

A Survey of Recent Advances in Efficient Parsing for Graph Grammars

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- 0 Introduction**
- 1 Context-Free Graph Grammars**
- 2 General Approaches to HRG Parsing**
- 3 LL- and LR-like Restrictions to Avoid Backtracking**
- 4 Unique Decomposability**
- 5 Systems and Tools**
- 6 Future Work?**

Introduction

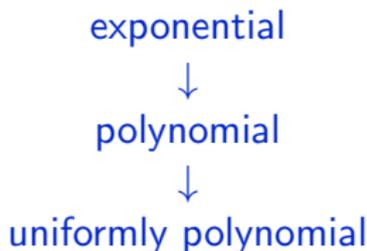
Context-Free Graph Grammars and Parsing

Brief facts about context-free graph grammars:

- ① emerged in the 1980s
- ② generalization of context-free string grammars to graphs
- ③ can easily generate NP-complete graph languages
⇒ even **non-uniform** parsing is impractical
- ④ early polynomial solutions were merely of theoretical interest:
 - strong restrictions
 - restrictions difficult to check
 - degree of polynomial usually depends on grammar
- ⑤ renewed interest nowadays due to **Abstract Meaning Representation** and similar notions of semantic graphs in computational linguistics.

Recent attempts use different strategies to deal with NP-completeness:

- ① Do your best, but be prepared to **pay the price** in the worst case.
- ② Generate deterministic parsers based on **LL- or LR-like** restrictions.
- ③ Make sure that the generated graphs have a **unique decomposition** which determine the structure of derivation trees.

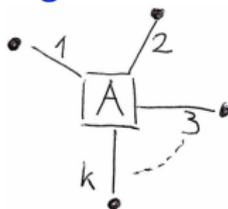


This talk will summarize those approaches.

Context-Free Graph Grammars

Here: hyperedge-replacement grammars

Graphs contain **labelled hyperedges** instead of edges:



The number k is the **rank** of A and of the hyperedge.

Rank 2 yields an ordinary edge: $o \xrightarrow{1} [A] \xrightarrow{2} o$ is $o \xrightarrow{A} o$.

Some nodes may be marked $1, 2, \dots, p$ and are called **ports**.

The number p is the **rank** of the hypergraph.

From now on: “edge” means “hyperedge”

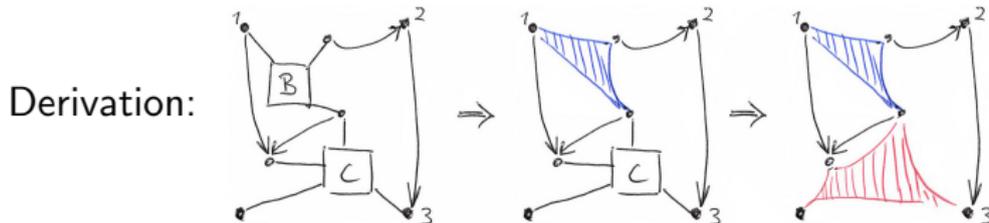
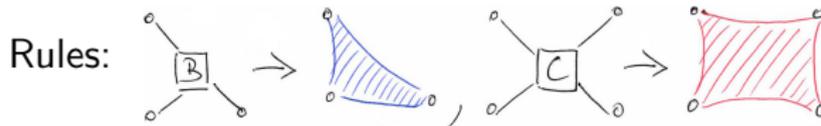
“graph” means “hypergraph”

Hyperedge Replacement (HR)

Hyperedge replacement:

- A **rule** $A \rightarrow H$ consists of a label A and a graph H of equal rank.
- Rule application:
 - ① remove a hyperedge e with label A ,
 - ② insert H by fusing its ports with the incident nodes of e .

Example



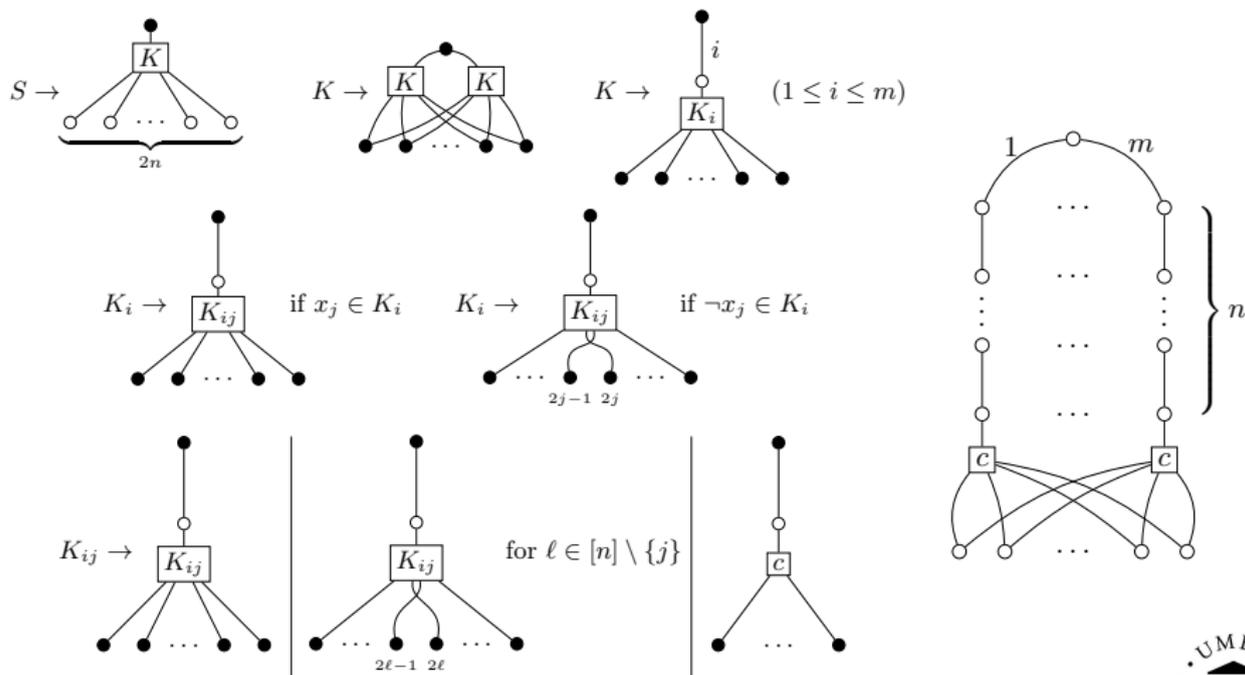
Why is Parsing Difficult?

Cocke-Kasami-Younger for HR works, but is inefficient because a graph has exponentially many subgraphs.

Even when this is not the problem, we still have too many ways to order the attached nodes of nonterminal hyperedges. . .



Consider a propositional formula $K_1 \wedge \dots \wedge K_m$ over x_1, \dots, x_n in CNF.



Early Approaches to HR Grammar Parsing

- Cocke-Kasami-Younger style:
 - Conditions for polynomial running time³
 - DiaGen⁴
- Cubic parsing of languages of strongly connected graphs^{5 6}
- After that, the area fell more or less silent for almost 2 decades.

Then came [Abstract Meaning Representation](#)⁷,
and with it a renewed interest in the question.

³Lautemann, *Acta Inf.* 27, 1990

⁴Minas, *Proc. IEEE Symposium on Visual Languages* 1997

⁵W. Vogler, *LNCS* 532, 1990

⁶D., *Theoretical Computer Science* 109, 1993

⁷Banarescu et al., *Proc. 7th Linguistic Annotation Workshop, ACL* 2013



Recent General Approaches to HRG Parsing

Choosing Generality over (Guaranteed) Efficiency

Approaches that avoid restrictions (exponential worst-case behaviour):

- Lautemann's algorithm refined by efficient matching⁸, implemented in [Bolin](#)
- S-graph grammar parsing⁹, using interpreted regular tree grammars as implemented in [Alto](#)
- Generalized predictive shift-reduce parsing¹⁰, implemented in [Grappa](#)

⁸Chiang et al., ACL 2013

⁹Groschwitz et al., ACL 2015

¹⁰Hoffmann & Minas, LNCS 11417, 2019



The Approach by Chiang et al.

- Use **dynamic programming** to determine, for “every” subgraph G' of the input G , the set of nonterminals A that can derive G' .
- “Every”: Consider G' that can be cut out along $rank(A)$ nodes.
- For efficient matching of rules, use **tree decompositions of right-hand sides**.

The algorithm runs in time $O((3^d n)^{k+1})$ where

- d is the node degree of G ,
- n is the number of nodes, and
- k is the width of tree decompositions of right-hand sides.

Important: G is assumed to be connected!



The S-Graph Grammar Approach

- Instead of HR, use the more primitive **graph construction** operations by Engelfriet and Courcelle with **interpreted regular tree grammars**¹¹.
- Strategy (**parsing by intersection**):
 - Compute regular tree language L_G of all trees denoting G .
 - Intersect with the language of the grammar's derivation trees.
 - Trick: use a **lazy approach** to avoid building L_G explicitly.

The algorithm runs in time $O(n^s 3^{sep(s)})$ where

- s is the number of **source names** (\sim number of ports)
- $sep(s)$ is Lautemann's s -separability ($\leq n$)

Alto is reported to be 6722 times faster than Bolinas on a set of AMRs from the "Little Prince" AMR-bank.

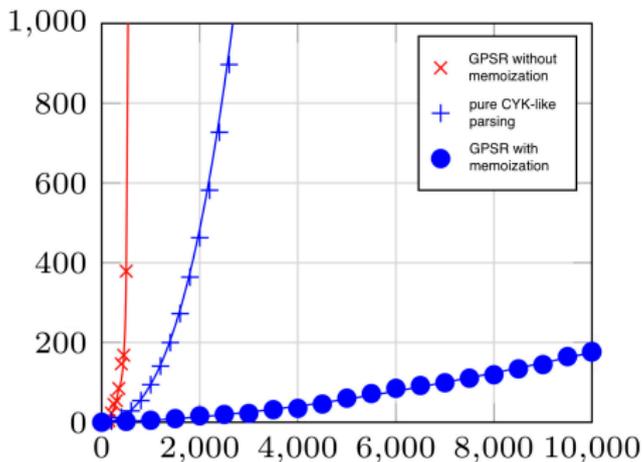
¹¹Koller & Kuhlmann, Proc. Intl. Conf. on Parsing Technologies 2011



Generalized Predictive Shift-Reduce Parsing

- A **compiler generator** approach.
- Use **LR parsing** from compiler construction, but allow conflicts.
- Parser uses **characteristic finite automaton** to select actions.
- In case of conflicts, use breadth-first search implemented with **graph structured stack**.
- In addition, use **memoization**.

Grappa measurements for a grammar generating Sierpinski graphs (by M. Minas):



LL- and LR-like Restrictions to Avoid Backtracking

Two versions of **predictive parsing**:

- deterministic recursive descent, generalizing SLL string parsing
→ **predictive top-down**¹²
- deterministic bottom-up, generalizing SLR string parsing
→ **predictive shift-reduce**¹³

Common modus operandi:

- View right-hand side as a list of edges to be **matched step by step**.
- Terminal edges are “consumed” from the input graph.
- Nonterminal edges are handled by **recursive call** (top-down) or **reduction** (bottom-up).

¹²D., Hoffmann, Minas, LNCS 10373, 2015

¹³D., Hoffmann, Minas, J. Logical and Alg. Methods in Prog. 104, 2019

Predictive Top-Down Parsing (PTD)

In PTD parsing, each nonterminal A becomes a parsing procedure:

- parser generator determines **lookahead** for every A -rule:
rest graphs (lookahead sets) for alternative A -rules must be disjoint
 \Rightarrow the current rest graph determines which rule to apply;
- in doing so, we have to distinguish between different **profiles** of A ;
- alternative terminal edges require **free edge choice**.

Lookahead and free edge choice are **approximated by Parikh sets** to obtain efficiently testable conditions.

Running time of generated parser is $O(n^2)$.



Predictive Shift-Reduce Parsing (PSR)

PSR parsing **reduces** the input graph back to the initial nonterminal:

- parser maintains a stack representing the graph to which the input read so far has been reduced
- **shift** steps read the next terminal edge from the input graph (free edge choice needed here as well)
- **reduce** steps replace rhs on top of stack with lhs
- parser generator determines **characteristic finite automaton (CFA)** that guides the choice of shift and reduce steps
- CFA must be **conflict free**
- string parsing only faces shift-reduce and reduce-reduce conflicts; now there may also be **shift-shift conflicts**.

Running time of generated parser is $O(n)$.



Unique Decomposability

- PTD and PSR grammar analysis can be expensive for **large grammars**.
- In NLP, grammars may be volatile and very large
⇒ **uniformly polynomial parsing** may be preferable.
- Restrictions take inspiration of **Abstract Meaning Representation**, viewing graphs as **trees with reentrancies**.
- Original strong assumptions¹⁴ were later relaxed¹⁵ and extended to weighted HR grammars¹⁶.
- This type of HR grammar can also be **learned à la Angluin**¹⁷.

¹⁴H. Björklund et al., LNCS 9618, 2016

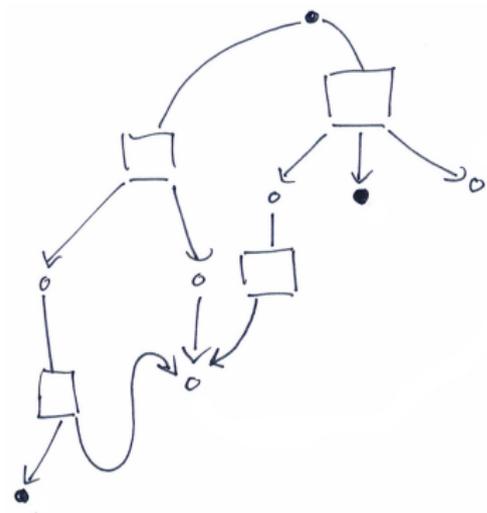
¹⁵H. Björklund et al., 2018 (under review)

¹⁶H. Björklund et al., Mathematics of Language 2018

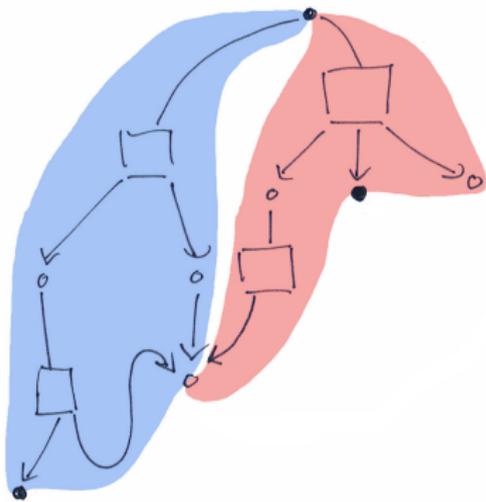
¹⁷J. Björklund et al., LNCS 10329, 2017



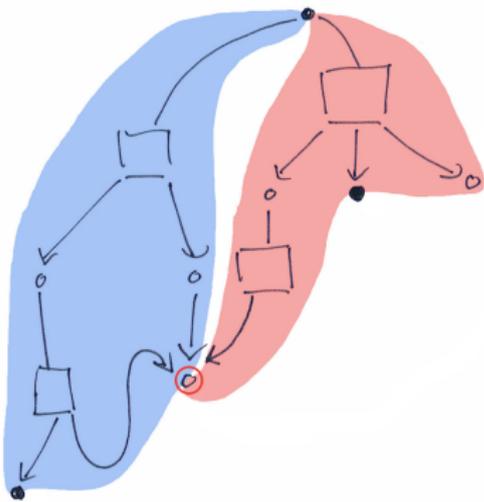
Reentrancies in a nutshell (bullets are ports)



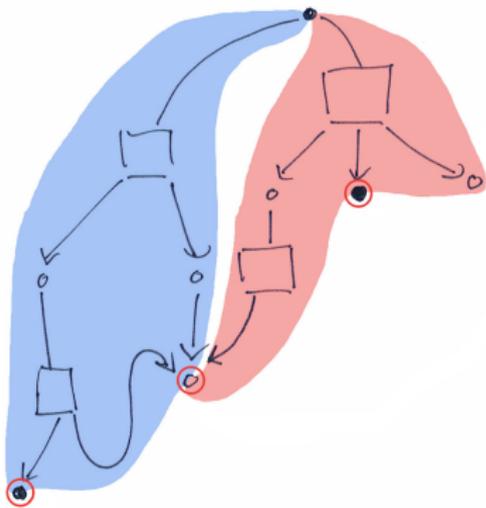
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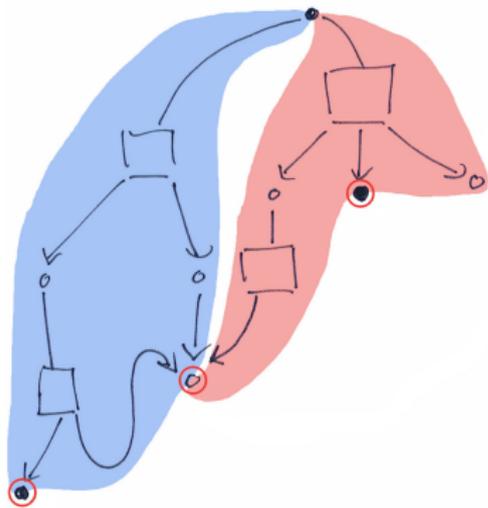
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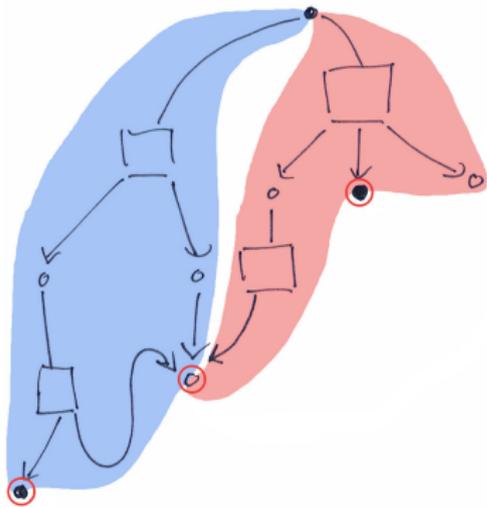
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Requirements on right-hand sides:

- 1 targets of every nonterminal hyperedge e are reentrant w.r.t. e
- 2 all nodes reachable from the root

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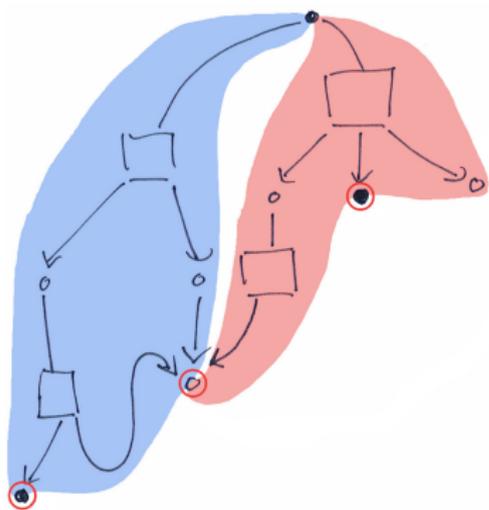


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Yields a unique hierarchical decomposition revealing the structure of derivation trees.

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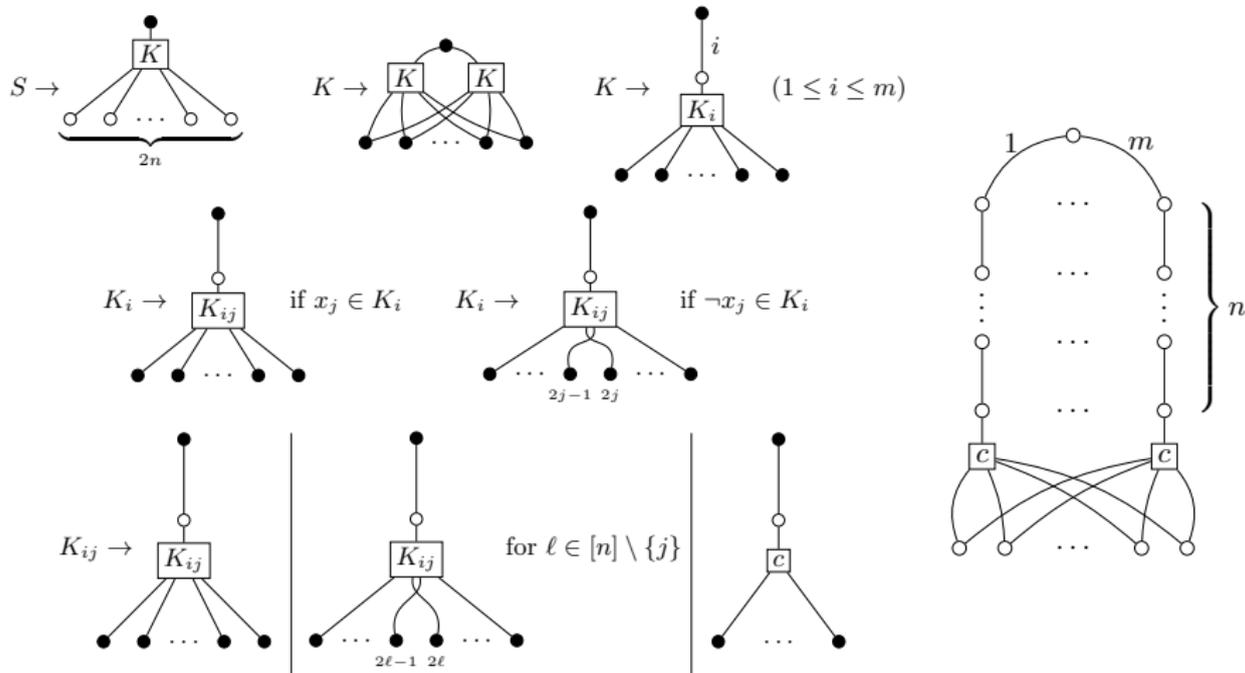
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Yields a unique hierarchical decomposition revealing the structure of derivation trees.

However, there is one problem left. . .

Recall: Reducing SAT



Conclusion: we also need **order preservation!**

We must provide a binary relation on nodes that

- ① is efficiently computable,
- ② coincides with the order of targets of nonterminal edges, and
- ③ is compatible with hyperedge replacement.

Theorem

For a reentrancy and order preserving HRG \mathcal{G} and a graph G as input, $G \in L(\mathcal{G})$ can be decided in time

$$O(\max(|\mathcal{G}|, |G|)^2).$$

This holds also for computing the weight of G if the rules of \mathcal{G} have weights from a commutative semiring.

Systems and Tools

Bolinas¹⁸ (USC/ISI, D. Bauer, K. Knight) implements the parser of (Chiang et al., ACL 2013).

Main features:

- weighted rules
- n -best derivations
- translation via synchronous HR grammars
- EM training from corpora

¹⁸<http://www.isi.edu/licensed-sw/bolinas>



Alto¹⁹ (A. Koller) implements *interpreted regular tree grammars*.

One instantiation is the HR parser of (Koller & Kuhlmann, 2011).

Main features correspond to those of Bolinas:

- weighted rules
- n -best derivations
- translation via synchronous HR grammars
- EM training from corpora

¹⁹<http://github.com/coli-saar/alto>

Grappa²⁰ (M. Minas) provides parser generators for HRG grammars.

Main features:

- generators for predictive top-down (PTD), predictive shift-reduce (PSR), generalized PSR parsers
- can generate PTD and PSR parsers for **contextual HR grammars**²¹
- is constantly being improved and extended
- has a tasty logo

²⁰<http://www.unibw.de/inf2/grappa>

²¹Drewes & Hoffmann, Acta Informatica 52 2015



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Future Work?

Some Questions for Future Work

- How to make HR grammars efficiently parsable **by design**?
- Can HR grammars be **learned from data** so that they are (1) small and (2) efficiently parsable?
- What are useful and benign **extensions** that can be handled efficiently (like contextual HR)?
- How to handle **node labels** in a good way (e.g., enabling **relabelling**)?
- Efficient **transductions** that turn strings/trees into graphs?

Thank you!

Questions?

