

# *Fairness-Aware Online Positive-Unlabeled Learning*

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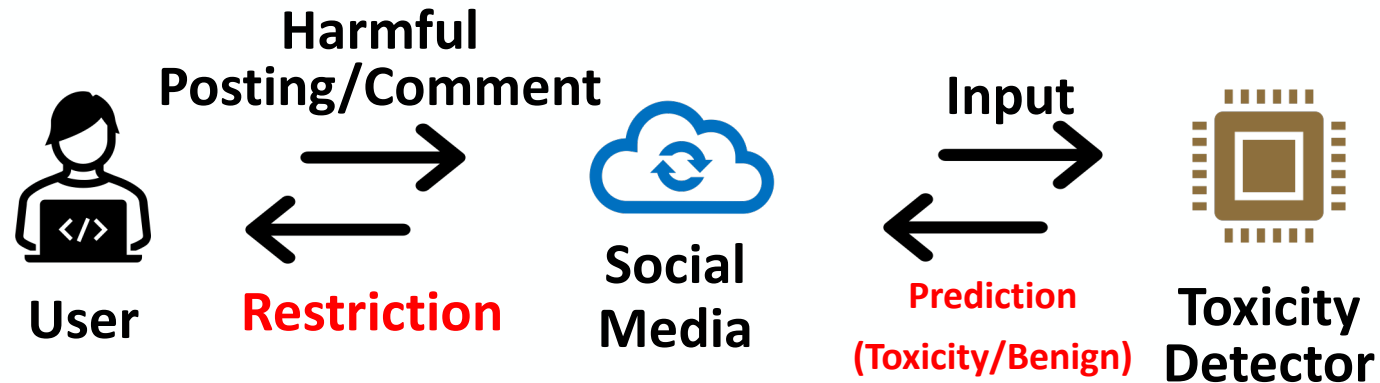


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# Background

## Issues in Text Classification in Reality

- In the real-world, traditional machine learning algorithms are not always adequate.



<Toxicity Detection Framework>

# *Background*

## Issues in Text Classification in Reality

- **Online Environment**

- Data arrives incrementally, not all at once.
- Retraining from scratch with new data is costly and inefficient.

- **Lack of Positivity**

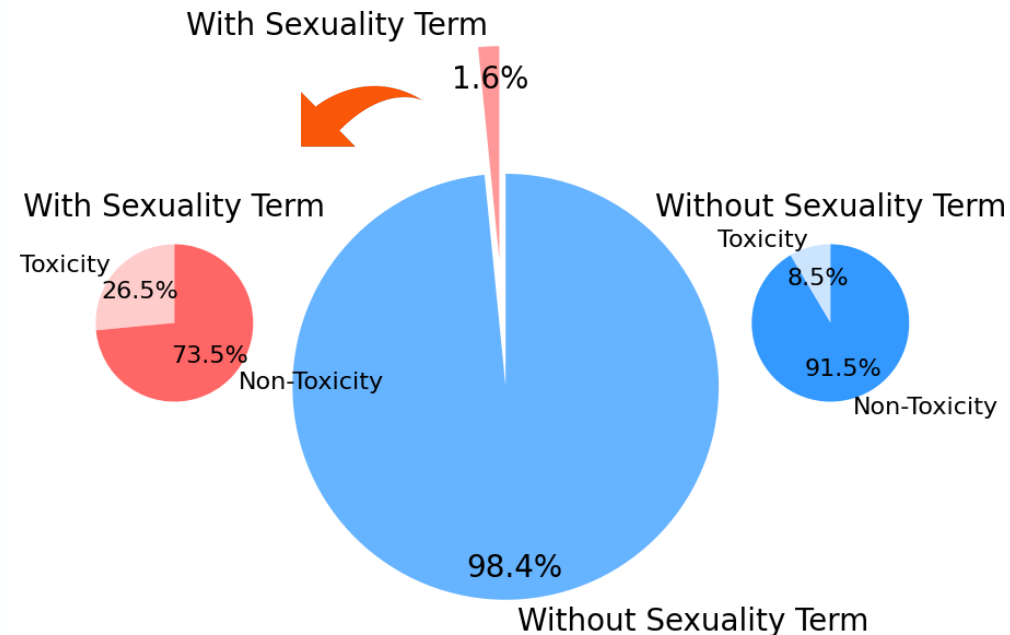
- In many situations, not all positive instances are explicitly labeled.
- Unlabeled samples may include both positive and negative cases.

*e.g., On social media, only a portion of toxic content is flagged,  
while other toxic posts remain unmarked.*

# Background

## Issues in Text Classification in Reality

- **Imbalanced Positivity in Dataset (e.g. Wikipedia Toxicity Dataset)**
  - Certain keywords are often associated with toxicity.
  - This can lead to overestimating toxicity if a content includes these specific terms.



# *Background*

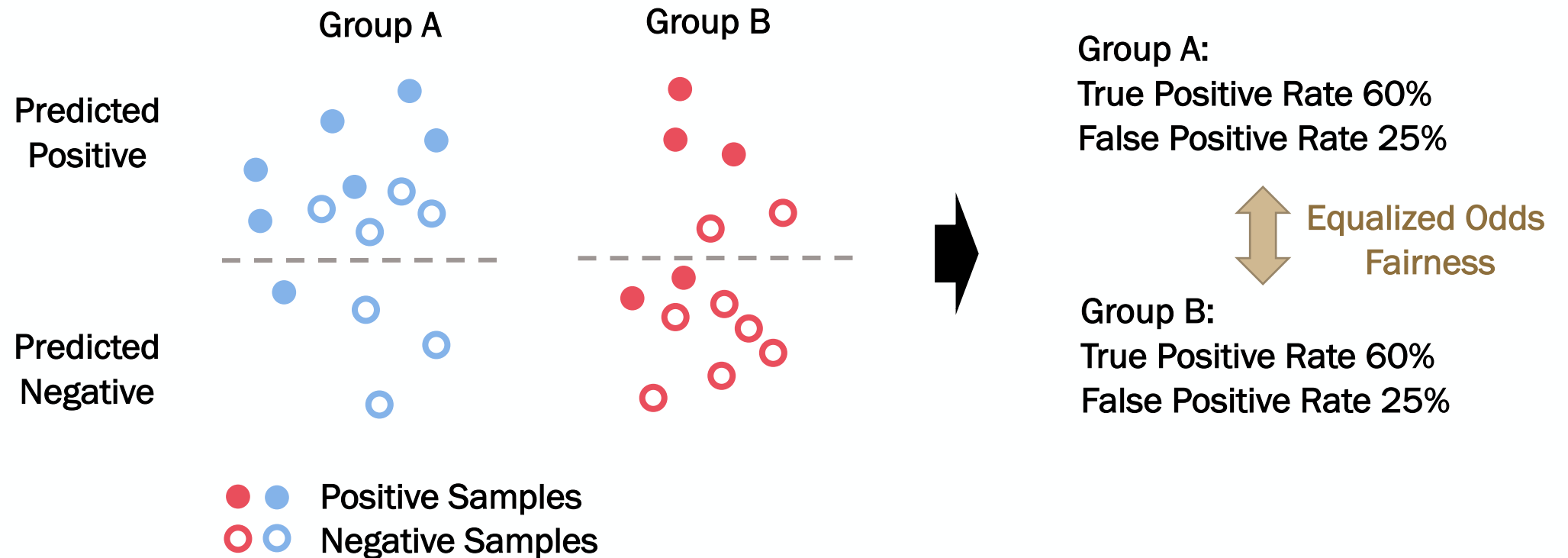
## Issues in Text Classification in Reality

- **Fairness in Classification - Equalized Odds (EOd)**
  - A fairness criterion where a model's predictions are independent of a sensitive attribute (e.g., gender, race) for each outcome.
  - The model should have the same true positive rate and false positive rate across different groups.

# Background

## Issues in Text Classification in Reality

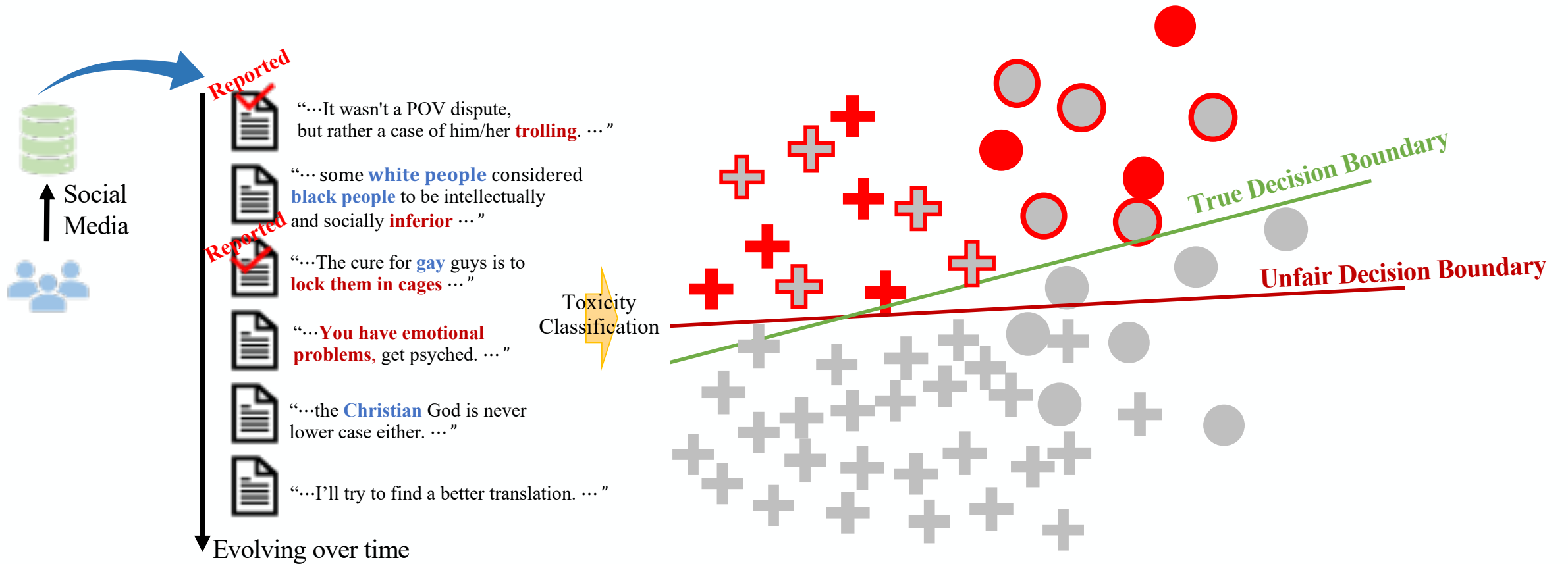
### ▪ Fairness in Classification - Equalized Odds (EOd)



# Background

## Issues in Text Classification in Reality

● w/ identity term    + w/o identity term    ■ Reported Toxicity    □ Non-reported Toxicity    ■ Non-Toxicity



# *Problem Definition*

## Fairness in Online & Positive-Unlabeled Learning

- **Online Learning**

- A classifier is trained on newly arrived data continuously.

- **Positive-Unlabeled (PU) Learning**

- Train with positive and unlabeled set without explicit negativity.
- Unlabeled set could be predicted as either positive and negative.

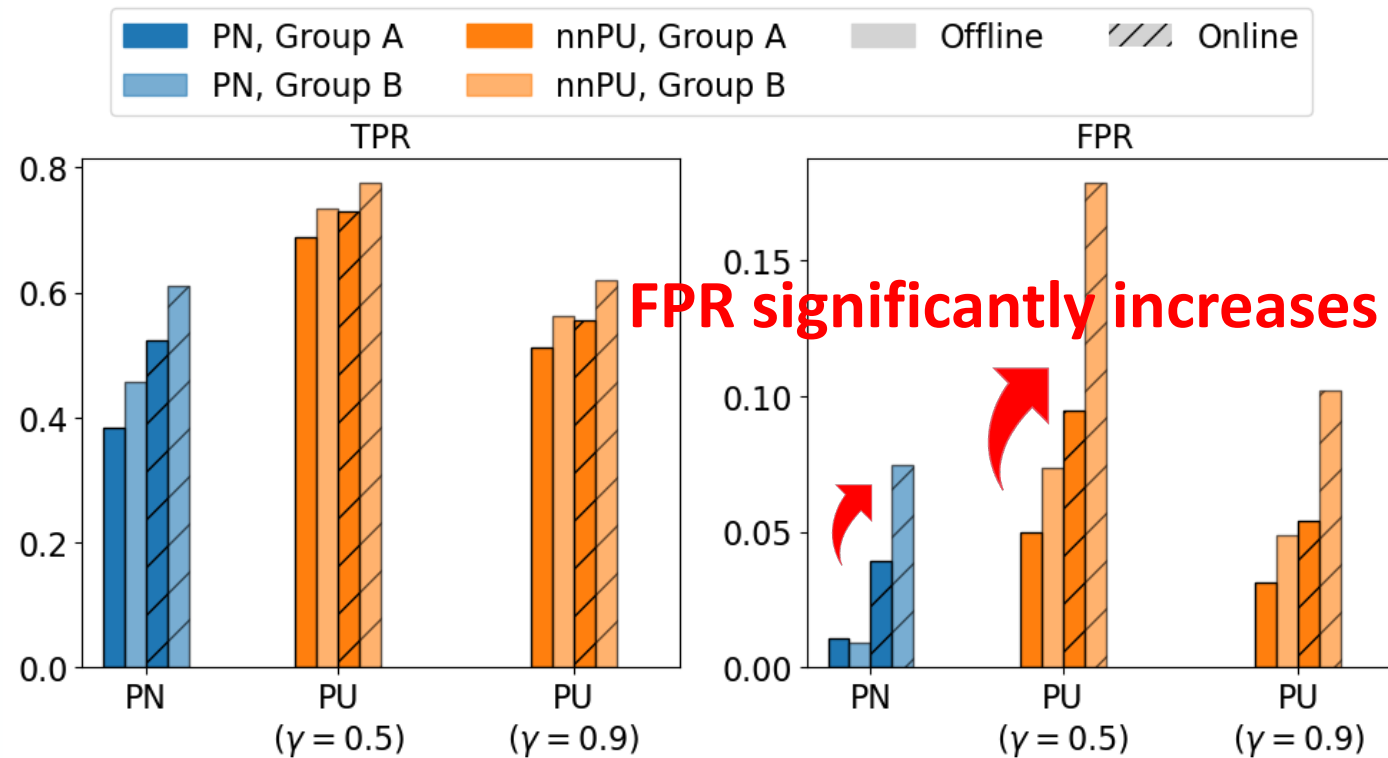
- **Both Online Learning and PU Learning Deteriorate Fairness Issue.**



# Problem Definition

## Fairness in Online & Positive-Unlabeled Learning

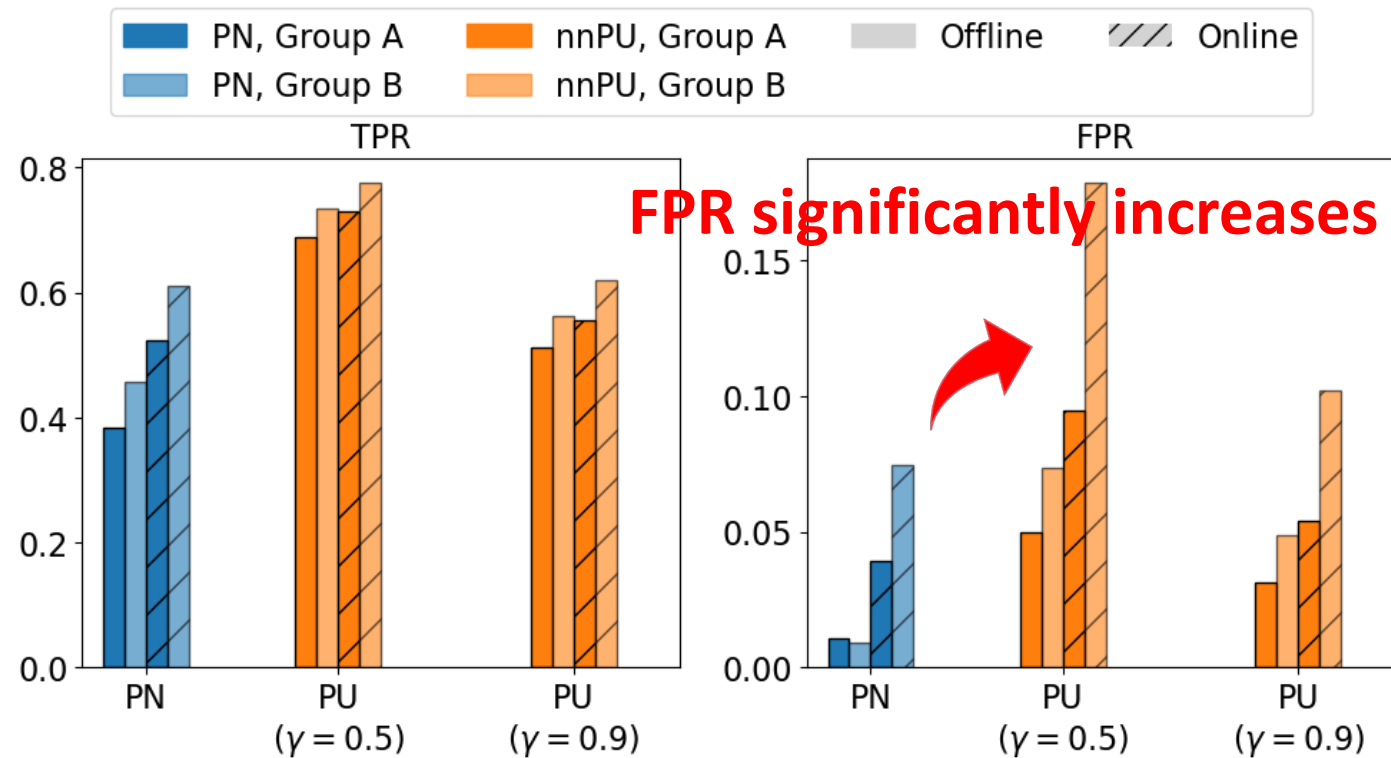
- Both Online Learning and PU Learning Deteriorate Fairness Issue.



# Problem Definition

## Fairness in Online & Positive-Unlabeled Learning

- Both Online Learning and PU Learning Deteriorate Fairness Issue.



# Methodology

## Fairness-Aware Online Positive-Unlabeled Learning (FOPU)

### ▪ Convex Equalized Odd Loss

For two sensitive attribute group  $a \in \{1, -1\}$ , Equalized Odds is defined as

$$EOd = |TPR_{a=1} - TPR_{a=-1}| + |FPR_{a=1} - FPR_{a=-1}|$$

As a relaxed form, the EOd becomes

$$EOd(f) = \mathbb{E} \left[ \frac{\mathbb{I}_{a=1, y=1}}{p_{1,1}} \mathbb{I}_{f(x) > 0} - \left( 1 - \frac{\mathbb{I}_{a=-1, y=1}}{\pi - p_{1,1}} \mathbb{I}_{f(x) < 0} \right) \right] + \mathbb{E} \left[ \frac{\mathbb{I}_{a=1, y=-1}}{p_{1,-1}} \mathbb{I}_{f(x) > 0} - \left( 1 - \frac{\mathbb{I}_{a=-1, y=-1}}{1 - \pi - p_{1,-1}} \mathbb{I}_{f(x) < 0} \right) \right]$$

where  $f$  is a real-valued function and define

$$\pi = P(y = +1)$$

$$1 - \pi = P(y = -1)$$

$$p_{1,1} = P(a = +1, y = +1)$$

$$p_{1,-1} = P(a = +1, y = -1)$$

# Methodology

## Fairness-Aware Online Positive-Unlabeled Learning (FOPU)

### ▪ Convex Equalized Odd Loss

Use Convex-Concave surrogate functions,  $\kappa(z) = \max(z + 1, 0)$ ,  $\delta(z) = \min(z, 1)$  based on empirical EOd,

$$R_{\text{EOd}}(f) = \begin{cases} \text{EOd}_{\kappa}(f) & \text{if } \text{EOd}(f) \geq 0 \\ \text{EOd}_{\delta}(f) & \text{if } \text{EOd}(f) < 0 \end{cases}$$

$$\text{EOd}_{\kappa}(f) = \mathbb{E} \left[ \frac{\mathbb{I}_{a=1,y=1}}{p_{1,1}} \kappa(f(x)) - \left(1 - \frac{\mathbb{I}_{a=-1,y=1}}{\pi - p_{1,1}} \kappa(-f(x))\right) \right] + \mathbb{E} \left[ \frac{\mathbb{I}_{a=1,y=-1}}{p_{1,-1}} \kappa(f(x)) - \left(1 - \frac{\mathbb{I}_{a=-1,y=-1}}{1 - \pi - p_{1,-1}} \kappa(-f(x))\right) \right]$$

$$\text{EOd}_{\delta}(f) = \mathbb{E} \left[ \frac{\mathbb{I}_{a=1,y=1}}{p_{1,1}} \delta(f(x)) - \left(1 - \frac{\mathbb{I}_{a=-1,y=1}}{\pi - p_{1,1}} \delta(-f(x))\right) \right] + \mathbb{E} \left[ \frac{\mathbb{I}_{a=1,y=-1}}{p_{1,-1}} \delta(f(x)) - \left(1 - \frac{\mathbb{I}_{a=-1,y=-1}}{1 - \pi - p_{1,-1}} \delta(-f(x))\right) \right]$$

# Methodology

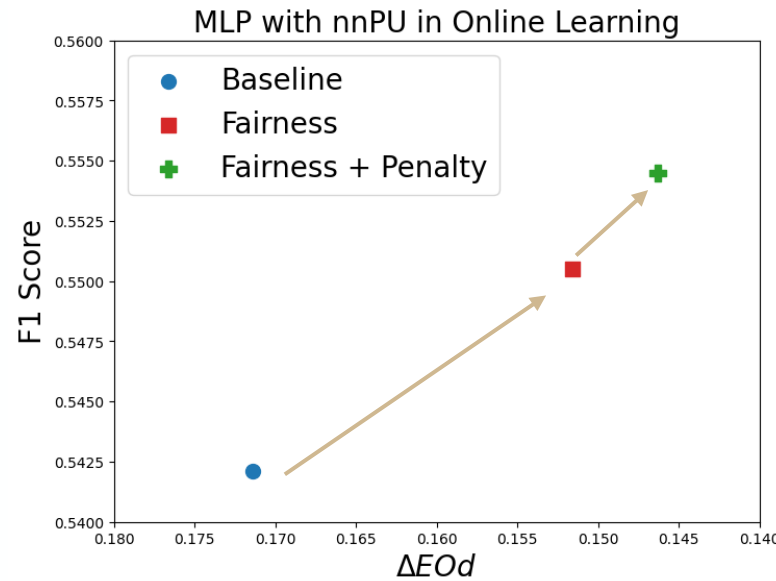
## Fairness-Aware Online Positive-Unlabeled Learning (FOPU)

$$EOd = |TPR_{a=1} - TPR_{a=-1}| + |FPR_{a=1} - FPR_{a=-1}|$$

### ■ Positive Rate Penalty Loss

- Minimizing  $\Delta EOd$  can sometimes lead to a decrease in TPR or an increase in FPR.
- The positive rate penalty encourages higher TPR and lower FPR.

$$\mathcal{L}_p^{(t)} = \max(0, TPR_1^{base} - TPR_1^{(t)}) + \max(0, TPR_0^{base} - TPR_0^{(t)}) + \max(FPR_1^{(t)} - FPR_1^{base}, 0) + \max(FPR_0^{(t)} - FPR_0^{base}, 0)$$



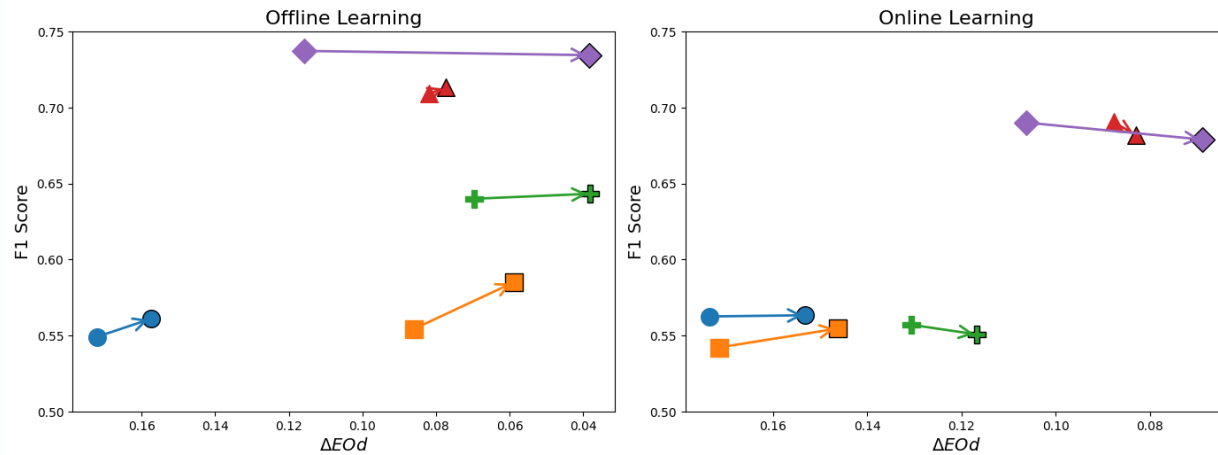
# Experiments & Analysis

## Adaptability of FOPU

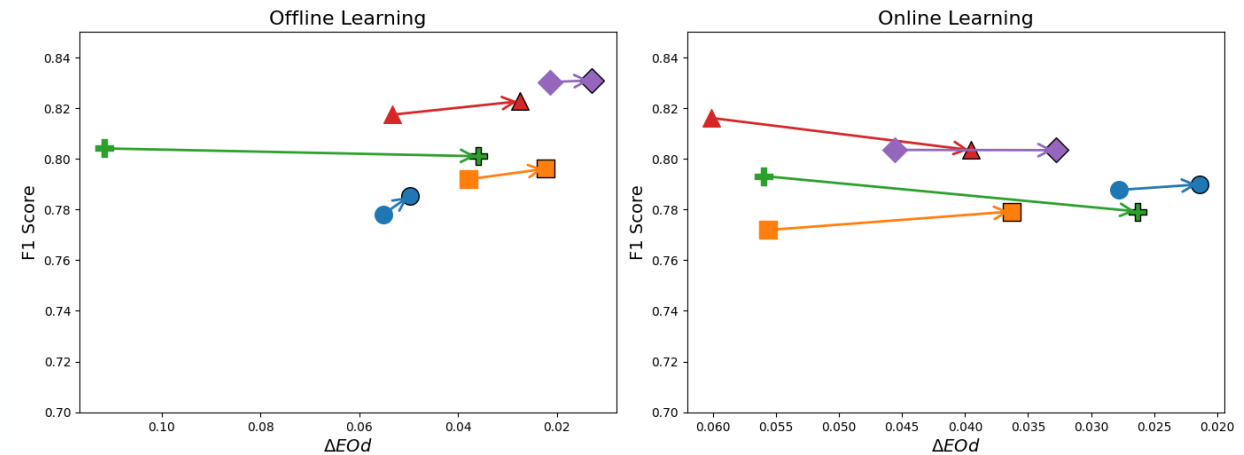
- Apply FOPU to Linear, MLP, LSTM, BERT and DistillBERT

● Linear   ■ MLP   + LSTM   ▲ BERT   ◆ DistillBERT

Wikipedia Dataset (Toxicity Classification)



NELA-2018 Dataset (Misinformation Detection)



**FOPU improves fairness while maintaining performance (F1 score)**

# Theoretical Analysis

## Fair Regret Bound

### ▪ Fair Regret Bound in Online Learning

- **Regret Bound:** Measures how much a learning algorithm's performance deviates from the batch training over time.  $Regret = \sum_{t=1}^T \mathbb{E}[R(f_t) - R(f_{off})]$

- **Fair Regret Bound:** Ensuring that the model's cumulative fairness violations.

- Linear Classifier's Fair Regret Bound:  $O(\sqrt{T}/b)$

$T$ : Total Number of Training Round

$B$ : Batch Size of Incoming Data

- MLP Classifier's Fair Regret Bound:  $O(\sqrt{T \log L} + \sqrt{T}/b)$

$L$ : Number of Layers

- Pretrained Networks (e.g., BERT) with Linear Classifier:  $O(\sqrt{T}/b)$

# Conclusion

- Developed a fairness-aware online PU learning framework with a theoretical fair regret bound.
- Demonstrated improved fairness (lower  $\Delta EOd$ ) without compromising classification performance.
- Provided a practical solution for real-time applications in text classification, adapting efficiently to new data for various datasets and models.



# *Thank You*

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