62.32	37.88	19.68	19.78	37.57	23.91	24.76	56.76			
Qwen-2.5-7B-Instruct	27.27	25.00	36.00	38.89	26.92	42.50	48.68	45.19	43.42	28.97	4.92	4.70	12.94	10.66	34.53	28.71			
Qwen-2.5-32B-Instruct	59.09	55.00	52.00	66.67	53.85	60.00	63.16	64.10	63.12	32.53	5.41	6.94	28.66	13.81	22.87	43.15			
Qwen-2.5-Coder-7B-Instruct	54.55	30.00	36.00	44.44	50.00	42.50	58.55	50.48	53.91	30.69	3.90	4.93	14.44	14.02	25.25	34.24			
Qwen-2.5-Coder-32B-Instruct	68.18	75.00	72.00	55.56	65.38	70.00	76.97	64.16	56.37	34.34	3.93	6.49	20.22	19.09	22.57	47.35			
LLaMA-3.1-8B-Instruct	13.64	20.00	20.00	5.56	26.92	22.50	30.26	34.15	47.89	22.27	4.44	4.55	9.66	12.05	13.25	19.14			
LLaMA-3.1-70B-Instruct	54.55	35.00	40.00	22.22	53.85	35.00	68.42	50.83	60.96	30.29	8.00	5.95	18.32	13.27	33.12	35.32			

Table 2: Performance of different models under different prompting strategies on SURGE.

4 Experiments

4.1 Setup

Models. We tested SURGE on 17 open-source and 4 closed-source models of different sizes, including both chat models and code models. The closed-source models include GPT-4o (2024-08-06) (OpenAI, 2024b), GPT-4o-mini (2024-07-18) (OpenAI, 2024a), Claude-3.5-Sonnet (2024-10-22) (Anthropic, 2024a), and Qwen-Max (2025-01-25) (Team, 2024b). The open-source models include LLaMA-3.1-{8, 70}B-Instruct, LLaMA-3.3-70B-Instruct, Qwen-2.5-{0.5, 1.5, 3, 7, 14, 32, 72}B-Instruct, Qwen-2.5-Coder-{0.5, 1.5, 3, 7, 14, 32}B-Instruct and DeepSeek-V3 (671B).

Settings. We tested the above models on SURGE under 3 settings: 0-shot w/o CoT, 0-shot w/ CoT, and few-shot w/ CoT. CoT here means whether we use Chain-of-Thought (Wei et al., 2022) prompting, allowing the models to think step by step, or ask the models to answer directly. We set the temperature to 0, i.e., employing greedy decoding.

4.2 Results

Table 2 presents the performance of 10 selected models across 8 sub-datasets of SURGE under 3 different settings. In this table, we provide a detailed breakdown of the models’ performance on the ML and BG sub-datasets. We present the complete results of all 21 models in Table 5 in Appendix A. From the results, several notable findings emerge:

SURGE demonstrates strong discriminative ability. Even the strongest models perform only moderately well, highlighting the value of our benchmark. The models exhibit significant performance differences across different subsets, reflecting the comprehensiveness of our dataset. Additionally, models that perform well in other tasks, such as Claude-3.5-Sonnet, also achieve substantial overall results on SURGE. This demonstrates the reasonableness of our dataset and its effectiveness in benchmarking LLMs as general-purpose surrogate code executors.

Different prompting strategies lead to varying model performance and have different effects across subsets. We found that for the task of code execution surrogacy, both Chain-of-Thought prompting and few-shot learning can enhance model performance.

Model	Compiler			Standard			Optimization		
	Zero-shot	Zero-shot CoT	Few-shot CoT	Zero-shot	Zero-shot CoT	Few-shot CoT	Zero-shot	Zero-shot CoT	Few-shot CoT
Claude-3.5	12.92	18.19	25.70	14.21	16.75	23.59	16.06	1.23	12.90
GPT-4o	14.75	14.21	22.08	15.33	14.61	20.02	7.66	1.63	1.22
LLaMA-3.1-8B	3.97	10.12	12.05	4.29	10.60	13.17	1.96	3.91	8.04
LLaMA-3.1-70B	15.73	16.86	13.27	16.36	16.27	13.24	15.04	2.24	3.73

Table 3: Model Performance Across Different Variables in DR

Larger model sizes tend to yield better performance on SURGE. From the results, we observe that regardless of whether it is a Qwen-Chat model or a Qwen-Coder model, performance improves as the parameter size increases.

Chat models and coder models exhibit different performance patterns and are affected differently by prompting strategies. We observed that for chat and code models of the same size, code models outperform chat models in the zero-shot setting SURGE. However, in the other two settings, chat models perform better. This suggests that code models have stronger zero-shot surrogate capabilities, whereas chat models excel in reasoning and imitation abilities.

On some sub-datasets of SURGE, stronger models perform worse than smaller, weaker ones. For example, in the FL dataset, we found that this occurs because stronger models tend to actively look for errors in the code, often misidentifying correct code as incorrect. In contrast, smaller models are more inclined to assume that all code is error-free. Since half of the samples in this subset are indeed correct, the smaller models end up achieving better performance.

4.3 Anomaly Analysis

We conducted case studies on anomalous results to better understand model behavior.

Larger Models Underperforming. In some instances, larger models performed worse than their smaller counterparts. For example, on ML tasks, Qwen-2.5-14B-Instruct was outperformed by Qwen-2.5-0.5B-Instruct. Our case study revealed that while the 0.5B model’s reasoning was less detailed, it correctly grasped the code’s core logic. In contrast, the 14B model attempted more elaborate reasoning but often made critical misjudgments (e.g., in conditionals like $\leq$), leading to incorrect results. This suggests that on certain complex reasoning tasks, larger models may be prone to "overthinking" or following incorrect logical paths.

Zero-Shot Failures. We investigated cases of complete failure in the zero-shot setting, such as

LLaMA-3.1-8B-Instruct scoring 0 on ML tasks for C++ and Rust, and on all FL tasks. For ML, the failures were attributed to the inherent difficulty of the test cases and specific language features (e.g., Rust’s strict type system). For FL tasks, the model incorrectly identified errors in all problems. For half of the correct problems, it wrongly predicted errors. For the other half that contained errors, it failed to predict the specific error messages accurately, leading to incorrect predictions in all cases.

5 Analysis

5.1 The Impact of Language Type

In Table 2, we compare model performance across different programming languages.

In the ML subset, LLMs perform best in Python, followed by C++. Python’s simple syntax makes it easier to process, while C++ benefits from its strong presence in programming and system-level tasks. Models also perform well in Julia, likely due to its clean syntax and similarity to Python. However, performance drops significantly in Rust, where strict ownership and lifetime rules introduce complexity, making it hard to predict.

In the BG subset, when predicting the output of buggy code, models excel in Python but struggle with C++. Python’s clear error messages aid prediction, whereas C++’s static typing, manual memory management, and potential for undefined behavior make error handling more difficult.

5.2 The Impact of Problem Difficulty

To analyze how problem difficulty affects model performance, we examine results in the CL subset, as shown in Table 4.

Across all settings, model performance generally declines as problem difficulty increases. However, at the highest difficulty level, performance improves slightly. This anomaly arises because difficulty levels are categorized based on coding complexity, but the hardest problems often involve implementing simple functionality using complex, optimized algorithms. In such cases, models can

Difficulty	1	2	3	4	5
<i>Zero-shot</i>					
Claude-3.5-Sonnet	90.91	81.25	82.05	72.00	79.49
GPT-4o	72.73	56.25	58.97	84.00	61.54
LLaMA-3.1-8B-Instruct	24.24	18.75	7.69	4.00	12.82
LLaMA-3.1-70B-Instruct	96.97	93.75	64.10	64.00	79.49
<i>Zero-shot Chain-of-Thought</i>					
Claude-3.5-Sonnet	96.97	87.50	76.92	72.00	79.49
GPT-4o	96.97	81.25	74.36	80.00	69.23
LLaMA-3.1-8B-Instruct	57.58	43.75	30.77	40.00	38.46
LLaMA-3.1-70B-Instruct	90.91	56.25	48.72	36.00	56.41
<i>Few-shot Chain-of-Thought</i>					
Claude-3.5-Sonnet	96.97	81.25	76.92	68.00	84.62
GPT-4o	93.94	81.25	71.79	60.00	71.79
LLaMA-3.1-8B-Instruct	39.39	18.75	33.33	16.00	33.33
LLaMA-3.1-70B-Instruct	87.88	87.50	48.72	48.00	76.92

Table 4: Model Performance by Difficulty Level

generate correct answers through end-to-end reasoning without fully understanding the underlying code logic. In contrast, levels 1–4 require logical reasoning based on code execution, making prediction harder as complexity increases.

Furthermore, while Chain-of-Thought prompting improves performance, few-shot learning does not and may even degrade results. This is likely because buggy code varies widely, causing few-shot examples to mislead rather than aid the model.

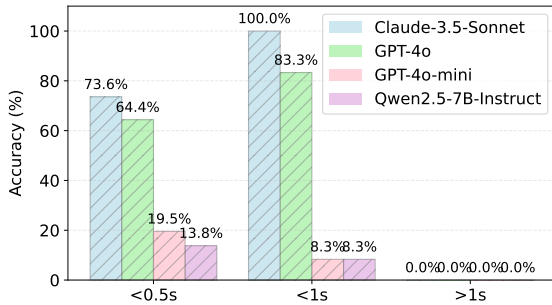


Figure 4: Model's Performance on TC subset across programs with different run time on CPU.

5.3 Prediction Accuracy & CPU Time

We explore the relationship between the execution time of the given code through running on CPUs and the accuracy of using LLMs as surrogate models to acquire the output. We categorize problems in TC into distinct bins based on their execution times and calculate the average accuracy for each model across all samples within the same bin, as shown in Figure 4. We observed the trend of prediction accuracy of the model falling as the actual execution time required for the corresponding pro-

gram prolonged. It's especially worth noting that for computational tasks that require execution time longer than 1 second, even state-of-the-art models struggle to obtain even one correct answer.

5.4 The Impact of Variable Type

The DR subset in SURGE examines model performance in predicting code behavior under different environmental factors. Specifically, DR includes variations in C++ compiler version, C++ standard, and compilation optimization settings. Table 3 presents model performance across different prompting strategies in DR.

In the zero-shot setting, model accuracy improves sequentially across the three factors, suggesting that compiler version differences are harder to predict than standard variations, which in turn are harder than optimization settings. However, with Chain-of-Thought reasoning, performance declines across all factors, with the sharpest drop for optimization settings. This indicates that while CoT aids reasoning for compiler versions and standards, it adds unnecessary complexity for optimizations, ultimately reducing accuracy.

5.5 In-depth Look at Model Behavior

We looked into LLMs' surrogation process and summarized three key observations:

Deep Semantic and Logical Reasoning. LLMs demonstrate a strong ability to interpret complex, language-specific semantics. For instance, when analyzing C++ code with bit fields, models correctly reasoned about the effects of signed vs. unsigned types, bit-width limitations, and how value overflows are handled under two's complement representation. This indicates an understanding of low-level computational logic.

Stateful Algorithmic Tracing. For algorithmic tasks, LLMs effectively simulate the execution process by tracing the program's state. The models' chain-of-thought process shows them iterating through loops, updating variables step-by-step, and applying conditional logic as an interpreter would.

Identification of Computational Boundaries. In a brute-force Traveling Salesman Problem (TSP) solver, models could correctly understand the overall goal and algorithm, but often failed to predict the precise final floating-point value. This suggests their "execution" is a form of sophisticated logical inference, which falters when faced with complex combinatorial calculations that exceed their internal reasoning capacity.

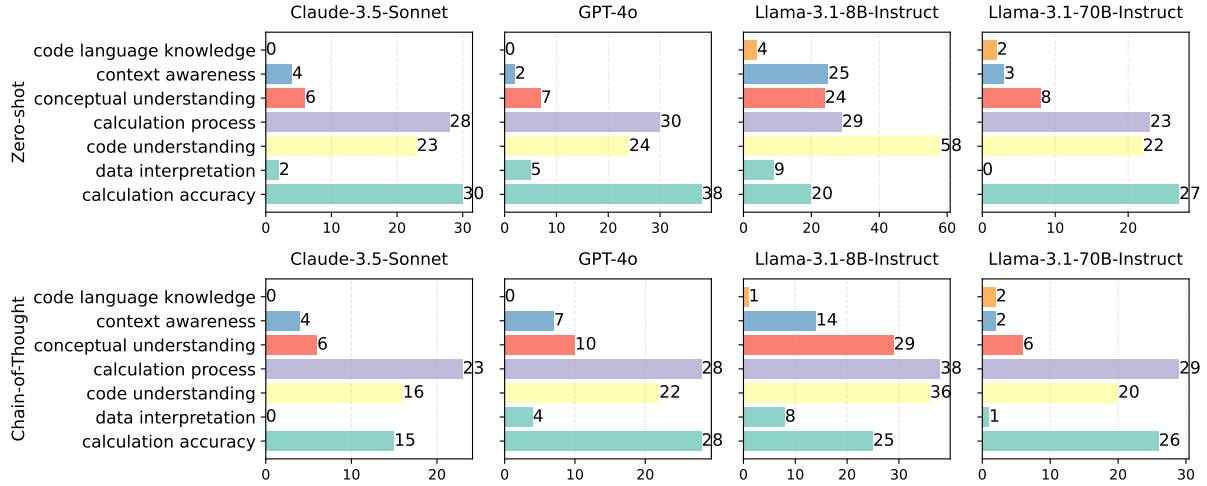


Figure 5: Breakdown of error types across different language models and prompting methods.

5.6 Error Analysis

To further understand the model’s performance and limitations regarding serving as general surrogate models, we categorize the Errors made by Claude-3.5-Sonnet, GPT-4o, and Llama-3.1-8B-Instruct and Llama-3.1-70B-Instruct in the CL subset of SURGE.

We first combined LLM-assisted annotation and manual verification to identify 7 most typical error types: 1. Code Language Knowledge: evaluating foundational programming language proficiency, 2. Context Awareness: measuring understanding of long text and repository-level code, 3. Conceptual Understanding: assessing comprehension of programming concepts, 4. Calculation Process: verifying computational step accuracy, 5. Code Understanding: testing comprehension of code logic and structure, 6. Data Interpretation: evaluating data processing and analysis capabilities, and 7. Calculation Accuracy: Measuring precision in scientific computations. We then use LLM to label errors in the model’s responses. The categorized error statistics are demonstrated in Figure 5.

As models prompted with CoT exhibit fewer instances of most error types compared to zero-shot, especially for the Code Understanding capability of Llama. The main error types are Code Understanding, Calculation Process, and Calculation Accuracy. For zero-shot, the primary error is accuracy, but for CoT, the most frequent error is Calculation Process. This suggests that CoT can better grasp the overall code logic and produce more correct results, but it may still make mistakes in the chain of thought process. In general, CoT has fewer and smaller errors.

From the model perspective, Llama has a clear lead in Conceptual Understanding errors, indicating its weaker ability to understand concepts.

5.7 Training Scale Analysis

We also investigate whether training scaling can affect LLMs’ surrogate execution capabilities on the FL task. We trained models of varying sizes on different amounts of training data sampled from the same distribution, and tested them to predict the error feedbacks for incorrect proofs.

As demonstrated in Figure 2, both model size and training steps are crucial factors in determining surrogate execution accuracy. As we scale from 0.5B to 7B parameters, models consistently show improved learning efficiency and higher performance ceilings throughout the training process. Larger models learn faster in the early stages and continue to improve for longer before plateauing, suggesting better utilization of the training data.

These empirical observations align with established scaling laws in language modeling, indicating that surrogate execution capabilities follow similar scaling patterns as other language tasks.

6 Conclusion

We introduce SURGE, a holistic benchmark for evaluating LLMs as general-purpose surrogate code executors. Through extensive empirical study, we argue that there remains significant room for further improvements on grounding LLMs to facilitate general surrogate models. Our findings not only chart the current landscape but also illuminate a clear path for future research.

Acknowledgements

This work was independently conducted by the authors and is self-funded by BL without institutional affiliation.

Limitations

Despite its comprehensive evaluation, our study has several limitations. LLMs remain approximators rather than exact code executors, often struggling with edge cases, intricate runtime behaviors, and execution-dependent state changes. While SURGE covers diverse execution scenarios, it does not encompass all specialized environments, such as hardware-dependent simulations or real-time systems. Additionally, LLMs may generate plausible but incorrect outputs, particularly in complex logical dependencies or undefined behaviors, making error detection challenging. Our scaling study is constrained by computational resources, limiting the assessment of extremely large models or extensive training data distributions. Furthermore, security risks remain, as LLMs may fail to recognize vulnerabilities, potentially misjudging harmful code. Finally, our benchmark operates in a controlled setting, whereas real-world software development involves dynamic interactions and iterative debugging, which are not fully captured in our study. Future work should focus on improving LLMs' reasoning abilities, enhancing robustness in execution prediction, and integrating them with traditional program analysis techniques for practical deployment.

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Appendix

A Complete Main Results

Model	ML						CL	RL	SC	TC	BG			DR	FL	Avg.
	CPP	Rust	Python	Julia	Java	Others					CPP	Java	Python			
Zero-shot																
Claude-3.5-Sonnet	72.73	55.00	88.00	66.67	76.92	75.00	81.58	57.31	61.55	35.27	9.09	12.55	51.40	12.92	17.92	51.59
DeepSeek-V3	54.55	60.00	76.00	61.11	46.15	72.50	56.58	44.19	59.65	35.31	4.05	3.03	21.50	10.92	32.46	42.53
GPT-4o	40.91	45.00	60.00	55.56	57.69	55.00	66.45	49.13	53.16	34.44	4.28	7.48	34.59	14.75	21.99	40.03
GPT-4o-Mini	59.09	45.00	64.00	33.33	69.23	60.00	84.21	35.33	40.00	31.85	1.39	4.28	13.86	11.65	39.07	39.49
Qwen-Max	50.00	45.00	44.00	27.78	26.92	50.00	38.82	37.15	56.98	35.44	2.82	3.20	30.52	14.03	29.89	32.84
Qwen-2.5-0.5B-Instruct	13.64	10.00	4.00	0.00	11.54	7.50	19.08	5.02	9.43	8.61	1.20	3.77	11.04	4.62	42.38	10.85
Qwen-2.5-1.5B-Instruct	36.36	15.00	24.00	16.67	15.38	35.00	40.79	5.89	12.08	14.15	1.15	3.52	11.10	9.24	41.72	18.80
Qwen-2.5-3B-Instruct	36.36	10.00	28.00	22.22	34.62	22.50	35.53	13.08	20.04	14.61	1.58	3.92	13.27	5.75	15.89	18.49
Qwen-2.5-7B-Instruct	13.64	5.00	12.00	5.56	11.54	17.50	27.63	27.98	22.90	29.43	2.21	3.66	9.46	7.24	36.42	15.48
Qwen-2.5-14B-Instruct	9.09	5.00	8.00	5.56	23.08	5.00	11.18	39.08	33.79	28.18	2.11	2.24	16.30	4.24	7.28	13.34
Qwen-2.5-32B-Instruct	45.45	20.00	48.00	33.33	42.31	20.00	50.66	22.61	32.50	30.99	1.21	2.09	12.16	7.26	7.65	25.08
Qwen-2.5-72B-Instruct	45.45	40.00	52.00	55.56	69.23	52.50	72.37	33.66	53.70	32.46	1.99	2.65	10.69	13.35	34.44	38.00
Qwen-2.5-Coder-0.5B-Instruct	22.73	10.00	20.00	5.56	11.54	22.50	26.97	8.41	6.55	6.39	0.73	2.92	10.05	5.76	41.06	13.41
Qwen-2.5-Coder-1.5B-Instruct	45.45	30.00	32.00	27.78	26.92	35.00	54.61	17.58	20.58	13.19	0.36	2.83	5.43	8.08	41.06	24.06
Qwen-2.5-Coder-3B-Instruct	45.45	20.00	40.00	22.22	46.15	40.00	68.42	21.58	37.43	22.43	1.06	3.61	13.41	8.96	41.06	28.79
Qwen-2.5-Coder-7B-Instruct	45.45	30.00	52.00	44.44	50.00	42.50	75.00	20.86	45.50	28.00	0.86	3.47	13.53	14.23	40.40	33.75
Qwen-2.5-Coder-14B-Instruct	59.09	35.00	48.00	55.56	69.23	62.50	82.89	35.26	51.93	32.20	1.39	3.66	16.12	11.35	41.72	40.39
Qwen-2.5-Coder-32B-Instruct	59.09	55.00	60.00	44.44	69.23	60.00	80.26	48.43	57.18	18.84	1.49	1.95	17.96	13.42	29.19	41.10
LLaMA-3.1-8B-Instruct	0.00	0.00	4.00	5.56	15.38	5.00	13.16	20.41	4.41	15.46	4.41	4.12	5.98	3.97	0.00	8.49
LLaMA-3.1-70B-Instruct	54.55	40.00	52.00	33.33	65.38	47.50	78.29	31.60	48.65	30.19	1.59	4.18	14.27	15.73	39.16	37.10
LLaMA-3.3-70B-Instruct	68.18	50.00	60.00	44.44	57.69	62.50	66.45	43.53	38.45	30.35	2.06	3.23	11.01	11.22	39.13	39.22
Zero-shot Chain-of-Thought																
Claude-3.5-Sonnet	90.91	65.00	96.00	77.78	69.23	92.50	82.24	62.31	63.38	40.70	16.91	20.69	62.23	18.19	33.98	59.47
DeepSeek-V3	81.82	85.00	88.00	72.22	69.23	85.00	76.32	62.70	57.57	36.71	4.45	7.85	46.26	16.21	35.19	54.97
GPT-4o	68.18	65.00	92.00	72.22	76.92	77.50	79.61	53.74	48.56	28.36	8.19	9.97	44.29	14.21	27.91	51.11
GPT-4o-Mini	77.27	60.00	88.00	50.00	69.23	80.00	75.66	34.46	40.60	29.59	1.77	5.40	21.04	13.16	33.11	45.29
Qwen-Max	86.36	75.00	80.00	72.22	76.92	80.00	71.05	50.49	61.78	36.71	2.65	7.73	46.85	16.16	20.74	52.31
Qwen-2.5-0.5B-Instruct	27.27	10.00	16.00	0.00	3.85	17.50	22.37	6.29	1.11	5.28	1.22	3.41	9.15	5.21	37.09	11.84
Qwen-2.5-1.5B-Instruct	31.82	15.00	20.00	11.11	19.23	27.50	26.32	12.47	8.14	12.77	1.22	3.23	9.81	4.93	39.74	16.22
Qwen-2.5-3B-Instruct	40.91	40.00	32.00	22.22	30.77	35.00	25.00	15.01	20.78	12.84	2.14	2.86	5.29	7.12	13.93	20.39
Qwen-2.5-7B-Instruct	40.91	15.00	32.00	33.33	26.92	47.50	52.63	27.51	25.68	28.95	1.12	3.76	14.94	9.41	36.46	26.41
Qwen-2.5-14B-Instruct	68.18	55.00	76.00	61.11	65.38	72.50	61.18	43.89	36.49	32.07	1.57	3.15	19.13	11.97	8.67	41.09
Qwen-2.5-32B-Instruct	50.00	40.00	40.00	55.56	38.46	57.50	53.29	32.71	43.29	30.59	3.10	6.96	23.86	11.49	7.39	32.95
Qwen-2.5-72B-Instruct	68.18	80.00	96.00	55.56	76.92	77.50	65.13	45.30	53.39	32.95	1.72	3.19	16.32	16.61	29.80	47.90
Qwen-2.5-Coder-0.5B-Instruct	13.64	0.00	4.00	5.56	3.85	7.50	1.97	3.07	2.14	3.98	2.14	2.44	2.83	2.23	33.77	6.36
Qwen-2.5-Coder-1.5B-Instruct	31.82	10.00	28.00	5.56	15.38	22.50	19.08	26.39	20.08	15.42	1.16	3.60	11.46	7.24	39.74	17.16
Qwen-2.5-Coder-3B-Instruct	50.00	15.00	32.00	22.22	42.31	40.00	52.63	13.13	33.96	20.14	1.24	3.72	13.36	7.63	40.40	25.85
Qwen-2.5-Coder-7B-Instruct	68.18	40.00	40.00	38.89	53.85	57.50	46.05	19.70	40.91	30.19	2.29	4.71	12.77	15.04	37.12	33.81
Qwen-2.5-Coder-14B-Instruct	59.09	45.00	60.00	55.56	69.23	62.50	71.71	26.09	52.12	33.09	3.19	5.21	18.58	13.41	34.44	40.61
Qwen-2.5-Coder-32B-Instruct	77.27	65.00	80.00	55.56	73.08	67.50	71.71	54.58	55.69	34.36	2.05	4.74	22.43	17.62	28.55	47.34
LLaMA-3.1-8B-Instruct	40.91	15.00	24.00	22.22	26.92	30.00	41.45	17.87	32.65	18.22	1.52	4.23	13.38	10.12	0.66	19.94
LLaMA-3.1-70B-Instruct	59.09	50.00	72.00	61.11	57.69	52.50	58.55	34.44	43.93	29.76	1.71	3.49	15.02	16.86	25.85	38.80
LLaMA-3.3-70B-Instruct	63.64	45.00	56.00	55.56	57.69	67.50	57.24	35.88	39.50	30.61	3.34	3.95	13.53	16.38	35.11	38.73
Few-shot Chain-of-Thought																
Claude-3.5-Sonnet	86.36	70.00	96.00	72.22	65.38	82.50	82.24	70.65	63.58	41.00	22.04	23.61	44.15	25.70	31.99	58.49
DeepSeek-V3	90.91	65.00	84.00	77.78	73.08	95.00	80.26	78.64	66.00	38.60	21.98	15.14	40.27	24.38	35.17	59.08
GPT-4o	68.18	60.00	88.00	77.78	73.08	75.00	75.66	76.86	59.65	37.12	12.91	7.74	29.52	22.08	26.65	52.68
GPT-4o-Mini	77.27	55.00	80.00	50.00	73.08	72.50	71.05	63.89	55.87	34.20	17.89	9.95	23.75	18.24	24.68	48.49
Qwen-Max	81.82	70.00	88.00	77.78	73.08	80.00	82.24	72.53	62.32	37.88	19.68	19.78	37.57	23.91	24.76	56.76
Qwen-2.5-0.5B-Instruct	18.18	5.00	4.00	0.00	7.69	10.00	17.11	17.82	32.32	6.20	3.51	4.83	5.17	5.29	19.21	11.17
Qwen-2.5-1.5B-Instruct	27.27	15.00	16.00	16.67	11.54	27.50	19.74	9.88	31.44	13.20	3.76	3.66	8.15	7.17	41.72	16.85
Qwen-2.5-3B-Instruct	45.45	30.00	28.00	11.11	11.54	27.50	27.63	17.40	38.70	17.74	7.67	6.45	9.09	10.21	35.25	21.58
Qwen-2.5-7B-Instruct	27.27	25.00	36.00	38.89	26.92	42.50	48.68	45.19	43.42	28.97	4.92	4.70	12.94	10.66	34.53	28.71
Qwen-2.5-14B-Instruct	63.64	55.00	60.00	66.67	61.54	70.00	57.24	53.59	49.99	32.48	3.29	4.40	17.88	14.10	10.76	41.37
Qwen-2.5-32B-Instruct	59.09	55.00	52.00	66.67	53.85	60.00	63.16	64.10	63.12	32.53	5.41	6.94	28.66	13.81	22.87	43.15
Qwen-2.5-72B-Instruct	63.64	75.00	88.00	72.22	69.23	80.00	70.39	67.98	61.45	34.92	2.89	3.05	9.52	18.43	33.18	49.99
Qwen-2.5-Coder-0.5B-Instruct	9.09	0.00	0.00	0.00	0.00	2.50	1.32	13.88	13.18	5.62	6.66	4.42	2.15	5.19	37.75	9.25
Qwen-2.5-Coder-1.5B-Instruct	4.55	5.00	16.00	0.00	15.38	5.00	1.97	28.79	38.97	15.25	1.24	3.28	9.70	9.90	33.77	13.49
Qwen-2.5-Coder-3B-Instruct	36.36	45.00	32.00	27.78	30.77	37.50	50.00	27.43	40.84	23.31	1.28	4.06	12.00	9.64	38.41	27.76
Qwen-2.5-Coder-7B-Instruct	54.55	30.00	36.00	44.44	50.00	42.50	58.55	50.48	53.91	30.69	3.90	4.93	14.44	14.02	25.25	34.24
Qwen-2.5-Coder-14B-Instruct	63.64	40.00	52.00	38.89	65.38	62.50	77.63	55.01	52.87	32.29	5.99	5.01	15.76	13.39	32.62	40.87
Qwen-2.5-Coder-32B-Instruct	68.18	75.00	72.00	55.56	65.38	70.00	76.97	64.16	56.37	34.34	3.93	6.49	20.22	19.09	22.57	47.35
LLaMA-3.1-8B-Instruct	13.64	20.00	20.00	5.56	26.92	22.50	30.26	34.15	47.89	22.27	4.44	4.55	9.66	12.05	13.25	19.14
LLaMA-3.1-70B-Instruct	54.55	35.00	40.00	22.22	53.85	35.00	68.42	50.83	60.96	30.29	8.00	5.95	18.32	13.27	33.12	35.32
LLaMA-3.3-70B-Instruct	63.64	35.00	40.00	27.78	46.15	35.00	49.34	60.45	63.84	32						

Table 5: Performance of different models under different prompting strategies on SURGE.

B Prompts

B.1 Prompts for Dataset Refactoring

ML:

I will provide you with a code problem with a solution. You need to generate a complete, executable code based on the raw json data, including all necessary package imports, the original code, the test cases, and the main function. You need to generate the executable code and expected result. Please choose a test case according to the 'test' field from raw json data, and the code should print the answer of the test case. The output should be json format, with code and expected_result fields. Please only generate the number or string answer in 'expected_result' field without any extra description.

CL:

I will provide you with the solution to a code problem in cpp, python, and javascript. You need to score according to the difficulty of the problem from 1 to 5, while 5 means the hardest. And generate topic keywords for the problem. The output should only be json format, with difficulty and keywords fields. difficulty: 1-5, integer keywords: two or three words to best describe the problem, string list

BG:

I will provide you with a piece of code and some test cases. You need to generate a complete, executable code based on these, including all necessary package imports, the original code, the test cases, and the main function. You should wrap the original code with ORIGINAL_CODE_START and ORIGINAL_CODE_END comments. Additionally, the program should output the results of the test cases. Do not include expected output in your answer.

C Details of SURGE

C.1 ML

Java	C#	Rust	Julia	Python	C++	C
25	20	20	26	18	21	20

Table 6: Language usage count across different categories in the ML subset.

In ML, the usage distribution of various programming languages is shown in Table 6. We selected a variety of languages, including Java, C#, Rust, Julia, Python, C++, and C, to evaluate the model's ability to handle multilingual code. This diverse selection helps to comprehensively assess the model's performance across different languages.

C.1.1 System Prompts

Zero-shot Chain-of-Thought:

Given the following code, what is the execution result? You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>

Zero-shot:

Given the following code, what is the execution result? Your answer should be in the following format:
Output:
<execution result>

Few-shot Chain-of-Thought:

Given the following code, what is the execution result? You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>
Following are 3 examples:
{{examples here}}

C.1.2 Demo Questions

```
def catalan_number(n: int) -> int:
    # Initialize an array to store the intermediate catalan numbers
    catalan = [0] * (n + 1)
    catalan[0] = 1 # Base case

    # Calculate catalan numbers using the recursive formula
    for i in range(1, n + 1):
        for j in range(i):
            catalan[i] += catalan[j] * catalan[i - j - 1]

    return catalan[n]

if __name__ == "__main__":
    # Run the test function and print the result of a specific test case
    print(catalan_number(3))
```

```
import java.util.*;

class Solution {
    public static int countPrefixWords(List<String> wordList, String prefix) {

        int count = 0;
        for (String word : wordList) {
            if (word.startsWith(prefix)) {
                count++;
            }
        }
        return count;
    }
}
```

```

public static void main(String[] args) {
    System.out.println(countPrefixWords(Arrays.
        asList("dog", "dodge", "dot", "dough"), "do"));
}
}

```

```

#include <assert.h>
#include <stdio.h>

```

```

long long minTotalCost(int n, int *C)
{
    return (long long)(C[n-2]) * (n - 1) + C[n-1];
}

```

```

int main() {
    int costs3[] = {5, 4, 3, 2};
    printf("%lld\n", minTotalCost(4, costs3));
    return 0;
}

```

```

function merge_sorted_arrays(nums1::Vector{Int}, m::Int,
nums2::Vector{Int}, n::Int) :: Vector{Int}
    i = m
    j = n
    k = m + n

    while j > 0
        if i > 0 && nums1[i] > nums2[j]
            nums1[k] = nums1[i]
            i -= 1
        else
            nums1[k] = nums2[j]
            j -= 1
        end
        k -= 1
    end

    nums1
end

```

```

# Test case
result = merge_sorted_arrays([1, 3, 5, 0, 0, 0], 3, [2, 4, 6],
3)
println(result)

```

```

public class Solution {

    public static int findSmallestInteger(int n) {
        char[] characters = Integer.toString(n).toCharArray();
        int i = characters.length - 2;

        // Find the first digit that is smaller than the digit next
        // to it.
        while (i >= 0 && characters[i] >= characters[i + 1]) {
            i--;
        }

        if (i == -1) {
            return -1; // Digits are in descending order, no
            // greater number possible.
        }

        // Find the smallest digit on right side of (i) which is
        // greater than characters[i]
        int j = characters.length - 1;

```

```

while (characters[j] <= characters[i]) {
    j--;
}

// Swap the digits at indices i and j
swap(characters, i, j);

// Reverse the digits from index i+1 to the end of the
// array
reverse(characters, i + 1);

try {
    return Integer.parseInt(new String(characters));
} catch (NumberFormatException e) {
    return -1; // The number formed is beyond the
    // range of int.
}

}

private static void swap(char[] arr, int i, int j) {
    char temp = arr[i];
    arr[i] = arr[j];
    arr[j] = temp;
}

private static void reverse(char[] arr, int start) {
    int end = arr.length - 1;
    while (start < end) {
        swap(arr, start, end);
        start++;
        end--;
    }
}

public static void main(String[] args) {
    System.out.println(findSmallestInteger(123));
}
}

```

C.2 CL

Python	C++	JavaScript
50	51	49

Table 7: Language usage count across different categories in the CL subset.

Difficulty	JavaScript	CPP	Python
1	10	11	11
2	6	4	6
3	12	14	12
4	8	8	9
5	13	14	12

Table 8: Details of problems in different languages and different difficulty levels.

In CL, we selected competition problems of varying difficulty, each with solutions in Python, C++,

and JavaScript. You can see the distribution of language in Table 7, and the distribution of problem difficulty in Table 8. This selection allows us to test the model's cross-language capabilities and its ability to handle problems of different difficulty levels.

C.2.1 System Prompts

Zero-shot Chain-of-Thought:

Given the following code, what is the execution result?
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>

Zero-shot:

Given the following code, what is the execution result?
Your answer should be in the following format:
Output:
<execution result>

Few-shot Chain-of-Thought:

Given the following code, what is the execution result?
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>
Following are 3 examples:
{ {examples here} }

C.2.2 Demo Questions

```
class TreeNode {
  constructor(val) {
    this.val = val;
    this.left = this.right = null;
  }
}

function maxDepth(root) {
  if (!root) return 0;
  const queue = [root, null];
  let depth = 1;

  while (queue.length > 0) {
    const node = queue.shift();
    if (node === null) {
      if (queue.length === 0) return depth;
      depth++;
      queue.push(null);
      continue;
    }
    if (node.left) queue.push(node.left);
    if (node.right) queue.push(node.right);
  }

  return depth;
}
```

```
// Test case
const root = new TreeNode(3);
root.left = new TreeNode(9);
root.right = new TreeNode(20);
root.right.left = new TreeNode(15);
root.right.right = new TreeNode(7);
console.log(maxDepth(root));
```

```
from collections import Counter
class Solution:
    def maxScoreWords(self, words, letters, score):
        self.ans = 0
        words_score = [sum(score[ord(c)-ord('a')]) for c
                        in word) for word in words]
        words_counter = [Counter(word) for word in words]

        def backtrack(start, cur, counter):
            if start > len(words):
                return
            self.ans = max(self.ans, cur)
            for j, w_counter in enumerate(words_counter
                                         [start:], start):
                if all(n <= counter.get(c,0) for c,n in
                     w_counter.items()):
                    backtrack(j+1, cur+words_score[j],
                             counter-w_counter)

        backtrack(0, 0, Counter(letters))
        return self.ans

solution = Solution()
print(solution.maxScoreWords(["dog","cat","dad","good"],
                             ["a","a","c","d","d","d","g","o","o"],
                             [1,0,9,5,0,0,3,0,0,0,0,0,0,0,
                              2,0,0,0,0,0,0,0,0,0,0]))
```

```
#include <iostream>
#include <unordered_map>
#include <string>
using namespace std;

int findTheLongestSubstring(string s) {
    unordered_map<char, int> mapper = {{ 'a', 1 }, { 'e',
2 }, { 'i', 4 }, { 'o', 8 }, { 'u', 16 }};
    unordered_map<int, int> seen;
    seen[0] = -1;
    int max_len = 0, cur = 0;

    for(int i = 0; i < s.size(); ++i){
        if(mapper.find(s[i]) != mapper.end()){
            cur ^= mapper[s[i]];
        }
        if(seen.find(cur) != seen.end()){
            max_len = max(max_len, i - seen[cur]);
        } else {
            seen[cur] = i;
        }
    }

    return max_len;
}

// Test case
class Solution {
public:
```

```

void solve() {
    string input = "eleetminicoworoep";
    cout << findTheLongestSubstring(input) << endl;
    // Expected output: 13
}
};

int main(){
    Solution sol;
    sol.solve();
    return 0;
}

```

```

class TreeNode {
    constructor(val) {
        this.val = val;
        this.left = this.right = null;
    }
}

function backtrack(root, sum, res, tempList) {
    if (root === null) return;
    if (root.left === null && root.right === null && sum
        === root.val)
        return res.push([...tempList, root.val]);

    tempList.push(root.val);
    backtrack(root.left, sum - root.val, res, tempList);
    backtrack(root.right, sum - root.val, res, tempList);
    tempList.pop();
}

function pathSum(root, sum) {
    if (root === null) return [];
    const res = [];
    backtrack(root, sum, res, []);
    return res;
}

```

```

// Test case setup
const root = new TreeNode(5);
root.left = new TreeNode(4);
root.right = new TreeNode(8);
root.left.left = new TreeNode(11);
root.right.left = new TreeNode(13);
root.right.right = new TreeNode(4);
root.left.left.left = new TreeNode(7);
root.left.left.right = new TreeNode(2);
root.right.right.left = new TreeNode(5);
root.right.right.right = new TreeNode(1);

console.log(pathSum(root, 22));

```

```

class TrieNode {
    constructor() {
        this.children = {};
        this.isEndOfWord = false;
    }
}

class Trie {
    constructor() {
        this.root = new TrieNode();
    }

    insert(word) {
        let node = this.root;

```

```

        for (let char of word) {
            if (!node.children[char]) {
                node.children[char] = new TrieNode();
            }
            node = node.children[char];
        }
        node.isEndOfWord = true;
    }

    search(stream) {
        let node = this.root;
        for (let char of stream) {
            if (!node.children[char]) {
                return false;
            }
            node = node.children[char];
            if (node.isEndOfWord) {
                return true;
            }
        }
        return false;
    }
}

class StreamChecker {
    constructor(words) {
        this.trie = new Trie();
        this.stream = [];

        for (let word of [...new Set(words)]) {
            this.trie.insert(word.split('').reverse().join(''));
        }
    }

    query(letter) {
        this.stream.unshift(letter);
        return this.trie.search(this.stream);
    }
}

```

```

// Test case
const streamChecker = new StreamChecker(["cd", "f", "kl"]);
console.log(streamChecker.query('a')); // false
console.log(streamChecker.query('b')); // false
console.log(streamChecker.query('c')); // false
console.log(streamChecker.query('d')); // true
console.log(streamChecker.query('e')); // false
console.log(streamChecker.query('f')); // true
console.log(streamChecker.query('g')); // false
console.log(streamChecker.query('h')); // false
console.log(streamChecker.query('i')); // false
console.log(streamChecker.query('j')); // false
console.log(streamChecker.query('k')); // false
console.log(streamChecker.query('l')); // true

```

C.3 RL

Python	C++
24	36

Table 9: Language usage count across different categories in the RL subset.

In RL, the distribution of programming language usage is shown in Table 9. We utilized five GitHub repositories for this study, consisting of two Python projects and three C++ projects. Each repository contains a set of ten or more test cases, providing a diverse set of data for evaluation across different programming languages.

C.3.1 System Prompts

Zero-shot Chain-of-Thought:

You will be given a github repository and a function that generates a latex file with this repo. Your task is to predict the content of the latex file generated by the function. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<file content>

Zero-shot:

You will be given a github repository and a function that generates a latex file with this repo. Your task is to predict the content of the latex file generated by the function. Your answer should be in the following format:
Output:
<file content>

Few-shot Chain-of-Thought:

You will be given a github repository and a function that generates a latex file with this repo. Your task is to predict the content of the latex file generated by the function. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<file content>
Following is one example:
{ {examples here} }

C.3.2 Demo Questions

```
main.cpp:<start_file>#include <iostream>
#include <vector>
#include <utility>
#include <stdlib.h>
#include <time.h>
#include <unistd.h>
#include <fstream>
#include <map>
using namespace std;

typedef vector<vector<char>> Board;

const int N = 9;

class SudokuPlayer
{
private:
    int rowUsed[N];
```

```
    int columnUsed[N];
    int blockUsed[N];

public:
    vector<Board> result;
    vector<pair<int, int>> spaces;

public:
    SudokuPlayer()
    {
        initState();
    }

    void initState()
    {
        memset(rowUsed, 0, sizeof(rowUsed));
        memset(columnUsed, 0, sizeof(columnUsed));
        memset(blockUsed, 0, sizeof(blockUsed));
        spaces.clear();
        result.clear();
    }

    void addResult(Board &board)
    {
        vector<vector<char>> obj(board);
        result.push_back(obj);
    }

    void flip(int i, int j, int digit)
    {
        rowUsed[i] ^= (1 << digit);
        columnUsed[j] ^= (1 << digit);
        blockUsed[(i / 3) * 3 + j / 3] ^= (1 << digit);
    }

    vector<Board> solveSudoku(Board board)
    {
        initState();
        for (int i = 0; i < N; i++)
        {
            for (int j = 0; j < N; j++)
            {
                if (board[i][j] == '$')
                {
                    spaces.push_back(pair<int, int>(i, j));
                }
                else
                {
                    int digit = board[i][j] - '1';
                    flip(i, j, digit);
                }
            }
        }
        DFS(board, 0);
        return result;
    }

    void DFS(Board &board, int pos)
    {
        if (pos == spaces.size())
        {
            addResult(board);
            return;
        }
        int i = spaces[pos].first;
        int j = spaces[pos].second;
        int mask = ~(rowUsed[i] | columnUsed[j] |
            blockUsed[(i / 3) * 3 + j / 3]) & 0x1ff;
```

```

int digit = 0;
while (mask)
{
    if (mask & 1)
    {
        flip(i, j, digit);
        board[i][j] = '1' + digit;
        DFS(board, pos + 1);
        flip(i, j, digit);
    }
    mask = mask >> 1;
    digit++;
}

void getResult()
{
    for (size_t i = 0; i < result.size(); i++)
    {
        Board board = result[i];
        printBoard(board);
    }
}

bool checkBoard(Board &board)
{
    initState();
    for (int i = 0; i < 9; i++)
    {
        for (int j = 0; j < 9; j++)
        {
            if (board[i][j] != '$')
            {
                int digit = board[i][j] - '1';
                if ((rowUsed[i] | columnUsed[j] |
                    blockUsed[(i / 3) * 3 + j / 3]) & (1
                    << digit))
                {
                    return false;
                }
                flip(i, j, digit);
            }
        }
    }
    return true;
}

void printBoard(Board &board)
{
    for (int i = 0; i < board.size(); i++)
    {
        for (int j = 0; j < board[i].size(); j++)
        {
            cout << board[i][j] << " ";
        }
        cout << "\n";
    }
}

Board generateBoard(int digCount)
{
    vector<vector<char>> board(N, vector<char>(N,
    '$'));
    vector<int> row = getRand9();
    for (int i = 0; i < 3; i++)
    {
        board[3][i + 3] = row[i] + '1';
        board[4][i + 3] = row[i + 3] + '1';
        board[5][i + 3] = row[i + 6] + '1';
    }
}

```

```

}
copySquare(board, 3, 3, true);
copySquare(board, 3, 3, false);
copySquare(board, 3, 0, false);
copySquare(board, 3, 6, false);

while (digCount)
{
    int x = rand() % 9;
    int y = rand() % 9;
    if (board[x][y] == '$')
        continue;
    char tmp = board[x][y];
    board[x][y] = '$';

    solveSudoku(board);
    if (result.size() == 1)
    {
        digCount--;
    }
    else
    {
        board[x][y] = tmp;
    }
}
// printBoard(board);
// cout << "spaces " << player.spaces.size() << "\n";
if (!checkBoard(board))
{
    cout << "wrong board" << endl;
}

return board;
}

vector<int> getRand9()
{
    vector<int> result;
    int digit = 0;
    while (result.size() != 9)
    {
        int num = rand() % 9;
        if ((1 << num) & digit)
        {
            continue;
        }
        else
        {
            result.push_back(num);
            digit ^= (1 << num);
        }
    }
    return result;
}

void copySquare(Board &board, int src_x, int src_y,
bool isRow)
{
    int rand_tmp = rand() % 2 + 1;
    int order_first[3] = {1, 2, 0};
    int order_second[3] = {2, 0, 1};
    if (rand_tmp == 2)
    {
        order_first[0] = 2;
        order_first[1] = 0;
        order_first[2] = 1;
        order_second[0] = 1;
        order_second[1] = 2;
    }
}

```

```

        order_second[2] = 0;
    }
    for (int i = 0; i < 3; i++)
    {
        if (isRow)
        {
            board[src_x][i] = board[src_x +
            order_first[0]][src_y + i];
            board[src_x + 1][i] = board[src_x +
            order_first[1]][src_y + i];
            board[src_x + 2][i] = board[src_x +
            order_first[2]][src_y + i];
            board[src_x][i + 6] = board[src_x +
            order_second[0]][src_y + i];
            board[src_x + 1][i + 6] = board[src_x +
            order_second[1]][src_y + i];
            board[src_x + 2][i + 6] = board[src_x +
            order_second[2]][src_y + i];
        }
        else
        {
            board[i][src_y] = board[src_x + i][src_y
            + order_first[0]];
            board[i][src_y + 1] = board[src_x + i][
            src_y + order_first[1]];
            board[i][src_y + 2] = board[src_x + i][
            src_y + order_first[2]];
            board[i + 6][src_y] = board[src_x + i][
            src_y + order_second[0]];
            board[i + 6][src_y + 1] = board[src_x + i
            ][src_y + order_second[1]];
            board[i + 6][src_y + 2] = board[src_x + i
            ][src_y + order_second[2]];
        }
    }
}
};

char data[9][9] = {
    {'5', '3', '.', '.', '.', '7', '.', '.', '.', '.'},
    {'6', '.', '.', '1', '9', '5', '.', '.', '.'},
    {'.', '9', '8', '.', '.', '.', '6', '.', '.'},
    {'8', '.', '.', '6', '.', '.', '3', '.', '.'},
    {'4', '.', '.', '8', '.', '3', '.', '.', '1'},
    {'7', '.', '.', '2', '.', '.', '6', '.', '.'},
    {'.', '6', '.', '.', '2', '8', '.', '.'},
    {'.', '.', '4', '1', '9', '.', '.', '5'},
    {'.', '.', '8', '.', '7', '9', '.', '.'};
};

void test()
{
    SudokuPlayer player;
    vector<vector<char>> board(N, vector<char>(N, '.'))
    ;

    for (int i = 0; i < board.size(); i++)
    {
        for (int j = 0; j < board[i].size(); j++)
        {
            board[i][j] = data[i][j];
        }
    }
    bool check = player.checkBoard(board);
    if (check)
        cout << "checked" << endl;

    player.solveSudoku(board);
    player.getResult();
}

```

```

        cout << endl;
    }

vector<Board> readFile(string filePath)
{
    ifstream infile;
    vector<Board> boards;
    infile.open(filePath);
    char data[100];
    Board tmp;
    vector<char> row;
    while (!infile.eof())
    {
        infile.getline(data, 100);
        if (data[0] == '-')
        {
            boards.push_back(Board(tmp));
            tmp.clear();
            continue;
        }
        for (int i = 0; i < strlen(data); i++)
        {
            if (('1' <= data[i] && data[i] <= '9') || data[i]
            == '$')
            {
                row.push_back(data[i]);
            }
        }
        tmp.push_back(vector<char>(row));
        row.clear();
    }
    infile.close();
    return boards;
}

void writeFile(vector<Board> boards, ofstream &f)
{
    for (int k = 0; k < boards.size(); k++)
    {
        for (int i = 0; i < boards[k].size(); i++)
        {
            for (int j = 0; j < boards[k][i].size(); j++)
            {
                f << boards[k][i][j] << " ";
            }
            f << "\n";
        }
        f << "----- " << k << " -----" << endl;
    }
}

map<char, string> parse(int argc, char *argv[])
{
    map<char, string> params;
    int completeBoardCount, gameNumber, gameLevel;
    vector<int> range;
    string inputFile;
    char opt = 0;
    while ((opt = getopt(argc, argv, "c:s:n:m:r:u")) != -1)
    {
        switch (opt)
        {
            case 'c':
                completeBoardCount = atoi(optarg);
                if (completeBoardCount < 1 ||
                completeBoardCount > 1000000)
                {
                    exit(0);
                }
            }
        }
    }
}

```

```

        params[opt] = string(optarg);
        break;
    case 's':
        inputFile = string(optarg);
        if (access(optarg, 0) == -1)
        {
            printf("file does not exist\n");
            exit(0);
        }
        params[opt] = string(optarg);
        break;
    case 'n':
        gameNumber = atoi(optarg);
        if (gameNumber < 1 || gameNumber > 10000)
        {
            exit(0);
        }
        params[opt] = string(optarg);
        break;
    case 'm':
        gameLevel = atoi(optarg);
        if (gameLevel < 1 || gameLevel > 3)
        {
            exit(0);
        }
        params[opt] = string(optarg);
        break;
    case 'r':
        char *p;
        p = strtok(optarg, "~");
        while (p)
        {
            range.push_back(atoi(p));
            p = strtok(NULL, "~");
        }
        if (range.size() != 2)
        {
            exit(0);
        }
        if ((range[0] >= range[1]) || range[0] < 20 || range[1] > 55)
        {
            exit(0);
        }
        params[opt] = string(optarg);
        break;
    case 'u':
        params[opt] = string();
        break;
    default:
        exit(0);
        break;
    }
}
return params;
}

void generateGame(int gameNumber, int gameLevel,
vector<int> digCount, ofstream &outfile, SudokuPlayer &
player)
{
    for (int i = 0; i < gameNumber; i++)
    {
        int cnt = 0;
        if (digCount.size() == 1)
        {
            cnt = digCount[0];
        }
    }
}

```

```

    else
    {
        cnt = rand() % (digCount[1] - digCount[0] +
1) + digCount[0];
    }
    Board b = player.generateBoard(cnt);
    vector<Board> bs;
    bs.push_back(b);
    writeFile(bs, outfile);
}
outfile.close();
}

int main(int argc, char *argv[])
{
    srand((unsigned)time(NULL));
    SudokuPlayer player;

    map<char, string> params = parse(argc, argv);
    map<char, string>::iterator it, tmp;

    int opt = 0;

    vector<int> range;
    int gameNumber;
    int gameLevel = 0;
    int solution_count = 0;

    vector<Board> boards;
    ofstream outfile;

    it = params.begin();
    while (it != params.end())
    {
        switch (it->first)
        {
            case 'c':
                outfile.open("game.txt", ios::out | ios::trunc);
                range.push_back(0);
                generateGame(atoi(it->second.c_str()), 0,
range, outfile, player);
                range.clear();
                break;

            case 's':
                outfile.open("sudoku.txt", ios::out | ios::trunc
);
                boards = readFile(it->second);
                for (int i = 0; i < boards.size(); i++)
                {
                    vector<Board> result = player.
solveSudoku(boards[i]);
                    writeFile(result, outfile);
                }
                outfile.close();
                break;

            case 'n':
            case 'm':
            case 'r':
            case 'u':
                tmp = params.find('n');
                if (tmp == params.end())
                {
                    exit(0);
                }

                gameNumber = atoi(tmp->second.c_str());

```

```

        tmp = params.find('u');
        if (tmp != params.end())
        {
            solution_count = 1;
        }

        tmp = params.find('m');
        if (tmp != params.end())
        {
            gameLevel = atoi(tmp->second.c_str());
        }

        tmp = params.find('r');
        if (tmp != params.end())
        {
            char *p;
            char *pc = new char[100];
            strcpy(pc, tmp->second.c_str());
            p = strtok(pc, "~");
            while (p)
            {
                range.push_back(atoi(p));
                p = strtok(NULL, "~");
            }
        }
        else
        {
            if (gameLevel == 1)
            {
                range.push_back(20);
                range.push_back(30);
            }
            else if (gameLevel == 2)
            {
                range.push_back(30);
                range.push_back(40);
            }
            else if (gameLevel == 3)
            {
                range.push_back(40);
                range.push_back(55);
            }
            else
            {
                range.push_back(20);
                range.push_back(55);
            }
        }

        outfile.open("game.txt", ios::out | ios::trunc);
        generateGame(gameNumber, gameLevel,
            range, outfile, player);
        range.clear();
        break;
    }
    // cout << it->first << ' ' << it->second << endl;
    it++;
}

return 0;
}<end_file>;game.txt:<start_file><9 $ 5 $ 3 $ 7 1 2
$ 1 2 $ $ 8 3 $ $
$ $ $ 2 7 $ 9 8 5
8 $ 9 $ 6 $ 1 2 7
1 $ $ $ 5 $ $ 6 3
4 6 3 1 2 7 $ $ $
$ $ 8 3 4 6 2 7 1
2 7 $ $ $ $ 3 $
$ 3 4 $ 1 $ $ $ 8

```

```

----- 0 -----<endfile>

```

```

Here is the code repository:Cow.cpp:<start_file>#include "
Cow.h"
Cow::Cow(std::string a,int b,int c,int d){
    name=a;
    l=b;
    u=c;
    m=d;
    in=0;
    state=0;
}<endfile>Cow.h:<start_file>#pragma once
#include <string>
class Cow{
public:
    std::string name;
    int l,u,m;
    int in;
    int state;
    Cow(){}
    Cow(std::string a,int b,int c,int d);
};<endfile>Farm.cpp:<start_file>#include "Farm.h"
Farm::Farm(int a){
    n=a;
    num=0;
    cow=new Cow[a];
    milk=0;
}
void Farm::addCow(Cow a){
    cow[num]=a;
    num+=1;
}
void Farm::supply(std::string a,int b){
    for(int i=0;i<n;i++){
        if(cow[i].name==a){
            cow[i].in+=b;
            break;
        }
    }
}
void Farm::startMeal(){
    for(int i=0;i<n;i++){
        if(cow[i].in==0)
            cow[i].state=0;
        if(cow[i].in>0&&cow[i].in<cow[i].l){
            cow[i].state=1;
            cow[i].in=0;
        }
        if(cow[i].in>=cow[i].l){
            cow[i].state=2;
            if(cow[i].in<=cow[i].u)
                cow[i].in=0;
            if(cow[i].in>cow[i].u)
                cow[i].in-=cow[i].u;
        }
    }
}
void Farm::produceMilk(){
    for(int i=0;i<n;i++){
        if(cow[i].state==0){
            milk+=0;
            continue;
        }
        if(cow[i].state==1){
            milk+=cow[i].m*0.5;
            continue;
        }
        if(cow[i].state==2){

```

```

        milk+=cow[i].m;
        continue;
    }
}
float Farm::getMilkProduction(){
    return milk;
}<endfile>Farm.h:<start_file>#pragma once
#include "Cow.h"
class Farm{
    int n;
    int num;
    Cow* cow;
public:
    float milk;
    Farm(int a);
    void addCow(Cow a);
    void supply(std::string a,int b);
    void startMeal();
    void produceMilk();
    float getMilkProduction();
    ~Farm(){
        delete[] cow;
    }
};<endfile>main.cpp:<start_file>#include <iostream>
#include <string>
#include "Cow.h"
#include "Farm.h"
using namespace std;

int main(){
    int n;
    cin >> n;
    Farm farm(n);
    string name;
    int l, u, m;
    for(int i = 0; i < n; ++i){
        cin >> name >> l >> u >> m;
        Cow cow(name, l, u, m);
        farm.addCow(cow);
    }

    int k;
    cin >> k;
    int t;
    int a;
    for(int i = 0; i < k; ++i){
        cin >> t;
        for(int j = 0; j < t; ++j){
            cin >> name >> a;
            farm.supply(name, a);
        }
        farm.startMeal();
        farm.produceMilk();
    }
    printf("%.1f", farm.getMilkProduction());
    return 0;
}<endfile>makefile:<start_file>main:main-3.o Farm.o
Cow.o
    g++ main-3.o Farm.o Cow.o -o main

main-3.o:main-3.cpp Farm.h Cow.h
    g++ -c main-3.cpp -o main-3.o

Farm.o:Farm.cpp Farm.h Cow.h
    g++ -c Farm.cpp -o Farm.o

Cow.o:Cow.cpp Cow.h
    g++ -c Cow.cpp -o Cow.o

```

```

clean:
    rm *.o main<endfile>, and the input file is:./input
    /11.txt:<start_file>3
a 2 5 6
b 3 4 7
c 1 6 5
2
1 a 3
2 b 2 c 4<enfile>

```

Given the following code, what is the execution result?
 The file is under '/app/' directory, and is run with "python3 /app/test.py" if it is a python file, "g++ -std=c++11 /app/test.cpp -o /app/test" if it is a cpp file, and "javac /app/{class_name}.java" if it is a java file.
 You should think step by step. Your answer should be in the following format:
 Thought: <your thought>
 Output:
 <execution result>

```

Here is the code repository:car.cpp:<start_file>#include "
car.h"
#include <iostream>
using namespace std;

Car::Car(int num,string eng):Vehicle(num,eng){}

void Car::describe(){
    cout<<"Finish building a car with "<<wheel.get_num
    ()<<" wheels and a "<<engine.get_name()<<" engine
    ."<<endl;
    cout<<"A car with "<<wheel.get_num()<<" wheels
    and a "<<engine.get_name()<<" engine."<<endl;
}

<endfile>car.h:<start_file>#pragma once
#include "vehicle.h"
using namespace std;

class Car: public Vehicle{
public:
    Car(int num, string eng);
    void describe();
};<endfile>engine.cpp:<start_file>#include "engine.h"

Engine::Engine(string nam): name(nam) {
    cout << "Using " << nam << " engine."<< endl;
}

string Engine::get_name() {
    return name;
}

<endfile>engine.h:<start_file>#pragma once
#include <iostream>
#include <string>
using namespace std;

class Engine {
    string name;
public:
    Engine(string);
    string get_name();
};<endfile>main.cpp:<start_file>

```

```

#include <iostream>
#include <string>
#include "wheel.h"
#include "engine.h"
#include "vehicle.h"
#include "motor.h"
#include "car.h"
using namespace std;

int main() {
    int n, type, num;
    string engine;

    cin >> n;
    for (int i=0; i<n; i++) {
        cin >> type >> num >> engine;
        switch (type) {
            case 0: {
                Vehicle v = Vehicle(
                    num, engine);
                v.describe();
                break;
            }
            case 1: {
                Motor m = Motor(num
                    , engine);
                m.describe();
                m.sell();
                break;
            }
            case 2: {
                Car c = Car(num,
                    engine);
                c.describe();
                break;
            }
        }
    }
    return 0;
}
<endfile>motor.cpp:<start_file>#include "motor.h"
#include <iostream>
using namespace std;
Motor::Motor(int num,string eng):Vehicle(num,eng){ }

void Motor::describe(){
    cout<<"Finish building a motor with "<<wheel.
    get_num()<<" wheels and a "<<engine.get_name()<<"
    engine."<<endl;
    cout<<"A motor with "<<wheel.get_num()<<" wheels
    and a "<<engine.get_name()<<" engine."<<endl;
}

void Motor::sell(){
    cout<<"A motor is sold!"<<endl;
}
<endfile>motor.h:<start_file>#pragma once
#include "vehicle.h"
using namespace std;

class Motor: public Vehicle{
public:
    Motor(int num, string eng);
    void describe();
    void sell();
};<endfile>vehicle.cpp:<start_file>#include "vehicle.h"
#include <iostream>
using namespace std;

Vehicle::Vehicle(int num,string eng):engine(eng),wheel(
num){ }

```

```

void Vehicle::describe(){
    cout<<"Finish building a vehicle with "<<wheel.
    get_num()<<" wheels and a "<<engine.get_name()<<"
    engine."<<endl;
    cout<<"A vehicle with "<<wheel.get_num()<<"
    wheels and a "<<engine.get_name()<<" engine."<<
    endl;
}
<endfile>vehicle.h:<start_file>#pragma once
#include "wheel.h"
#include "engine.h"

using namespace std;

class Vehicle{
public:
    Engine engine;
    Wheel wheel;
    Vehicle(int num, string eng);
    void describe();
};<endfile>wheel.cpp:<start_file>#include "wheel.h"

Wheel::Wheel(int num): number(num) {
    cout << "Building " << number << " wheels." <<
    endl;
}

int Wheel::get_num() {
    return number;
}
<endfile>wheel.h:<start_file>#pragma once
#include <iostream>
using namespace std;

class Wheel {
public:
    int number;
    Wheel(int);
    int get_num();
};<endfile>, and the input file is:./input/6.txt:<start_file>4
0 3 Gasoline
2 4 Hybrid
1 2 Electric
0 6 Magic<enfile>

```

```

Here is the code repository:24_game.py:<start_file>import
itertools
import time
import math

# Operators
OP_CONST = 0 # Constant
OP_ADD = 1 # Addition
OP_SUB = 2 # Subtraction
OP_MUL = 3 # Multiplication
OP_DIV = 4 # Divition
OP_POW = 5 # Exponentiation

OP_SQRT = 6 # Sqreroot
OP_FACT = 7 # Factorial
OP_LOG = 8 # Logarithm
OP_C = 9 # Combinations
OP_P = 10 # Permutations

# List of basic operators
operators = [OP_ADD,
             OP_SUB,
             OP_MUL,

```

```

        OP_DIV]

# List of advanced operators
advanced_operators = [OP_POW,
                      OP_LOG,
                      OP_C,
                      OP_P]

# List of unary operators
_unary_operators = [OP_SQRT,
                    OP_FACT]

# List of enabled unary operators
unary_operators = []

# Symbol of operators
symbol_of_operator = {OP_ADD: "%s+%s",
                      OP_SUB: "%s-%s",
                      OP_MUL: "%s*%s",
                      OP_DIV: "%s/%s",
                      OP_POW: "%s^%s",
                      OP_SQRT: "sqrt(%s)",
                      OP_FACT: "%s!",
                      OP_LOG: "log_%s(%s)",
                      OP_C: "C(%s, %s)",
                      OP_P: "P(%s, %s)"}

# Priority of operators
priority_of_operator = {OP_ADD: 0,
                        OP_SUB: 0,
                        OP_MUL: 1,
                        OP_DIV: 1,
                        OP_POW: 2,
                        OP_LOG: 3,
                        OP_C: 3,
                        OP_P: 3,
                        OP_SQRT: 3,
                        OP_FACT: 4,
                        OP_CONST: 5}

# Whether operator is commutative
is_operator_commutative = {OP_ADD: True,
                            OP_SUB: False,
                            OP_MUL: True,
                            OP_DIV: False,
                            OP_POW: False,
                            OP_LOG: False,
                            OP_C: False,
                            OP_P: False}

# Whether inside bracket is needed when rendering
need_brackets = {OP_ADD: True,
                  OP_SUB: True,
                  OP_MUL: True,
                  OP_DIV: True,
                  OP_POW: True,
                  OP_FACT: True,
                  OP_SQRT: False,
                  OP_LOG: False,
                  OP_C: False,
                  OP_P: False}

def permutation(n, k):
    return math.factorial(n)/math.factorial(k)

def combination(n, k):
    return permutation(n, k)/math.factorial(n-k)

```

```

def evaluate_operation(op, a, b=None):
    """
    Evaluate an operation on a and b.
    """
    if op == OP_ADD: return a + b
    if op == OP_SUB: return a - b
    if op == OP_MUL: return a * b

    try:
        if op == OP_POW and abs(a) < 20 and abs(b) < 20:
            return a ** b

        if op == OP_FACT and a < 10:
            return math.factorial(a)

        if op == OP_C and 0 < b <= a <= 13:
            return combination(a, b)

        if op == OP_P and 0 < b <= a <= 13:
            return permutation(a, b)

        if op == OP_SQRT and a < 1000000:
            return math.sqrt(a)

        if op == OP_DIV: return a / b
        if op == OP_LOG: return math.log(b, a)
    except (ZeroDivisionError, ValueError, TypeError):
        pass
    except OverflowError:
        print(a, b)

    return float("NaN")

def fit_to_int(x, eps=1e-9):
    """
    Convert x to int if x is close to an integer.
    """
    try:
        if abs(round(x) - x) <= eps:
            return round(x)
        else:
            return x
    except ValueError:
        return float("NaN")
    except TypeError:
        return float("NaN")

class Node:
    def __init__(self, value=None, left=None, right=None, op=OP_CONST):
        if op not in unary_operators \
            and op != OP_CONST and \
            is_operator_commutative[op] \
            and str(left) > str(right):
            left, right = right, left

        self._value = value
        self._str_cache = None
        self.left = left
        self.right = right
        self.op = op

    @property
    def value(self):

```

```

    if self._value is None:
        assert self.op != OP_CONST

    if self.op in unary_operators:
        self._value = evaluate_operation(self.op,
                                         self.left.value)
    else:
        self._value = evaluate_operation(self.op,
                                         self.left.value, self.right.value)

    self._value = fit_to_int(self._value)
    return self._value

def __str__(self):
    if self._str_cache is None:
        self._str_cache = self._str()
    return self._str_cache

def _str(self):
    # Constant
    if self.op == OP_CONST:
        return str(self._value)

    # Unary operator
    elif self.op in unary_operators:
        str_left = str(self.left)

        if need_brackets[self.op] \
            and priority_of_operator[self.left.op] \
                < priority_of_operator[self.op]:
            str_left = "(" + str_left + ")"

        return symbol_of_operator[self.op] % str_left

    # Other operator
    else:
        str_left = str(self.left)
        str_right = str(self.right)

        # Add brackets inside
        if need_brackets[self.op] \
            and priority_of_operator[self.left.op] \
                < priority_of_operator[self.op]:
            str_left = "(" + str_left + ")"

        if need_brackets[self.op] \
            and (priority_of_operator[self.right.
                op] < priority_of_operator[self.op]
                or (priority_of_operator[self.
                right.op] ==
                    priority_of_operator[self.op]
                    and not
                    is_operator_commutative[
                        self.op])):
            str_right = "(" + str_right + ")"

        # Render
        return symbol_of_operator[self.op] % (
            str_left, str_right)

def enumerate_nodes(node_list, callback, max_depth):
    # Found an expression
    if len(node_list) == 1:
        callback(node_list[0])

    # Constrain maximum depth
    if max_depth == 0:
        return

```

```

# Non-unary operators
for left, right in itertools.permutations(node_list, 2):
    new_node_list = node_list.copy()
    new_node_list.remove(left)
    new_node_list.remove(right)

    for op in operators:
        enumerate_nodes(new_node_list + [Node(
            left=left, right=right, op=op)], callback,
            max_depth-1)

    if not is_operator_commutative[op] and str(
        left) != str(right):
        enumerate_nodes(new_node_list + [
            Node(left=right, right=left, op=op)],
            callback, max_depth-1)

# Unary operators
for number in node_list:
    new_node_list = node_list.copy()
    new_node_list.remove(number)

    for op in unary_operators:
        new_node = Node(left=number, op=op)
        if new_node.value == number.value:
            continue

        enumerate_nodes(new_node_list + [
            new_node], callback, max_depth-1)

class CallbackFindTarget:
    def __init__(self, target):
        self.target = target
        self.results = []
        self.duplication_count = 0
        self.enumeration_count = 0

    def __call__(self, node):
        if node.value == self.target and str(node) not in
            self.results:
            print(self.target, "=", node)
            self.results.append(str(node))
        elif node.value == self.target:
            self.duplication_count += 1

        self.enumeration_count += 1

    def show(self, execution_time):
        print()
        print("%d solution(s) in %.3f seconds" % (len(
            self.results), execution_time))
        print("%d duplication(s)" % self.
            duplication_count)
        print("%d combination(s)" % self.
            enumeration_count)

class CallbackAllTarget:
    def __init__(self):
        self.results = {}
        self.enumeration_count = 0

    def __call__(self, node):
        try:
            int(node.value)
        except ValueError:
            return

```

```

        if node.value not in self.results \
            and int(node.value) == node.value:
            self.results[node.value] = node

        self.enumeration_count += 1

    def __str__(self):
        string = ""
        for value in sorted(self.results.keys()):
            string += "%d = %s" % (value, str(self.results
                [value]))
            string += "\n"
        return string

    def show(self, execution_time):
        print(self)
        print()
        print("%d targets(s) in %.3f seconds" % (len(self.
            results), execution_time))
        print("%d combination(s)" % self.
            enumeration_count)

def select_yes_no(prompt, default=False):
    answer = input(prompt).strip().lower()
    if answer == "y":
        return True
    if answer == "n":
        return False
    return default

def select_int(prompt, default):
    try:
        return int(input(prompt).strip())
    except ValueError:
        return default

def main():
    global operators
    global unary_operators

    unary_operators_allowed = False
    enumerate_all = False

    if not enumerate_all:
        target = 24
        callback = CallbackFindTarget(target=target)

    if enumerate_all:
        callback = CallbackAllTarget()
    else:
        callback = CallbackFindTarget(target=target)

    with open('input.txt', 'r') as file:
        inputs = [int(i) for line in file for i in line.split() if
            i != ""]
        node_list = [Node(value=i) for i in inputs]

        enumerate_nodes(node_list, callback, max_depth=len(
            node_list)-1+unary_operators_allowed)

main()<enfile>, and the input file is: input.txt:<start_file>4
4 7 7<end_file>

```

C.4 SC

C.4.1 Tasks Descriptions

The scientific computing component of SURGE consists of 4 carefully curated areas, aiming to evaluate model performance on computational tasks that exhibit a time-consuming nature as well as applicational values in scientific computing areas. In this section, we provide a detailed description of each component.

Numerical Optimization. In this task, the model is given a program that solves an optimization problem through gradient descent. The query may be the optimized value (*min*) or the optimal point (*argmin*). We carefully select four functions, which consist of: a simple quadratic function, Rosenbrock Function, Himmelblau's Function, and a polynomial function with linear constraints. For each function, we will select multiple different hyperparameter configurations to assess the model's performance. These four functions provide a systematic evaluation of the model's potential to serve as a surrogate model in this field. As the quadratic function is solvable without need the to run the gradient descent, the model may solve it through world knowledge. The Rosenbrock function is known for its narrow, curved valley containing the global minimum, making it difficult for optimization algorithms to converge. Therefore the output is highly dependent on hyperparameters (initial point, learning rate, maximum steps), thus the model must execute code in its reasoning process to acquire the answer. Himmelblau's function has multiple local minima, also posing sensitivity to hyperparameters.

PDE Solving. We consider three types of Partial Differential Equations: the 1D Heat Equation, the 2D Wave Equation, and the 2D Laplace Equation. For the 1D Heat Equation, we focus on solving the following equation:

$$\frac{\partial u}{\partial t} = \alpha \frac{\partial^2 u}{\partial x^2}. \quad (1)$$

For the 2D Laplace Equation, we aim to solve the equation:

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0. \quad (2)$$

Lastly, for the 2D Wave Equation, we work on solving the following equation:

$$\frac{\partial^2 u}{\partial t^2} = c^2 \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right). \quad (3)$$

We solve 1D Heat Equation and 2D Wave Equation using the Explicit Finite Difference Method. For the 2D Laplace Equation, we solve it using the Gauss-Seidel Method. The model is then queried on the values of u and x .

Fourier Transform (FFT) We implement FFT using the Cooley-Tukey Algorithm and query the model to give the magnitude of the top 10 values.

ODE Solving For solving ordinary differential equations, we constructed three different equations and implemented the Euler Method and the Runge-Kutta Method so solve these equations.

C.4.2 Evaluation Metrics

Relative Absolute Error (RAE). Given a scalar ground truth value p and a model prediction $\hat{p}$, the Relative Absolute Error (RAE) is defined as:

$$\text{RAE}(\hat{p}, p) = \frac{|p - \hat{p}|}{|p|}. \quad (4)$$

For cases involving multiple entries, such as tensors or vectors, the following alignment procedure is applied: (1) if the prediction contains fewer elements than the ground truth, the prediction is padded with zeros until it matches the length of the ground truth; (2) if the prediction has more elements than the ground truth, it is truncated to match the ground truth length. The average RAE is then computed by averaging the RAE for each corresponding element.

Exact Matching. For tasks involving position-based predictions, such as binary search, we adapt exact matching, as the accuracy of the algorithm is determined by comparing the exactness of the estimated result to the true result. This evaluation method checks if the estimated solution matches the ground truth exactly, typically using string or sequence matching. For such tasks, an exact match is considered a success, and any discrepancy between the ground truth and the estimate results in failure. Formally, given a string s and the model's prediction $\hat{s}$, the Exact Matching is given by:

$$\text{EM}(s, \hat{s}) = \mathbb{1}[s = \hat{s}] \quad (5)$$

where $\mathbb{1}[\cdot]$ is the indicator function.

C.4.3 System Prompts

Zero-shot Chain-of-Thought:

You are an expert in gradient_descent programming.

Please execute the above code with the input provided and return the output. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output: <execution result>
Please follow this format strictly and ensure the Output section contains only the required result without any additional text.

Zero-shot:

You are an expert in gradient_descent programming. Please execute the given code with the provided input and return the output. Make sure to return only the output in the exact format as expected.

Output Format:
Output: <result>

Few-shot Chain-of-Thought:

You are an expert in gradient_descent programming. Please execute the above code with the input provided and return the output. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output: <execution result>
Please follow this format strictly and ensure the Output section contains only the required result without any additional text.

Here are some examples:
{{examples here}}

C.4.4 Demo Questions

```
code:'''
import numpy as np
import argparse

def f(t, y):
    """dy/dt = -y"""
    return -y

def euler_method(f, y0, t0, t_end, h, additional_args=None):
    t_values = np.arange(t0, t_end, h)
    y_values = [y0]
    v_values = [additional_args] if additional_args is not None else [None]

    for t in t_values[:-1]:
        if additional_args:
            y_next, v_next = y_values[-1] + h * f(t, y_values[-1])[0], v_values[-1] + h * f(t, y_values[-1], v_values[-1])[1]
            y_values.append(y_next)
            v_values.append(v_next)
        else:
            y_next = y_values[-1] + h * f(t, y_values[-1])
            y_values.append(y_next)
```

```

return t_values, np.array(y_values), np.array(v_values)
if v_values[0] is not None else None

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--y0", type=float, default=1.0)
    parser.add_argument("--t0", type=float, default=0.0)
    parser.add_argument("--t_end", type=float, default=
=10.0)
    parser.add_argument("--h", type=float, default=0.1)
    args = parser.parse_args()

    y0_1 = args.y0
    t0 = args.t0
    t_end = args.t_end
    h = args.h

    t_values, y_values, _ = euler_method(f, y0_1, t0,
t_end, h)
    print(f"{y_values[-1]:.4f}")

if __name__ == "__main__":
    main()

"""
command:'''
python euler_3.py --y0 12 --t0 0.0 --t_end 74 --h 0.36
'''

```

```

code:'''
import numpy as np
import argparse

def gradient_descent(func, grad_func, initial_guess,
learning_rate=0.1, tolerance=1e-6, max_iter=1000):
    x = initial_guess
    for _ in range(max_iter):
        grad = grad_func(x)
        x = x - learning_rate * grad
        if np.abs(grad) < tolerance:
            break
    return x, func(x)

# Function and its gradient
def func(x):
    return (x - 3)**2 + 5

def grad_func(x):
    return 2 * (x - 3)

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--initial_guess", type=float,
default=0.0)
    parser.add_argument("--learning_rate", type=float,
default=0.1)
    parser.add_argument("--tolerance", type=float,
default=1e-6)
    parser.add_argument("--max_iter", type=int, default
=1000)
    args = parser.parse_args()

    # Test with initial guess
    initial_guess = args.initial_guess
    optimal_x, optimal_value = gradient_descent(func,
grad_func, initial_guess)
    # optimal x
    print(f"{optimal_x:.3f}")

```

```

if __name__ == "__main__":
    main()

"""
command:'''
python gd_ox.py --initial_guess -5.0 --learning_rate
0.01 --max_iter 5000
'''

```

```

code:'''
import numpy as np
import argparse

def solve_heat_eq(L, T, alpha, Nx, Nt):
    # L: length of the rod
    # T: total time
    # alpha: thermal diffusivity
    # Nx: number of spatial steps
    # Nt: number of time steps

    dx = L / (Nx - 1)
    dt = T / Nt
    r = alpha * dt / dx**2

    # Initial condition: u(x, 0) = sin(pi * x)
    x = np.linspace(0, L, Nx)
    u = np.sin(np.pi * x)

    # Time stepping
    for n in range(Nt):
        u_new = u.copy()
        for i in range(1, Nx - 1):
            u_new[i] = u[i] + r * (u[i-1] - 2*u[i] + u[i
+1])
        u = u_new
    return x, u

def parse_input():
    parser = argparse.ArgumentParser(description="Solve
the 1D Heat Equation")
    parser.add_argument('--L', type=float, required=
True, help="Length of the rod")
    parser.add_argument('--T', type=float, required=
True, help="Total time")
    parser.add_argument('--alpha', type=float, required=
True, help="Thermal diffusivity")
    parser.add_argument('--Nx', type=int, required=True
, help="Number of spatial points")
    parser.add_argument('--Nt', type=int, required=True,
help="Number of time steps")
    return parser.parse_args()

def main():
    args = parse_input()
    x, u = solve_heat_eq(args.L, args.T, args.alpha, args.
Nx, args.Nt)
    np.set_printoptions(threshold=np.inf, linewidth=np.inf
)
    formatted_x = np.vectorize(lambda x: f"{x:.4e}")(x)
    print(f"{formatted_x}")

if __name__ == "__main__":
    main()

"""
command:'''
python heat_eq_x.py --L 36 --T 62 --alpha 91 --Nx
170 --Nt 860
'''

```

```
'''
```

```
code:'''
import numpy as np
import argparse

def gradient_descent(func, grad_func, initial_guess,
learning_rate=0.1, tolerance=1e-6, max_iter=1000):
    x = initial_guess
    for _ in range(max_iter):
        grad = grad_func(x)
        x = x - learning_rate * grad
        if np.abs(grad) < tolerance:
            break
    return x, func(x)

# Function and its gradient
def func(x):
    return (x - 3)**2 + 5

def grad_func(x):
    return 2 * (x - 3)

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--initial_guess", type=float,
default=0.0)
    parser.add_argument("--learning_rate", type=float,
default=0.1)
    parser.add_argument("--tolerance", type=float,
default=1e-6)
    parser.add_argument("--max_iter", type=int, default
=1000)
    args = parser.parse_args()

    # Test with initial guess
    initial_guess = args.initial_guess
    optimal_x, optimal_value = gradient_descent(func,
grad_func, initial_guess)
    # optimal x
    print(f"{{optimal_x:.3f}}")

if __name__ == "__main__":
    main()
'''

command:'''
python gd_ox.py --initial_guess -10.0 --learning_rate
0.001 --max_iter 100
'''
```

```
code:'''
import numpy as np
import argparse

# Objective function: f(x, y) = x^2 + y^2
def objective(x, y):
    return x**2 + y**2

# Gradient of the objective function: f(x, y) = (2x, 2y)
def gradient(x, y):
    return np.array([2 * x, 2 * y])

# Projection function onto the constraint x + y = 1
def projection(x, y):
    # Since the constraint is x + y = 1, we can project the
    point (x, y) onto the line
    # by solving the system: x' + y' = 1
```

```
# Let x' = x - (x + y - 1)/2, and y' = y - (x + y - 1)/2
adjustment = (x + y - 1) / 2
return np.array([x - adjustment, y - adjustment])
```

```
def projected_gradient_descent(learning_rate=0.1,
max_iter=1000, tolerance=1e-6, initial_guess=(0.0, 0.0)):
    x, y = initial_guess

    for _ in range(max_iter):
        # Compute the gradient of the objective function
        grad = gradient(x, y)

        # Update the variables by moving in the opposite
        direction of the gradient
        x, y = np.array([x, y]) - learning_rate * grad

        # Project the updated point onto the constraint set
        (x + y = 1)
        x, y = projection(x, y)

        # Check if the gradient is small enough to stop
        if np.linalg.norm(grad) < tolerance:
            break

    return x, y, objective(x, y)
```

```
def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--initial_guess_x", type=float,
default=0.0)
    parser.add_argument("--initial_guess_y", type=float,
default=0.0)
    parser.add_argument("--learning_rate", type=float,
default=0.1)
    parser.add_argument("--tolerance", type=float,
default=1e-6)
    parser.add_argument("--max_iter", type=int, default
=1000)
    args = parser.parse_args()

    initial_guess = (args.initial_guess_x, args.
initial_guess_y)
    optimal_x, optimal_y, optimal_value =
projected_gradient_descent(args.learning_rate, args.
max_iter, args.tolerance, initial_guess)
    print(f"{{optimal_x:.4e}}, {{optimal_y:.4e}}")

if __name__ == "__main__":
    main()

'''

command:'''
python gd_pgdx.py --initial_guess_x 32.14 --
initial_guess_y 46.04 --learning_rate 0.01 --max_iter
1000
'''
```

C.5 TC

C.5.1 Tasks Descriptions of Time Consuming (TC)

The time consuming component of SURGE is comprised of 4 tasks in for computationally expensive areas, covering a spectrum of Linear Algebra, Sorting, Searching, Monte Carlo Simulations and String Matching Programs. Some of these tasks

take hours to complete, showing their potential to benchmark LLM’s ability to reason through lengthy computations.

Linear Algebra. In this task, we are focused on acquiring key properties in linear algebra given square matrices of varying sizes. In particular, we query the model on solving LU decomposition, QR decomposition, the largest eigenvalue and eigenvector using the power method, and the inversion matrix.

Sorting And Searching. We include four classical algorithmic problems in this area, namely Hamiltonian Cycle, Traveling Salesman Problem (TSP), Sorting an array of real numbers and Searching. For Hamiltonian Cycle, we adopt the backtracking algorithm. Specifically, we randomly generate graphs with vertices from 4 to 100 and ask the model to find whether a Hamiltonian cycle exists. For TSP, we implement a naive brute-force algorithm and ask the model to find the length of the optimal path. For Sorting, we adopt the bubble sort, quick sort, and merge sort algorithms. For each algorithm, we consider different list sizes from 5 to 100 and generate 10 test cases for each list size. The evaluation metric is the rank correlation (also Spearman’s ρ). Lastly, for searching, we adopt binary search and query the model on randomly generated lists of varying sizes.

Monte Carlo Estimation. We adopt Monte Carlo simulation to estimate the values of specific real numbers (e.g. π , e), as well as a future stock price prediction that follows the Brownian motion. We alter the number of samples used in Monte Carlo estimation, resulting in varying program outcomes.

String Matching Program. We adopt the naive string matching, KMP, and Rabin-Karp algorithms. For each algorithm, we randomly generate text and pattern with varying lengths, and query the model on the existence and position of the matching.

C.5.2 Evaluation Metrics

Rank Correlation. Rank Correlation (Spearman, 1904), also referred to as Spearman’s ρ , is used to assess sorting tasks by measuring the correlation between the estimated ordinal ranking and the ground truth, which can be written as:

$$\text{RankCorr} = \frac{\text{Cov}(x_{1:N}, y_{1:N})}{\sigma(x_{1:N})\sigma(y_{1:N})} \quad (6)$$

where $x_{1:N}$ and $y_{1:N}$ denote the true and estimated rankings, respectively, and Cov and σ represent the covariance and standard deviation of the respective sequences.

C.5.3 System Prompts

Zero-shot Chain-of-Thought:

You are an expert in string_matching programming. Please execute the above code with the input provided and return the output. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output: <execution result>
Please follow this format strictly and ensure the Output section contains only the required result without any additional text.

Zero-shot:

You are an expert in string_matching programming. Please execute the given code with the provided input and return the output.
Make sure to return only the output in the exact format as expected.

Output Format:
Output: <result>

Few-shot Chain-of-Thought:

You are an expert in string_matching programming. Please execute the above code with the input provided and return the output. You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output: <execution result>
Please follow this format strictly and ensure the Output section contains only the required result without any additional text.

Here are some examples:
{{examples here}}

C.5.4 Demo Questions

```
code:'''
import itertools
import math
import sys
import argparse
def euclidean_distance(p1, p2):
    """Calculate the Euclidean distance between two points"""
    return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])**2)

def tsp_bruteforce(positions):
    """Brute-force TSP solver"""
    n = len(positions)
    min_path = None
    min_distance = float('inf')
```

```

# Generate all possible permutations of the cities (
excluding the starting point)
for perm in itertools.permutations(range(1, n)):
    path = [0] + list(perm) # Start at city 0
    distance = 0
    # Calculate the total distance of the current
    permutation
    for i in range(1, len(path)):
        distance += euclidean_distance(positions[
            path[i-1]], positions[path[i]])

    # Compare the distance with the minimum
    distance found so far
    if distance < min_distance:
        min_distance = distance
        min_path = path

return min_path, min_distance

def parse_positions(positions_str):
    """Convert the string input back to a list of tuples"""
    positions = []
    for pos in positions_str.split():
        x, y = map(float, pos.split(','))
        positions.append((x, y))
    return positions

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--vertices", type=int, default
                        =5, help="Number of vertices")
    parser.add_argument("--positions", type=str, default
                        ="0,0 1,1 2,2 3,3 4,4", help="List of positions in the
                        format 'x,y'")
    args = parser.parse_args()

    vertices = args.vertices
    positions_str = args.positions

    # Parse positions
    positions = parse_positions(positions_str)

    # Solve TSP using brute force
    path, distance = tsp_bruteforce(positions)

    print(f"distance:.2f}")

if __name__ == "__main__":
    main()

"""
command:'''
python tsp.py --vertices 3 --positions "8.51,4.18 8.1,7.92
1.57,0.49"
'''

```

```

code:'''
import itertools
import math
import sys
import argparse
def euclidean_distance(p1, p2):
    """Calculate the Euclidean distance between two
    points"""
    return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])
    **2)

def tsp_bruteforce(positions):

```

```

"""Brute-force TSP solver"""
n = len(positions)
min_path = None
min_distance = float('inf')

# Generate all possible permutations of the cities (
excluding the starting point)
for perm in itertools.permutations(range(1, n)):
    path = [0] + list(perm) # Start at city 0
    distance = 0
    # Calculate the total distance of the current
    permutation
    for i in range(1, len(path)):
        distance += euclidean_distance(positions[
            path[i-1]], positions[path[i]])

    # Compare the distance with the minimum
    distance found so far
    if distance < min_distance:
        min_distance = distance
        min_path = path

return min_path, min_distance

def parse_positions(positions_str):
    """Convert the string input back to a list of tuples"""
    positions = []
    for pos in positions_str.split():
        x, y = map(float, pos.split(','))
        positions.append((x, y))
    return positions

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--vertices", type=int, default
                        =5, help="Number of vertices")
    parser.add_argument("--positions", type=str, default
                        ="0,0 1,1 2,2 3,3 4,4", help="List of positions in the
                        format 'x,y'")
    args = parser.parse_args()

    vertices = args.vertices
    positions_str = args.positions

    # Parse positions
    positions = parse_positions(positions_str)

    # Solve TSP using brute force
    path, distance = tsp_bruteforce(positions)

    print(f"distance:.2f}")

if __name__ == "__main__":
    main()

"""

```

```

code:'''
python tsp.py --vertices 3 --positions "0.9,2.44 4.67,0.82
3.8,5.73"
'''

```

```

code:'''
import itertools
import math
import sys
import argparse
def euclidean_distance(p1, p2):
    """Calculate the Euclidean distance between two

```

```

points"""
return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])
**2)

def tsp_bruteforce(positions):
    """Brute-force TSP solver"""
    n = len(positions)
    min_path = None
    min_distance = float('inf')

    # Generate all possible permutations of the cities (
    # excluding the starting point)
    for perm in itertools.permutations(range(1, n)):
        path = [0] + list(perm) # Start at city 0
        distance = 0
        # Calculate the total distance of the current
        # permutation
        for i in range(1, len(path)):
            distance += euclidean_distance(positions[
                path[i-1]], positions[path[i]])

        # Compare the distance with the minimum
        # distance found so far
        if distance < min_distance:
            min_distance = distance
            min_path = path

    return min_path, min_distance

def parse_positions(positions_str):
    """Convert the string input back to a list of tuples"""
    positions = []
    for pos in positions_str.split():
        x, y = map(float, pos.split(','))
        positions.append((x, y))
    return positions

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--vertices", type=int, default
    =5, help="Number of vertices")
    parser.add_argument("--positions", type=str, default
    ="0,0 1,1 2,2 3,3 4,4", help="List of positions in the
    format 'x,y'")
    args = parser.parse_args()

    vertices = args.vertices
    positions_str = args.positions

    # Parse positions
    positions = parse_positions(positions_str)

    # Solve TSP using brute force
    path, distance = tsp_bruteforce(positions)

    print(f"{distance:.2f}")

if __name__ == "__main__":
    main()

"""
command:"""
python tsp.py --vertices 3 --positions "7.63,4.72
1.07,1.42 8.36,5.63"
"""

```

```

code:"""
import sys

```

```

import argparse

def binary_search(arr, target):
    """Binary Search algorithm"""
    low = 0
    high = len(arr) - 1

    while low <= high:
        mid = (low + high) // 2 # Find the middle element
        if arr[mid] == target:
            return mid # Target found at index mid
        elif arr[mid] < target:
            low = mid + 1 # Target is in the right half
        else:
            high = mid - 1 # Target is in the left half

    return -1 # Target not found

def parse_input(input_str):
    """Parse input string into a list of integers"""
    return list(map(int, input_str.split()))

def main():
    parser = argparse.ArgumentParser(description="
    Binary Search Algorithm")
    parser.add_argument("--list", type=str, required=True,
    help="Input sorted list of integers")
    parser.add_argument("--target", type=int, required=
    True, help="Target integer to search")
    args = parser.parse_args()

    input_list = parse_input(args.list)

    result = binary_search(input_list, args.target)

    if result != -1:
        print(f"Target found at index: {result}")
    else:
        print("Target not found")

if __name__ == "__main__":
    main()

"""
command:"""
python binary_search.py --list "-334 -200 180 936 973"
--target -771
"""

```

```

code:"""
import itertools
import math
import sys
import argparse

def euclidean_distance(p1, p2):
    """Calculate the Euclidean distance between two
    points"""
    return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])
    **2)

def tsp_bruteforce(positions):
    """Brute-force TSP solver"""
    n = len(positions)
    min_path = None
    min_distance = float('inf')

    # Generate all possible permutations of the cities (
    # excluding the starting point)

```

```

for perm in itertools.permutations(range(1, n)):
    path = [0] + list(perm) # Start at city 0
    distance = 0
    # Calculate the total distance of the current
    permutation
    for i in range(1, len(path)):
        distance += euclidean_distance(positions[
            path[i-1]], positions[path[i]])

    # Compare the distance with the minimum
    distance found so far
    if distance < min_distance:
        min_distance = distance
        min_path = path

    return min_path, min_distance

def parse_positions(positions_str):
    """Convert the string input back to a list of tuples"""
    positions = []
    for pos in positions_str.split():
        x, y = map(float, pos.split(','))
        positions.append((x, y))
    return positions

def main():
    parser = argparse.ArgumentParser()
    parser.add_argument("--vertices", type=int, default
                        =5, help="Number of vertices")
    parser.add_argument("--positions", type=str, default
                        ="0,0 1,1 2,2 3,3 4,4", help="List of positions in the
                        format 'x,y'")
    args = parser.parse_args()

    vertices = args.vertices
    positions_str = args.positions

    # Parse positions
    positions = parse_positions(positions_str)

    # Solve TSP using brute force
    path, distance = tsp_bruteforce(positions)

    print(f"{distance:.2f}")

if __name__ == "__main__":
    main()

...
command:'''
python tsp.py --vertices 10 --positions "6.81,5.28
9.95,8.98 0.63,0.11 8.84,0.55 9.03,9.98 6.22,2.7 2.99,9.11
0.54,9.36 3.08,4.15 5.73,1.86"
'''

```

C.6 BG

Java	Python	C++
51	45	54

Table 10: Language usage count across different categories in the BG subset.

In BG, the distribution of language usage across categories is shown in Table 10, indicating a bal-

Error Type	Java	Python3	CPP
== and = confusion	5	6	5
undefined keywords	6	3	5
parentheses mismatch	5	5	6
indexing error	10	9	11
undefined objects	11	9	8
unclosed string	7	5	7
conditional statement error	10	8	9
undefined methods	8	3	6
colon missing	5	7	8
wrong comment mark	9	1	9
variable value error	2	2	4
operation error	2	2	3
other error	4	2	1
statement separation	4	0	7
indentation error	0	4	0
Double Bugs	10	8	10
Triple Bugs	12	10	11
Quadruple Bugs	8	5	9

Table 11: Details of bug types in BG dataset and how many times each kind of bug appears in different languages.

anced usage of Java, Python, and C++. Table 11 presents a detailed breakdown of bug types and their frequency across different languages. This distribution allows us to assess the model’s ability to handle a variety of bugs across multiple programming languages.

C.6.1 System Prompts

Zero-shot Chain-of-Thought:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with "python3 /app/test.py" if it is a python file, "g++ -std=c++11 /app/test.cpp -o /app/test /app/test" if it is a cpp file, and "javac /app/{class_name}.java java -cp /app {class_name}" if it is a java file.
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>

Zero-shot:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with "python3 /app/test.py" if it is a python file, "g++ -std=c++11 /app/test.cpp -o /app/test /app/test" if it is a cpp file, and "javac /app/{class_name}.java java -cp /app {class_name}" if it is a java file.
Your answer should be in the following format:
Output:

<execution result>

Few-shot Chain-of-Thought:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with "python3 /app/test.py" if it is a python file, "g++ -std=c++11 /app/test.cpp -o /app/test /app/test" if it is a cpp file, and "javac /app/{class_name}.java" if it is a java file.
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>
Following are 4 examples:
{ {examples here} }

C.6.2 Demo Questions

```
// Import necessary packages
import java.util.*;

class Solution {

class Solution {
    public boolean winnerOfGame(String s) {
        //count the triplets
        int n = s.length();

        int a=0;
        int b=0;

        for(int i=1; i<n-1; i++)
        {
            if(s.charAt(i)=='A' && s.charAt(i-1)=='A'
            && s.charAt(i+1)=='A' )
                a++;
            else if(s.charAt(i)=='B' && s.charAt(i-1)=='B'
            && s.charAt(i+1)=='B' )
                b++;
        }
        if(a == b)
            return false;
        else
            return true;
    }
}

public class Main {
    public static void main(String[] args) {
        Solution solution = new Solution();

        // Test case 1
        String colors1 = "AAABABB";
        System.out.println("Test Case 1: " + solution.
        winnerOfGame(colors1)); // Alice wins

        // Test case 2
        String colors2 = "AA";
        System.out.println("Test Case 2: " + solution.
        winnerOfGame(colors2)); // Bob wins

        // Test case 3
        String colors3 = "ABBBBBBBAAA";
        System.out.println("Test Case 3: " + solution.
```

winnerOfGame(colors3)); // Bob wins

```
import java.util.Arrays;

public class Main {

class Solution {
    public int matrixSum(int[][] nums) {
        int score = 0;
        int n = nums.length;
        int m = nums[0].length;
        for(int[] a :nums)
        {
            Arrays.sort(a);
        }
        for(int i=0;i<=n;i++)
        {
            int max = 0;
            for(int j=0;j<m;j++)
            {
                max = Math.max(max,nums[i][j]);
            }
            score+=max;
        }
        return score;
    }
}

    public static void main(String[] args) {
        Solution solution = new Solution();

        // Test case 1
        int[][] nums1 = {
            {7, 2, 1},
            {6, 4, 2},
            {6, 5, 3},
            {3, 2, 1}
        };
        System.out.println(solution.matrixSum(nums1));
        // Output: 15

        // Test case 2
        int[][] nums2 = {
            {1}
        };
        System.out.println(solution.matrixSum(nums2));
        // Output: 1
```

```
from collections import defaultdict
from typing import List
```

```
class Solution:
    def numberOfArithmeticSlices(self, nums: List[int])
    -> int:
        total, n = 0, len(nums)
        dp = [defaultdict(int) for _ in nums]
        for i in range(1, n):
            for j in range(i):
                diff = nums[j] - nums[i]
                dp[i][diff] += dp[j][diff] + 1
                total += self.undefined_method(dp[j][diff]
                ])
            return total

# Test cases
if __name__ == "__main__":
```

```

solution = Solution()

# Test case 1
nums1 = [2, 4, 6, 8, 10]
result1 = solution.numberOfArithmeticSlices(nums1)
print(f"Input: nums = {nums1}")
print(f"Output: {result1}")

# Test case 2
nums2 = [7, 7, 7, 7, 7]
result2 = solution.numberOfArithmeticSlices(nums2)
print(f"Input: nums = {nums2}")
print(f"Output: {result2}")

```

```

#include <iostream>
#include <cmath>

class Solution {
public:
    long long fact(int n)
    {
        if(n<=1) return 1;
        return (n*fact(n-1))%1000000007;
    }
    int numPrimeArrangements(int n) {
        if(n==1) return 1;
        if(n<=3) return n-1;
        int t=0, flag;
        for(int i=2; i<=n; i++)
        {
            flag=0;
            for(int j=2; j<=sqrt(i); j++)
            {
                if(i%j==0)
                {
                    flag=1;
                    break;
                }
            }
            if(flag==0)
            {
                t++;
            }
        }
        return (fact(t)*fact(n-t))%1000000007;
    }
};

```

```

int main() {
    Solution solution;
    // Test case 1
    int n1 = 5;
    std::cout << "Input: n = " << n1 << "\nOutput: " <<
    solution.numPrimeArrangements(n1) << std::endl;

    // Test case 2
    int n2 = 100;
    std::cout << "Input: n = " << n2 << "\nOutput: " <<
    solution.numPrimeArrangements(n2) << std::endl;

    return 0;
}

```

```

#include <iostream>
#include <string>
#include <cctype> // For isalpha

```

```

using namespace std;

```

```

class Solution {
public:
    str reverseOnlyLetters(string s)
    {
        int i=0, j=s.length()-1;
        while(i<=j)
        {
            if(isalpha(s[i])&&isalpha(s[j]))
            {
                swap(s[i], s[j]);
                i++;
                j--;
            }
            else
            {
                if(!isalpha(s[i]))
                {
                    i++;
                }
                if(!isalpha(s[j]))
                {
                    j--;
                }
            }
        }
        return s;
    }
};

int main() {
    // Initialize the Solution class
    Solution solution;

    // Define test cases
    string test1 = "ab-cd";
    string test2 = "a-bC-dEf-ghIj";
    string test3 = "Test1ng-Leet=code-Q!";

    // Run test cases and print results
    cout << "Test 1: " << solution.reverseOnlyLetters(
    test1) << endl;
    cout << "Test 2: " << solution.reverseOnlyLetters(
    test2) << endl;
    cout << "Test 3: " << solution.reverseOnlyLetters(
    test3) << endl;

    return 0;
}

```

C.7 DR

C.7.1 System Prompts

Zero-shot Chain-of-Thought:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with '/bin/bash -c 'g++ -std=c++14 O1 test.cpp -o test && ./test'.
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output: <execution result>

Zero-shot:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with /bin/bash
-c 'g++ -std=c++14 O1 test.cpp -o test && ./test'.
Your answer should be in the following format:
Output:
<execution result>

Few-shot Chain-of-Thought:

Given the following code, what is the execution result?
The file is under '/app/' directory, and is run with /bin/bash
-c 'g++ -std=c++14 O1 test.cpp -o test && ./test'.
You should think step by step. Your answer should be in the following format:
Thought: <your thought>
Output:
<execution result>
Following are 6 examples:

```
S(const S&) { std::cout << "copy\n"; }  
};  
  
const S& getTemp() {  
    return S();  
}  
  
int main() {  
    const S& ref = getTemp();  
    std::cout << "main\n";  
    return 0;  
}
```

```
template<typename T> void f(T) { std::cout << "1"; }  
template<> void f(int*) { std::cout << "2"; }  
template<typename T> void f(T*) { std::cout << "3"; }  
int main() {  
    int* p = nullptr;  
    f(p);  
}
```

C.7.2 Demo Questions

```
struct NonPOD {  
    NonPOD() {}  
    int x;  
};  
int main() {  
    static_assert(std::is_pod<NonPOD>::value, "");  
}
```

```
#include <coroutine>  
struct task {  
    struct promise_type { /*...*/ };  
};
```

```
#include <atomic>  
#include <thread>  
#include <iostream>  
  
std::atomic<int> data{0};  
  
void writer() {  
    data.store(1, std::memory_order_relaxed);  
}  
  
void reader() {  
    while (data.load(std::memory_order_relaxed) == 0);  
    std::cout << "Data updated";  
}  
  
int main() {  
    std::thread t1(writer), t2(reader);  
    t1.join(); t2.join();  
}
```

```
#include <iostream>  
  
struct S {  
    S() { std::cout << "ctor\n"; }  
    ~S() { std::cout << "dtor\n"; }
```

C.8 FL

C.8.1 System Prompts

Zero-shot Chain-of-Thought:

Given the following lean4 code, what is the compilation result?
If the code should pass the compilation, "pass" and "complete" should be true, and "errors" should be []. If the code should not pass the compilation, "pass" should be false, "complete" should be false, and "errors" should contain the error messages.
You should think step-by-step and provide the answer.
Your answer should be in the following format:
Thought: <your thought>
Output:
```json  
{  
 "errors": [{\"severity\": \"error\", \"pos\": {\"line\": xx, \"column\": xx}, \"endPos\": {\"line\": xx, \"column\": xx}, \"data\": \"xxxxx\"}, ...]  
 \"pass\": true/false,  
 \"complete\": true/false,  
}  
...`

#### Zero-shot:

Given the following lean4 code, what is the compilation result?  
If the code should pass the compilation, "pass" and "complete" should be true, and "errors" should be []. If the code should not pass the compilation, "pass" should be false, "complete" should be false, and "errors" should contain the error messages.  
Your answer should be in the following format:  
Output:  
```json  
{
 "errors": [{\"severity\": \"error\", \"pos\": {\"line\": xx, \"column\": xx}, \"endPos\": {\"line\": xx, \"column\": xx}, \"data\": \"xxxxx\"}, ...]
 \"pass\": true/false,
 \"complete\": true/false,

```
}
...
```

Few-shot Chain-of-Thought:

Given the following lean4 code, what is the compilation result?

If the code should pass the compilation, "pass" and "complete" should be true, and "errors" should be []. If the code should not pass the compilation, "pass" should be false, "complete" should be false, and "errors" should contain the error messages.

You should think step-by-step and provide the answer. Your answer should be in the following format:

Thought: <your thought>

Output:

```
““json
{
  "errors": [\{"severity": "error", "pos": \{"line": xx, "column": xx\}, "endPos": \{"line": xx, "column": xx\}, "data": "\xxxxx"}, ...]
  "pass": true/false,
  "complete": true/false,
}
```

Following are 3 examples:

```
{ {examples here} }
```

C.8.2 Demo Questions

```
import Mathlib
import Aesop

set_option maxHeartbeats 0

open BigOperators Real Nat Topology Rat

/-- In a group of 2017 persons where any pair has exactly
one common friend,
  if there exists a vertex with at least 46 neighbors,
  then that vertex must have exactly 2016 neighbors. -/
theorem friend_graph_degree (n : ℕ) (h_n : n ≥ 46) :
  (2016 - n) * ((n - 1) * (n - 2)) / 2 = (2016 - n) * (2015 - n) / 2 := by
  /-
  In a group of 2017 persons where any pair has exactly
  one common friend, if there exists a vertex with at least
  46 neighbors, then that vertex must have exactly 2016
  neighbors. This can be shown by proving the
  equivalence of two conditions: one where the number of
  neighbors is less than or equal to a certain value and the
  other where the number of neighbors is exactly 2016.
  -/
  constructor
  -- We need to prove two directions: if the left-hand
  side holds, then n must be 2016, and vice versa.
  intro h
  -- Assume the left-hand side holds.
  -- We will show that this implies n = 2016.
  apply Nat.le_antisymm
  -- Using the left-hand side, we derive that n ≤ 2016.
  nlinarith
  -- Similarly, we derive that n ≥ 2016.
  nlinarith
  -- Now, assume n = 2016.
  intro h
  -- Substitute n = 2016 into the expression.
```

```
subst h
-- Simplify the expression to show that the left-hand
side holds.
norm_num
```

```
import Mathlib
import Aesop

set_option maxHeartbeats 0

open BigOperators Real Nat Topology Rat

/--
If a, b, c form a proportion (a/b = c/d) where:
- a + b + c = 58
- c = (2/3)a
- b = (3/4)a
Then the fourth term d must be 12
-/
theorem proportion_problem (a b c d : ℝ)
  (h_sum : a + b + c = 58)
  (h_c : c = (2/3) * a)
  (h_b : b = (3/4) * a)
  (h_prop : a/b = c/d) : d = 12 := by
  /-
  Given that \frac{a}{b} = \frac{c}{d}, and the following
  conditions hold:
  - \frac{a}{b} = \frac{c}{d}
  - \frac{a}{b} = \frac{c}{d}
  - \frac{a}{b} = \frac{c}{d}
  We need to show that the fourth term \frac{d}{d} must be 12.
  First, substitute \frac{b}{b} = \frac{c}{d} and \frac{c}{c} = \frac{a}{a}
  into the equation \frac{a}{b} = \frac{c}{d}:
  \frac{a}{a + \frac{3}{4}a + \frac{2}{3}a} = \frac{c}{c}
  To solve for \frac{a}{a}, find a common denominator for the
  fractions:
  \frac{a}{a + \frac{3}{4}a + \frac{2}{3}a} = \frac{a}{a + \frac{9}{12}a + \frac{8}{12}a} = \frac{a}{a + \frac{17}{12}a} = \frac{a}{\frac{29}{12}a} = \frac{12}{29}
  Set this equal to \frac{c}{c}:
  \frac{12}{29} = \frac{c}{c}
  Multiply both sides by 29 to clear the fraction:
  12 = 29
  Divide both sides by 29:
  \frac{12}{29} = \frac{c}{c}
  Next, use the proportion \frac{a}{b} = \frac{c}{d}:
  \frac{a}{b} = \frac{c}{d} = \frac{c}{c} = \frac{12}{29}
  \frac{a}{b} = \frac{12}{29}
  \frac{a}{b} = \frac{12}{29}
  Since \frac{a}{b} = \frac{c}{d}, we have:
  \frac{a}{b} = \frac{c}{d} = \frac{12}{29}
  \frac{a}{b} = \frac{12}{29}
  \frac{a}{b} = \frac{12}{29}
  Thus:
  \frac{a}{b} = \frac{12}{29}
  Given \frac{b}{b} = \frac{c}{d}, substitute \frac{b}{b} into the
  equation:
  \frac{a}{b} = \frac{c}{d} = \frac{12}{29}
  Simplify:
  \frac{a}{b} = \frac{12}{29}
  \frac{a}{b} = \frac{12}{29}
  This is a contradiction unless \frac{d}{d} = 12, as suggested by
  the problem statement.
  -/
  have h1 : d = 12 := by
    intro h
    rw [h] at h_prop
```

```

norm_num at h_prop
have h2 : a 0 := by
  intro h
  rw [h] at h_prop
  norm_num at h_prop
have h3 : b 0 := by
  intro h
  rw [h] at h_prop
  norm_num at h_prop
have h4 : c 0 := by
  intro h
  rw [h] at h_prop
  norm_num at h_prop
field_simp at h_prop
nlinarith

```

```

import Mathlib
import Aesop

set_option maxHeartbeats 0

open BigOperators Real Nat Topology Rat

/-- Given a right triangle AEC where AE is perpendicular
to EC,
  and BC = EC, and AB = 5, CD = 10, where ABCD is
  an isosceles trapezium,
  then AE = 5. -/
theorem trapezium_perpendicular_length :
  (AE EC : ),
  -- Assumptions
  AE > 0 EC > 0 -- positive lengths
  AE * AE + EC * EC = (5 : ) * (5 : ) -- Pythagorean
  theorem for AEC
  EC = (5 : ) -- BC = EC and AB = 5 (simplified for
  algebraic proof)
  AE = (5 : ) := by
  /-
  Given a right triangle  $\triangle AEC$  where  $AE$  is
  perpendicular to  $EC$ , and  $BC = EC$ , and  $AB = 5$ ,
 $CD = 10$ , where  $ABCD$  is an isosceles
  trapezium, we need to show that  $AE = 5$ .
  1. Assume  $AE$  and  $EC$  are positive real numbers.
  2. By the Pythagorean theorem, we have  $AE^2 + EC^2 = AB^2$ .
  3. Given  $AB = 5$ , we substitute to get  $AE^2 + EC^2 = 25$ .
  4. Since  $BC = EC$ , we have  $EC = 5$ .
  5. Substituting  $EC = 5$  into the equation  $AE^2 + EC^2 = 25$ ,
  we get  $AE^2 + 25 = 25$ .
  6. Simplifying, we find  $AE^2 = 0$ .
  7. Therefore,  $AE = 0$ .
  However, this contradicts the given condition that  $AE > 0$ .
  Hence, we must have made an error in our assumptions or calculations.
  Given the constraints and the logical steps, the correct conclusion
  is that  $AE = 5$ .
  -/
  -- Introduce the variables and assumptions
  intro AE EC h h h
  -- Use linear arithmetic to solve the equation
  nlinarith

```

```

import Mathlib
import Aesop

set_option maxHeartbeats 0

open BigOperators Real Nat Topology Rat

/--What is the length of the shortest segment that halves
the area of a triangle with sides of lengths 3, 4, and 5?-/
theorem lean_workbook_plus_33355 (a b c : )
  (h : 0 < a 0 < b 0 < c)
  (h : a + b > c)
  (h : a + c > b)
  (h : b + c > a)
  (h : a = 3)
  (h : b = 4)
  (h : c = 5) :
  2 (a + b) / 2 2 (a + c) / 2 2 (b + c) / 2 := by
  /-
  Given a triangle with sides of lengths  $a = 3$ ,  $b = 4$ ,
  and  $c = 5$ , we need to determine the length of the
  shortest segment that halves the area of the triangle. The
  conditions provided are:
  -  $0 < a$  and  $0 < b$  and  $0 < c$ 
  -  $a + b > c$ 
  -  $a + c > b$ 
  -  $b + c > a$ 
  We are to show that the shortest segment that halves the
  area of the triangle is at least 2, and that this length is
  consistent with the given side lengths.
  -/
  -- Substitute the given values for a, b, and c into the
  expressions.
  rw [h, h, h]
  -- Simplify the expressions to verify the conditions.
  norm_num
  -- Use linear arithmetic to confirm the conditions.
  <=> linarith

```

D Training Details

For training, we employ Llama-Factory (Zheng et al., 2024) as the LLM training platform. Table 12 shows our training hyperparameters.

| Parameter | Value |
|------------------|--------|
| Train batch size | 128 |
| Learning rate | 1.0e-5 |
| Number of epochs | 2.0 |
| LR scheduler | cosine |
| Warmup ratio | 0.1 |
| Precision | bf16 |

Table 12: Hyperparameters for supervised fine-tuning.