Winter School

Day 2: Word-based models and the EM algorithm

MT Marathon

27 Jan 2009





Lexical translation

• How to translate a word \rightarrow look up in dictionary

Haus — house, building, home, household, shell.

- Multiple translations
 - some more frequent than others
 - for instance: *house*, and *building* most common
 - special cases: *Haus* of a *snail* is its *shell*
- Note: During all the lectures, we will translate from a foreign language into English



Collect statistics

• Look at a *parallel corpus* (German text along with English translation)

Translation of Haus	Count
house	8,000
building	1,600
home	200
household	150
shell	50



Estimate translation probabilities

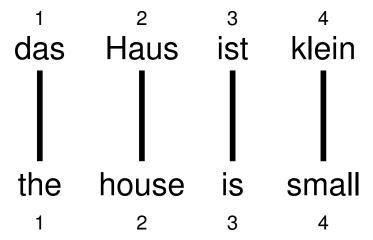
• Maximum likelihood estimation

$$p_f(e) = \begin{cases} 0.8 & \text{if } e = \text{house}, \\ 0.16 & \text{if } e = \text{building}, \\ 0.02 & \text{if } e = \text{home}, \\ 0.015 & \text{if } e = \text{household}, \\ 0.005 & \text{if } e = \text{shell}. \end{cases}$$



Alignment

• In a parallel text (or when we translate), we **align** words in one language with the words in the other



• Word *positions* are numbered 1–4



Alignment function

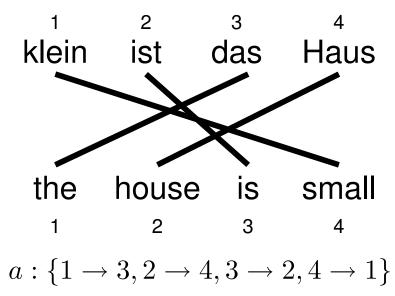
- Formalizing *alignment* with an **alignment function**
- Mapping an English target word at position i to a German source word at position j with a function $a:i\to j$
- Example

$$a: \{1 \rightarrow 1, 2 \rightarrow 2, 3 \rightarrow 3, 4 \rightarrow 4\}$$



Reordering

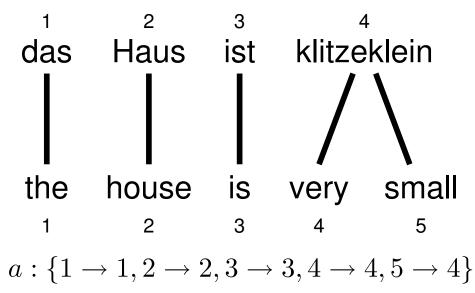
• Words may be **reordered** during translation





One-to-many translation

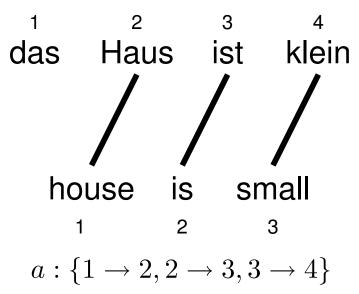
• A source word may translate into **multiple** target words





Dropping words

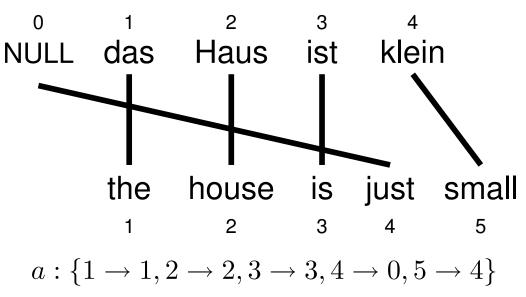
- Words may be **dropped** when translated
 - The German article *das* is dropped





Inserting words

- Words may be **added** during translation
 - The English *just* does not have an equivalent in German
 - We still need to map it to something: special NULL token





IBM Model 1

- Generative model: break up translation process into smaller steps

 IBM Model 1 only uses lexical translation
- Translation probability
 - for a foreign sentence $\mathbf{f} = (f_1, ..., f_{l_f})$ of length l_f
 - to an English sentence $\mathbf{e} = (e_1, ..., e_{l_e})$ of length l_e
 - with an alignment of each English word e_j to a foreign word f_i according to the alignment function $a: j \to i$

$$p(\mathbf{e}, a | \mathbf{f}) = \frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j | f_{a(j)})$$

– parameter ϵ is a *normalization constant*



Example

das		Haus		ist			klein	
e	t(e f)	e	t(e f)	e	t(e f)		e	t(e f)
the	0.7	house	0.8	is	0.8		small	0.4
that	0.15	building	0.16	's	0.16		little	0.4
which	0.075	home	0.02	exists	0.02		short	0.1
who	0.05	household	0.015	has	0.015		minor	0.06
this	0.025	shell	0.005	are	0.005		petty	0.04

$$p(e, a|f) = \frac{\epsilon}{4^3} \times t(\text{the}|\text{das}) \times t(\text{house}|\text{Haus}) \times t(\text{is}|\text{ist}) \times t(\text{small}|\text{klein})$$
$$= \frac{\epsilon}{4^3} \times 0.7 \times 0.8 \times 0.8 \times 0.4$$
$$= 0.0028\epsilon$$



Learning lexical translation models

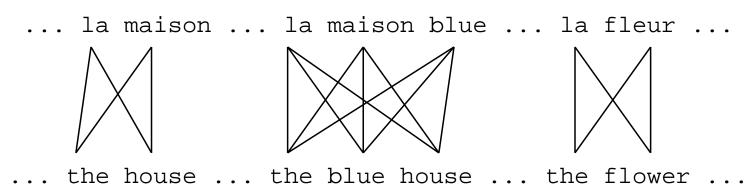
- \bullet We would like to estimate the lexical translation probabilities t(e|f) from a parallel corpus
- ... but we do not have the alignments
- Chicken and egg problem
 - if we had the *alignments*,
 - \rightarrow we could estimate the parameters of our generative model
 - if we had the *parameters*,
 - \rightarrow we could estimate the *alignments*



• Incomplete data

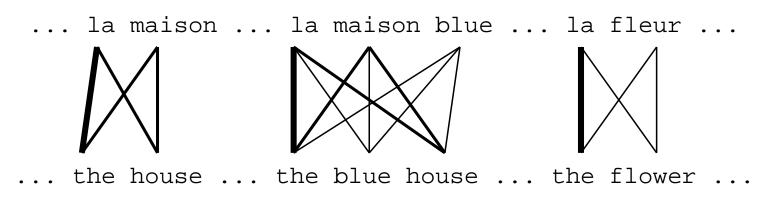
- if we had *complete data*, would could estimate *model*
- if we had *model*, we could fill in the *gaps in the data*
- Expectation Maximization (EM) in a nutshell
 - initialize model parameters (e.g. uniform)
 - assign probabilities to the missing data
 - estimate model parameters from completed data
 - iterate





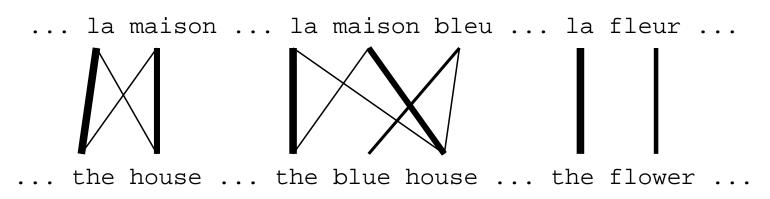
- Initial step: all alignments equally likely
- Model learns that, e.g., *la* is often aligned with *the*



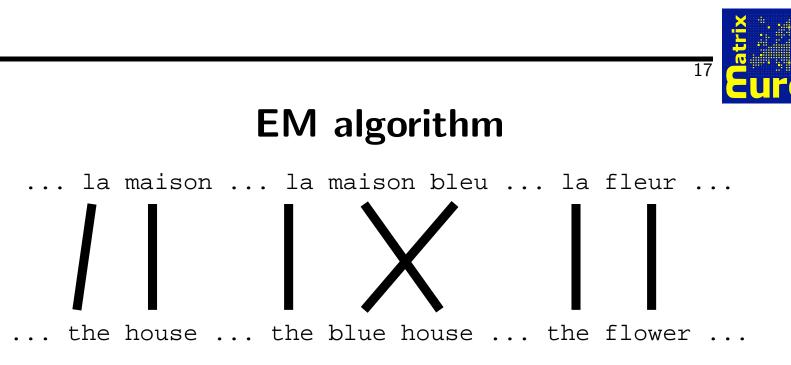


- After one iteration
- Alignments, e.g., between *la* and *the* are more likely

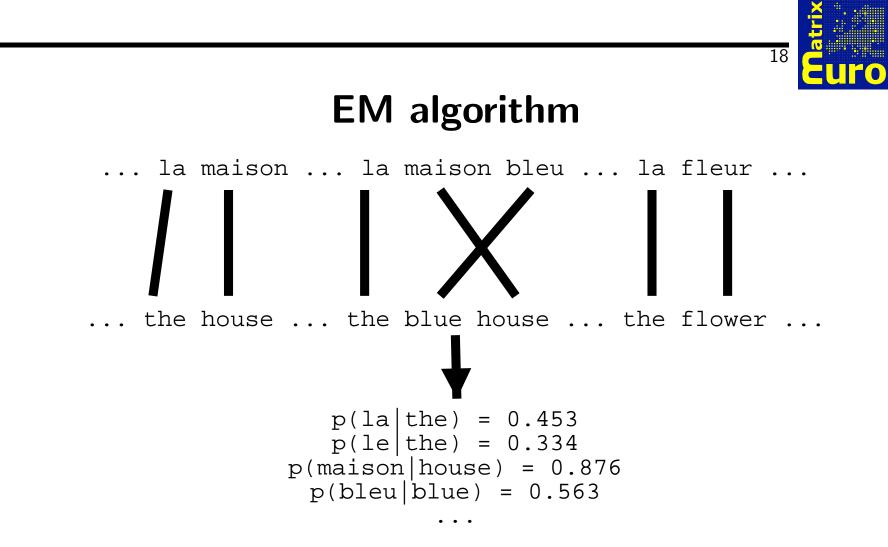




- After another iteration
- It becomes apparent that alignments, e.g., between *fleur* and *flower* are more likely (**pigeon hole principle**)



- Convergence
- Inherent hidden structure revealed by EM



• Parameter estimation from the aligned corpus



IBM Model 1 and EM

- EM Algorithm consists of two steps
- **Expectation-Step**: Apply model to the data
 - parts of the model are hidden (here: alignments)
 - using the model, assign probabilities to possible values
- Maximization-Step: Estimate model from data
 - take assign values as fact
 - collect counts (weighted by probabilities)
 - estimate model from counts
- Iterate these steps until **convergence**



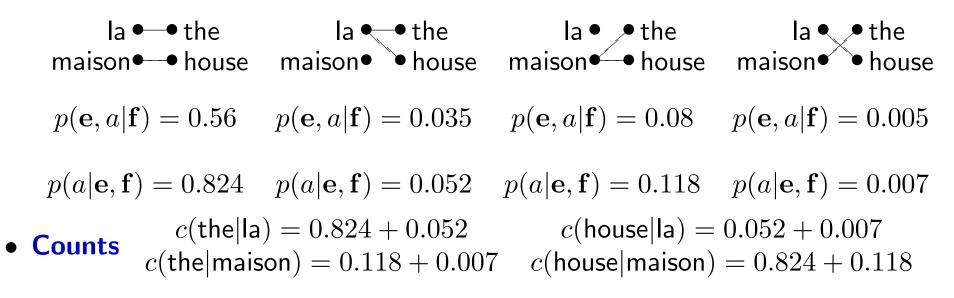
IBM Model 1 and EM

- We need to be able to compute:
 - Expectation-Step: probability of alignments
 - Maximization-Step: estimate translation probabilities from weighted counts



IBM Model 1 and EM

- $\begin{array}{ll} \bullet \mbox{ Probabilities } & p(\mathsf{the}|\mathsf{la}) = 0.7 & p(\mathsf{house}|\mathsf{la}) = 0.05 \\ p(\mathsf{the}|\mathsf{maison}) = 0.1 & p(\mathsf{house}|\mathsf{maison}) = 0.8 \end{array}$
- Alignments





- We need to compute $p(a|\mathbf{e},\mathbf{f})$
- Applying the *chain rule*:

$$p(a|\mathbf{e}, \mathbf{f}) = rac{p(\mathbf{e}, a|\mathbf{f})}{p(\mathbf{e}|\mathbf{f})}$$

• We already have the formula for $p(\mathbf{e}, \mathbf{a} | \mathbf{f})$ (definition of Model 1)



• We need to compute $p(\mathbf{e}|\mathbf{f})$

$$\begin{split} p(\mathbf{e}|\mathbf{f}) &= \sum_{a} p(\mathbf{e}, a | \mathbf{f}) \\ &= \sum_{a(1)=0}^{l_f} \dots \sum_{a(l_e)=0}^{l_f} p(\mathbf{e}, a | \mathbf{f}) \\ &= \sum_{a(1)=0}^{l_f} \dots \sum_{a(l_e)=0}^{l_f} \frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j | f_{a(j)}) \end{split}$$



$$p(\mathbf{e}|\mathbf{f}) = \sum_{a(1)=0}^{l_f} \dots \sum_{a(l_e)=0}^{l_f} \frac{\epsilon}{(l_f+1)^{l_e}} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})$$
$$= \frac{\epsilon}{(l_f+1)^{l_e}} \sum_{a(1)=0}^{l_f} \dots \sum_{a(l_e)=0}^{l_f} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})$$
$$= \frac{\epsilon}{(l_f+1)^{l_e}} \prod_{j=1}^{l_e} \sum_{i=0}^{l_f} t(e_j|f_i)$$

- Note the trick in the last line
 - removes the need for an *exponential* number of products
 - $\rightarrow\,$ this makes IBM Model 1 estimation tractable



The trick

(case
$$l_e = l_f = 2$$
)

$$\begin{split} \sum_{a(1)=0}^{2} \sum_{a(2)=0}^{2} &= \frac{\epsilon}{3^{2}} \prod_{j=1}^{2} t(e_{j}|f_{a(j)}) = \\ &= t(e_{1}|f_{0}) \ t(e_{2}|f_{0}) + t(e_{1}|f_{0}) \ t(e_{2}|f_{1}) + t(e_{1}|f_{0}) \ t(e_{2}|f_{2}) + \\ &+ t(e_{1}|f_{1}) \ t(e_{2}|f_{0}) + t(e_{1}|f_{1}) \ t(e_{2}|f_{1}) + t(e_{1}|f_{1}) \ t(e_{2}|f_{2}) + \\ &+ t(e_{1}|f_{2}) \ t(e_{2}|f_{0}) + t(e_{1}|f_{2}) \ t(e_{2}|f_{1}) + t(e_{1}|f_{2}) \ t(e_{2}|f_{2}) \\ &= t(e_{1}|f_{0}) \ [t(e_{2}|f_{0}) + t(e_{2}|f_{1}) + t(e_{2}|f_{2})] + \\ &+ t(e_{1}|f_{1}) \ [t(e_{2}|f_{1}) + t(e_{2}|f_{1}) + t(e_{2}|f_{2})] + \\ &+ t(e_{1}|f_{2}) \ [t(e_{2}|f_{2}) + t(e_{2}|f_{1}) + t(e_{2}|f_{2})] \\ &= \ [t(e_{1}|f_{0}) + t(e_{1}|f_{1}) + t(e_{1}|f_{2})] \ [t(e_{2}|f_{2}) + t(e_{2}|f_{2})] \end{split}$$



• Combine what we have:

 $p(a|\mathbf{e}, \mathbf{f}) = p(\mathbf{e}, a|\mathbf{f}) / p(\mathbf{e}|\mathbf{f})$ = $\frac{\frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j|f_{a(j)})}{\frac{\epsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} \sum_{i=0}^{l_f} t(e_j|f_i)}$ = $\prod_{j=1}^{l_e} \frac{t(e_j|f_{a(j)})}{\sum_{i=0}^{l_f} t(e_j|f_i)}$



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IBM Model 1 and EM: Maximization Step

- Now we have to *collect counts*
- Evidence from a sentence pair e, f that word e is a translation of word f:

$$c(e|f; \mathbf{e}, \mathbf{f}) = \sum_{a} p(a|\mathbf{e}, \mathbf{f}) \sum_{j=1}^{l_e} \delta(e, e_j) \delta(f, f_{a(j)})$$

• Using the expression on the previous slide, and noting that only alignments which link e and f are relevant, we obtain:

$$c(e|f; \mathbf{e}, \mathbf{f}) = \frac{t(e|f)}{\sum_{i=0}^{l_f} t(e|f_i)} \sum_{j=1}^{l_e} \delta(e, e_j) \sum_{i=0}^{l_f} \delta(f, f_i)$$



• After collecting these counts over a corpus, we can estimate the model:

$$t(e|f;\mathbf{e},\mathbf{f}) = \frac{\sum_{(\mathbf{e},\mathbf{f})} c(e|f;\mathbf{e},\mathbf{f}))}{\sum_{f} \sum_{(\mathbf{e},\mathbf{f})} c(e|f;\mathbf{e},\mathbf{f}))}$$



IBM Model 1 and EM: Pseudocode

```
initialize t(e|f) uniformly
do until convergence
  set count(e|f) to 0 for all e,f
  set total(f) to 0 for all f
  for all sentence pairs (e_s,f_s)
    for all words e in e s
     total_s(e) = 0
      for all words f in f_s
        total_s(e) += t(e|f)
    for all words e in e_s
      for all words f in f_s
        count(e|f) += t(e|f) / total_s(e)
        total(f) += t(e|f) / total_s(e)
  for all f
    for all e
     t(e|f) = count(e|f) / total(f)
```



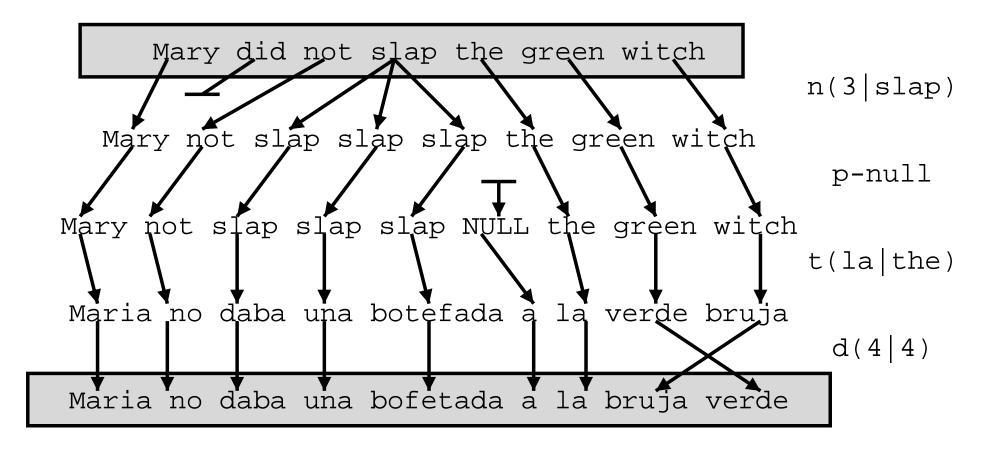
Higher IBM Models

IBM Model 1	lexical translation	
IBM Model 2	adds absolute reordering model	
IBM Model 3	adds fertility model	
IBM Model 4	relative reordering model	
IBM Model 5	fixes deficiency	

- Only IBM Model 1 has *global maximum*
 - training of a higher IBM model builds on previous model
- Computionally biggest change in Model 3
 - trick to simplify estimation does not work anymore
 - \rightarrow *exhaustive* count collection becomes computationally too expensive
 - sampling over high probability alignments is used instead

³¹ Euro

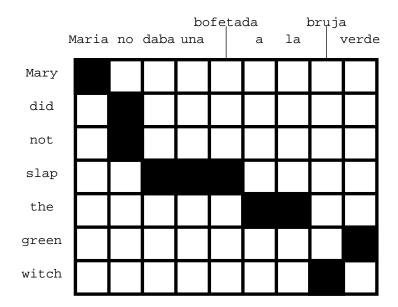
IBM Model 4





Word alignment

- IBM Models are nowadays mainly used for word alignment
- Other word alignment models proposed e.g. HMM
- Shared task at NAACL 2003 and ACL 2005 workshops



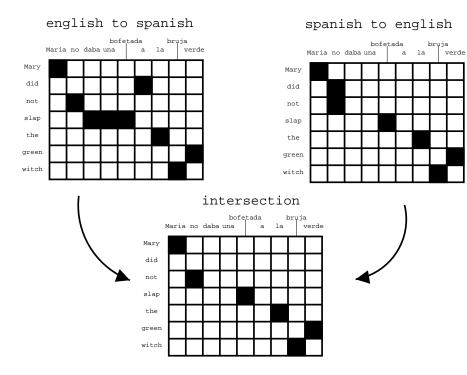


Word alignment with IBM models

- IBM Models create a *many-to-one* mapping
 - words are aligned using an alignment function
 - a function may return the same value for different input (one-to-many mapping)
 - a function can not return multiple values for one input (no many-to-one mapping)
- But we need *many-to-many* mappings



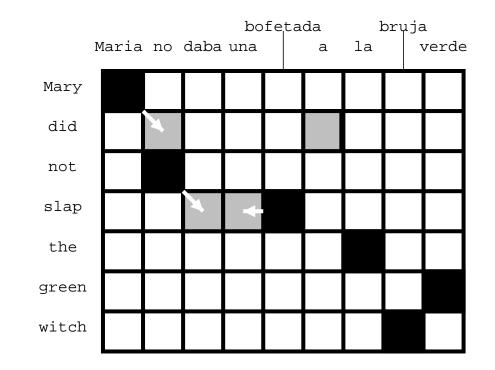
Symmetrizing word alignments



• *Intersection* of GIZA++ bidirectional alignments



Symmetrizing word alignments



• Grow additional alignment points [Och and Ney, CompLing2003]



Growing heuristic

```
GROW-DIAG-FINAL-AND(e2f,f2e):
  neighboring = ((-1,0),(0,-1),(1,0),(0,1),(-1,-1),(-1,1),(1,-1),(1,1))
  alignment = intersect(e2f,f2e);
  GROW-DIAG(); FINAL-AND(e2f); FINAL-AND(f2e);
GROW-DIAG():
  iterate until no new points added
    for english word e = 0 \dots en
      for foreign word f = 0 \dots fn
        if ( e aligned with f )
          for each neighboring point ( e-new, f-new ):
            if ( ( e-new not aligned or f-new not aligned ) and
                 (e-new, f-new) in union(e2f, f2e))
              add alignment point ( e-new, f-new )
FINAL-AND(a):
  for english word e-new = 0 ... en
    for foreign word f-new = 0 \dots fn
      if ( ( e-new not aligned and f-new not aligned ) and
           (e-new, f-new) in alignment a)
        add alignment point ( e-new, f-new )
```



More Recent Work

- Symmetrization during training
 - symmetrize after each iteration of IBM Models
 - integrate symmetrization into models
 - e.g. Liang, Taskar and Klein, NAACL 2006
- Discriminative training methods
 - supervised learning based on labeled data
 - semi-supervised learning with limited labeled data
 - e.g. Blunsom and Cohn, ACL 2006
- Better generative models
 - e.g. Fraser and Marcu, EMNLP 2007